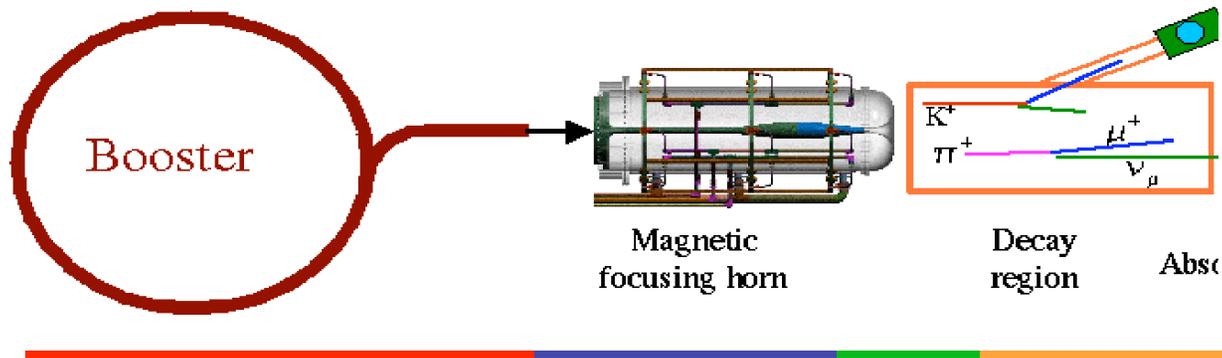


MiniBooNE beam simulation

Kendall Mahn

on behalf of those who did all this work

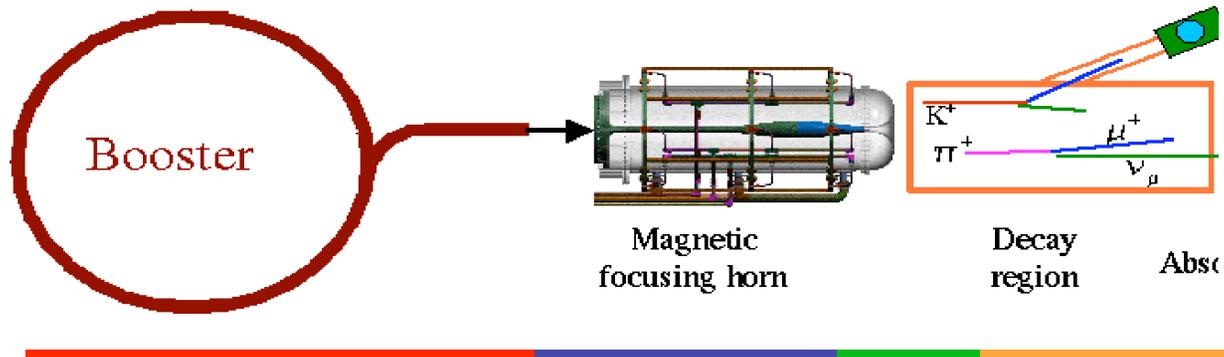


primary p+Be
interactions
 $\pi^{+/-}$, $K^{+/-}$, K^0
production

horn,
magnetic
field
modeling

secondary
interactions

neutrino
production



primary p+Be
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Primary (p+Be) interactions

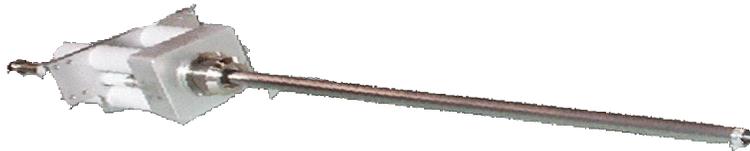
Proton beam and target

Beam protons produced around a mean position, angle, with gaussian smearing
central values of position, angle and spread (positional and directional)
based on beam position monitor information

Be target

7 “slugs” make a total of 1.7 interaction lengths

Target material, shape (including cooling fins)
included in simulation



Primary (p+Be) interactions

Beam Optics

Varying spread of beam in target changes the **relative efficiency** of an interaction by 1%

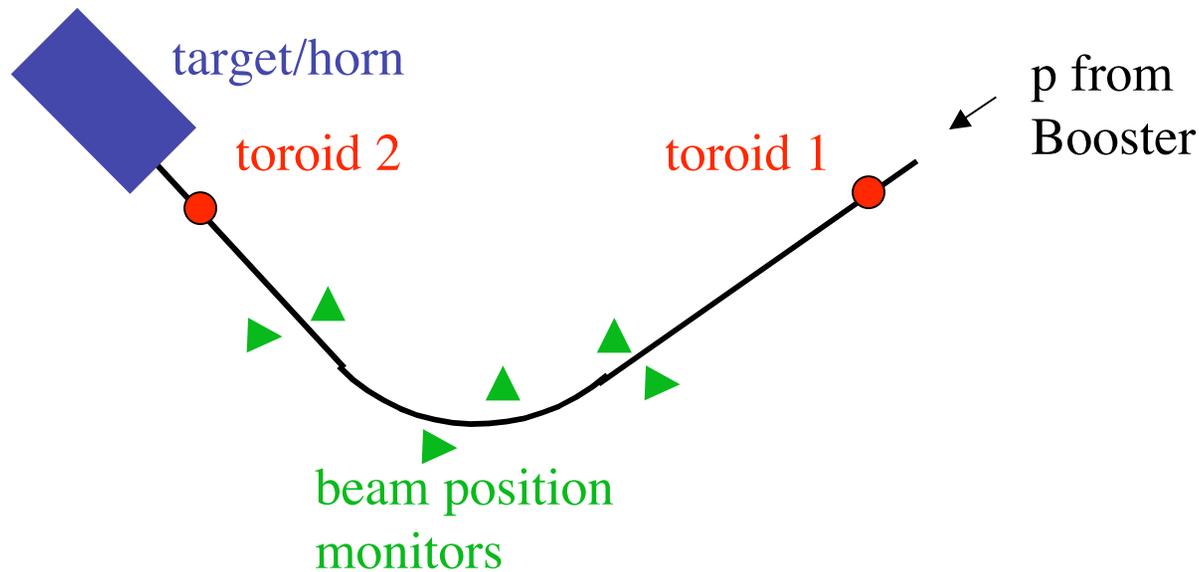
relative efficiency is how often a proton will or won't interact, roughly corresponds to how much the flux can change

Considered “pin” beam (no divergence or spread), perfectly focused beam, and different focus points

Primary (p+Be) interactions

Proton beam

- Absolute proton on target (p.o.t.) measured by two toroids upstream of the target
 - Two toroids measurements track each other well
 - Toroid drift main contributor to error
 - 3% total error on delivered p.o.t before March 2003, since then 1.7%



Primary (p+Be) interactions

p+Be cross sections

Protons then interact with the target, and either scatter or react to produce a meson

$$\sigma_{\text{total}} = \sigma_{\text{elastic}} + \sigma_{\text{inelastic}}$$

$$\sigma_{\text{inelastic}} = \sigma_{\text{quasi-elastic}} + \sigma_{\text{reaction}}$$

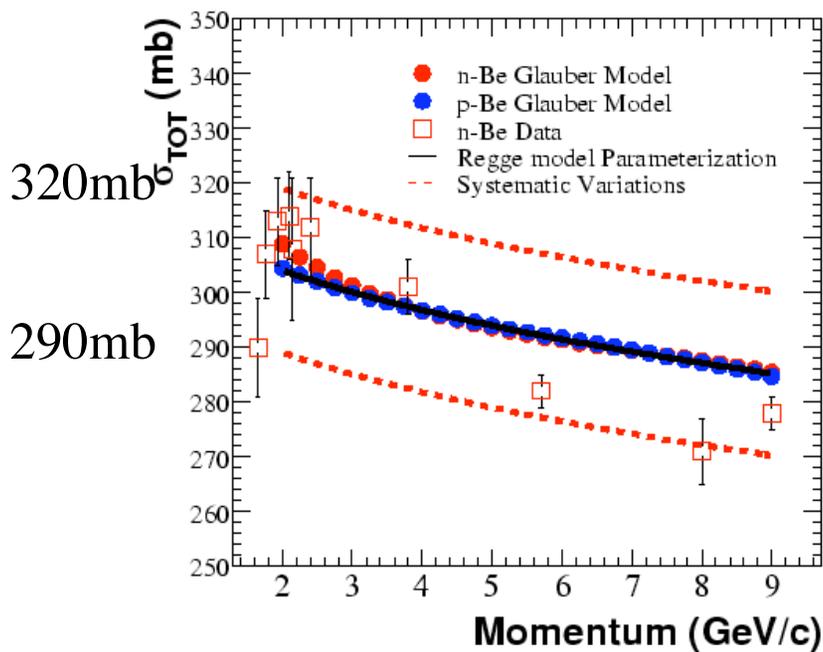
p+Be → p+...

p+Be → π, K+....

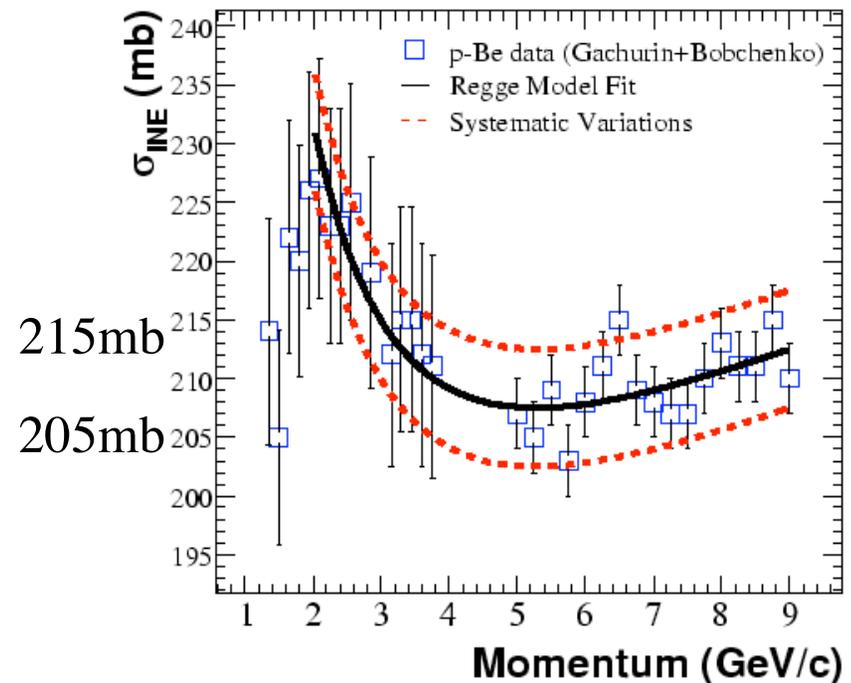
Primary (p+Be) interactions

p+Be cross sections

Measurements for σ_{total} , $\sigma_{\text{inelastic}}$



$$\sigma_{\text{total}} = 285 \pm 15 \text{ mb}$$



$$\sigma_{\text{inelastic}} = 212.4 \pm 5 \text{ mb}$$

$\Rightarrow 1\%$ change in reaction efficiency

Primary (p+Be) interactions

p+Be cross sections

$$\sigma_{\text{total}} = \sigma_{\text{elastic}} + \sigma_{\text{inelastic}}$$

$$\sigma_{\text{inelastic}} = \sigma_{\text{quasi-elastic}} + \sigma_{\text{reaction}}$$

Model dependent quantities:

σ_{elastic} range constrained by σ_{total} and $\sigma_{\text{inelastic}} \Rightarrow 1\%$

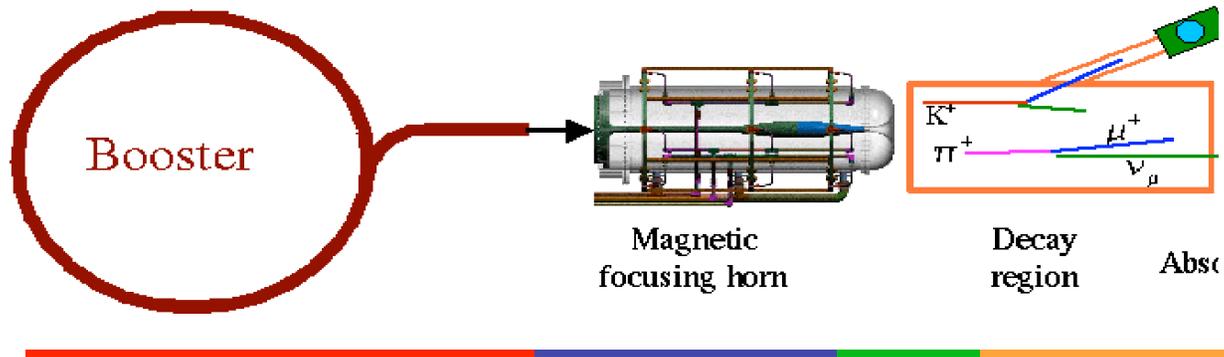
Variation of 30 mb for $\sigma_{\text{quasi-elastic}} \Rightarrow 2.5\%$

Kinematic variation in model

More forward going events see more target, material

$\Rightarrow <1\%$ change for σ_{elastic} , 2% for $\sigma_{\text{quasi-elastic}}$

Measure σ_{reaction} with differential cross sections



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Primary (p+Be) interactions

Differential cross sections of π, K

Various experiments have measured how often protons react to produce π, K

However, such data sets vary across proton beam energy, meson angle and momentum, as well as incident targets

=> Fit the differential cross section data sets with a parameterization function

Use of a parameterization allows for comparisons between data sets, as well as combining different data sets into one

Primary (p+Be) interactions

Sanford-Wang (S-W) Parametrization

MiniBooNE uses Sanford-Wang parametrization for the π, K fits

- Given the proton beam momentum (p_{beam}) and meson lab frame momentum (p) and angle (θ), can fit to data using c_1 - c_9
- Function based on Feynman scaling

$$\frac{d^2\sigma(p+A \rightarrow \pi^+ + X)}{dp d\Omega}(p, \theta) = c_1 p^{c_2} (c_9 - p/p_{\text{beam}}) \exp[-c_3 (p^{c_4}/p_{\text{beam}}^{c_5}) - c_6 \theta (p - c_7 p_{\text{beam}} \cos^c \theta)]$$

- c_9 represents mass threshold for kaons (=1 for pions)

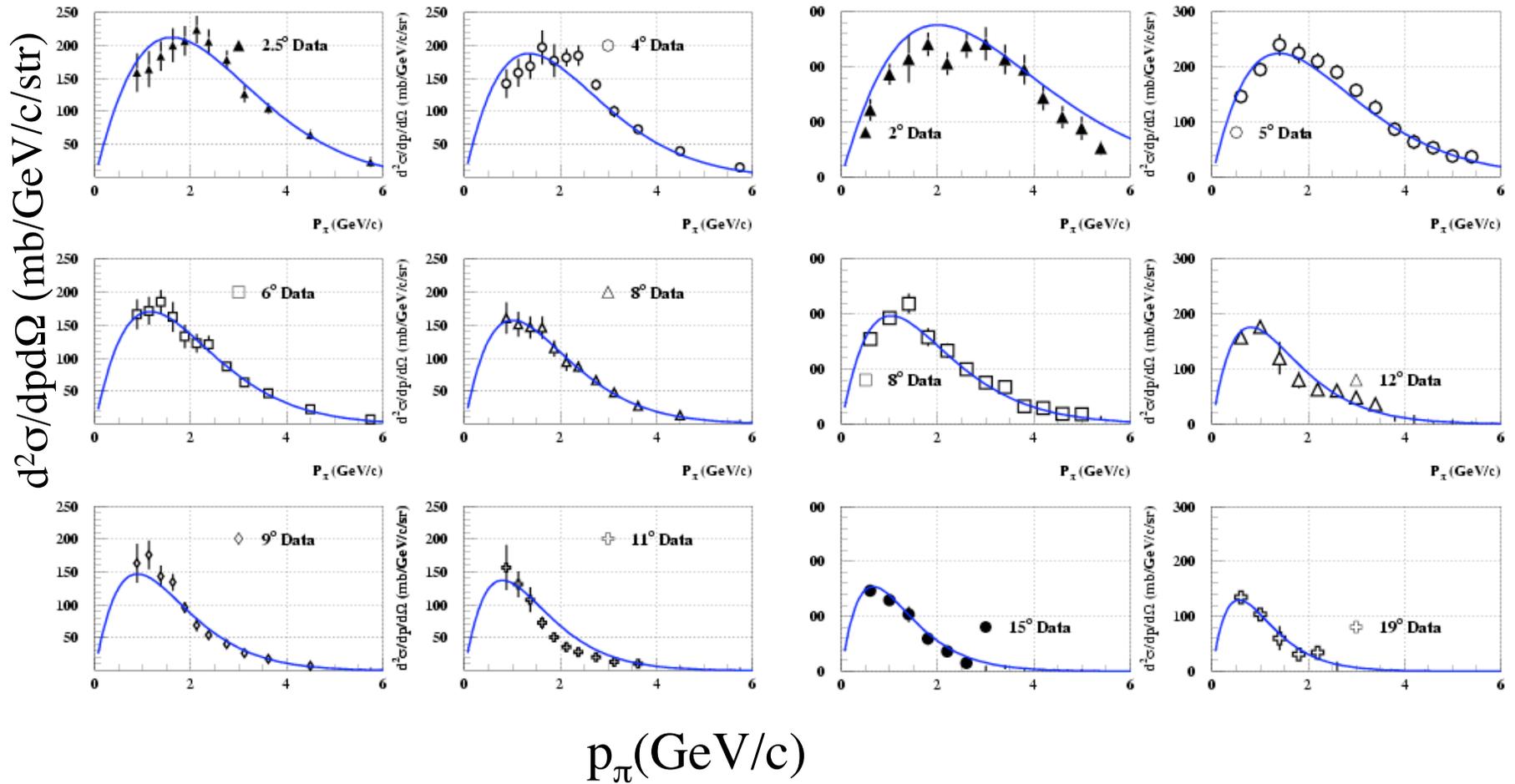
Errors are calculated based on the allowed 1σ variations in the c_i ; c_i correlations are included

π^+ external data

- Combined S-W fit to preliminary HARP 8.9 GeV and E910 6.4,12.3 GeV datasets
 - HARP is at correct beam energy, E910 provides some of the smallest angular bins
- E910 and HARP have similar normalization, some difference in shape of fits
- Fit pre-HARP is consistent with current fit including HARP

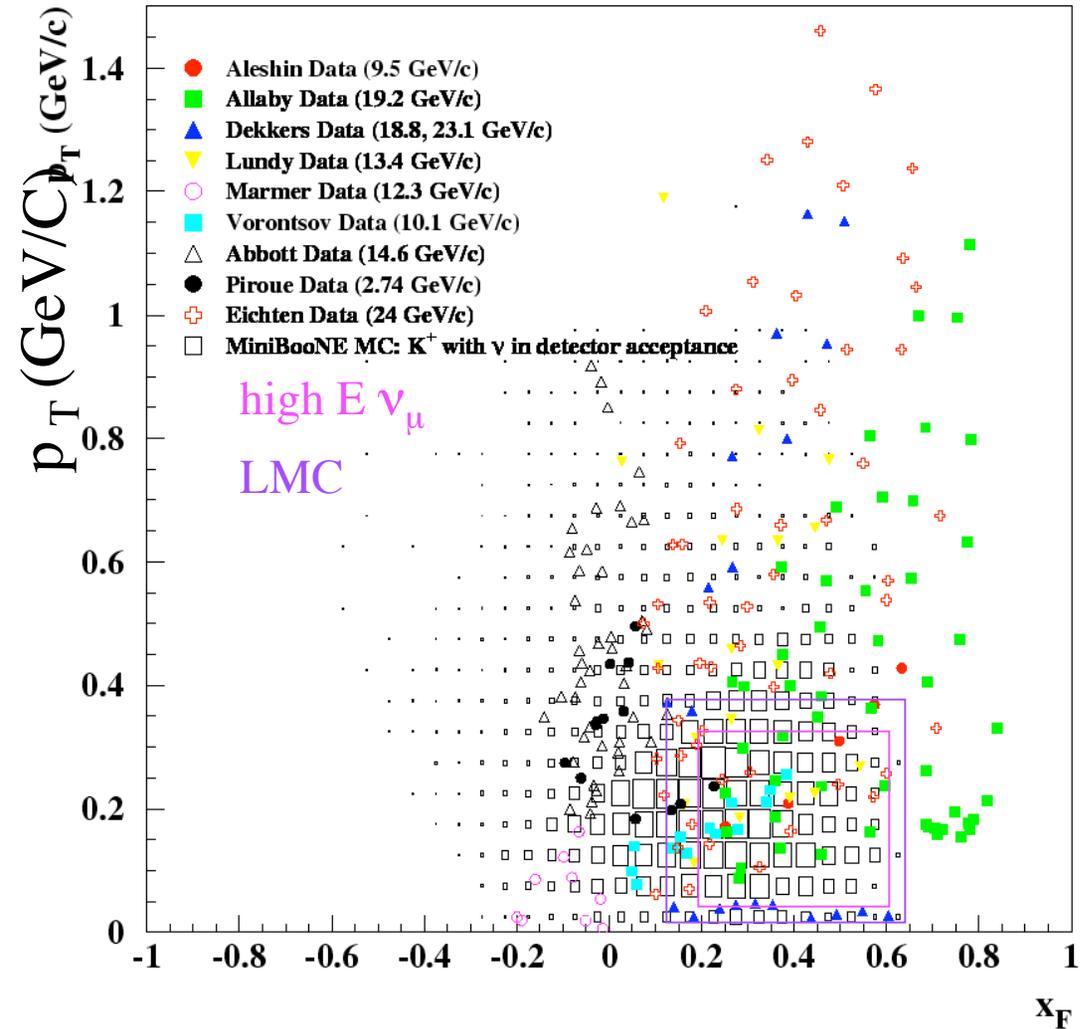
π^+ external data

HARP (preliminary) 8.9 GeV Combined S-W fit E910 12.3 GeV



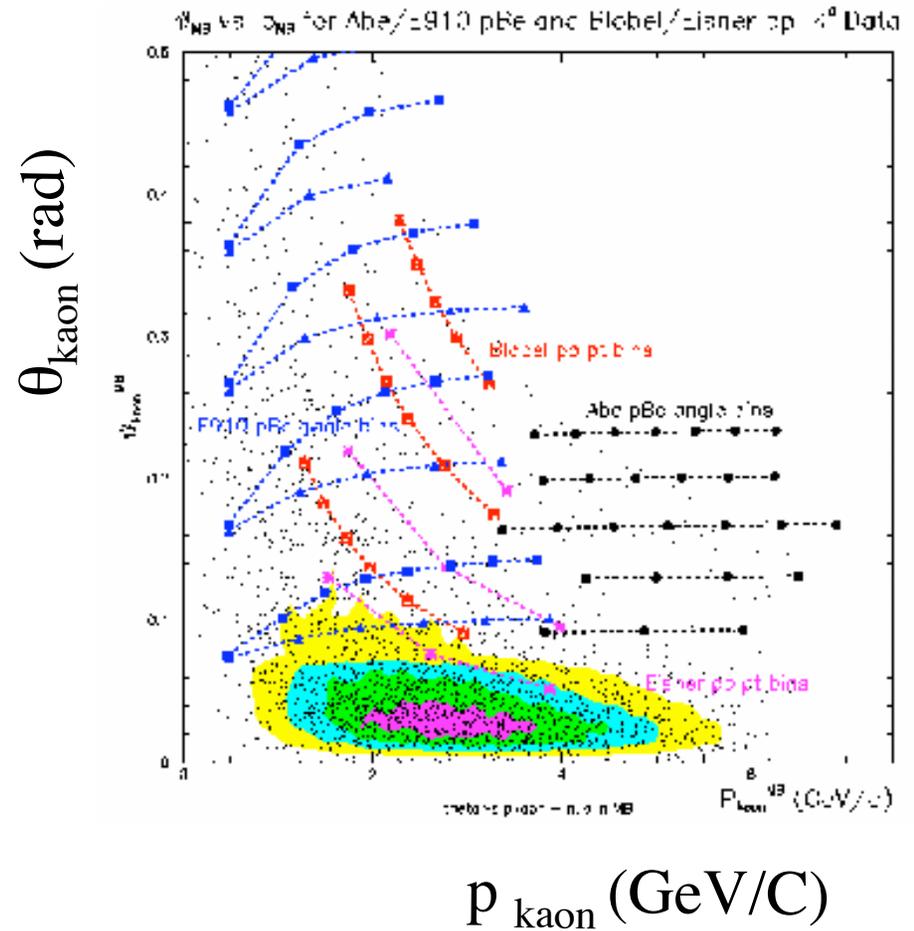
K⁺ external data

- Currently use Aleshin, Abbot, Eichten and Vorontsov data
- K⁺ flux shape fixed by fit, normalization determined by beam data
 - LMC, high E ν_μ
- HARP will make a measurement of kaon production on Be in the next year



K⁰ external data

- K⁰ data sets: **E910** 12.3,17.6, Abe 12 GeV/c
 - Other data sets exist (**Eisner**, 6.0 GeV/c, **Blobel**, 12,24 GeV/c) but p-p not p-Be

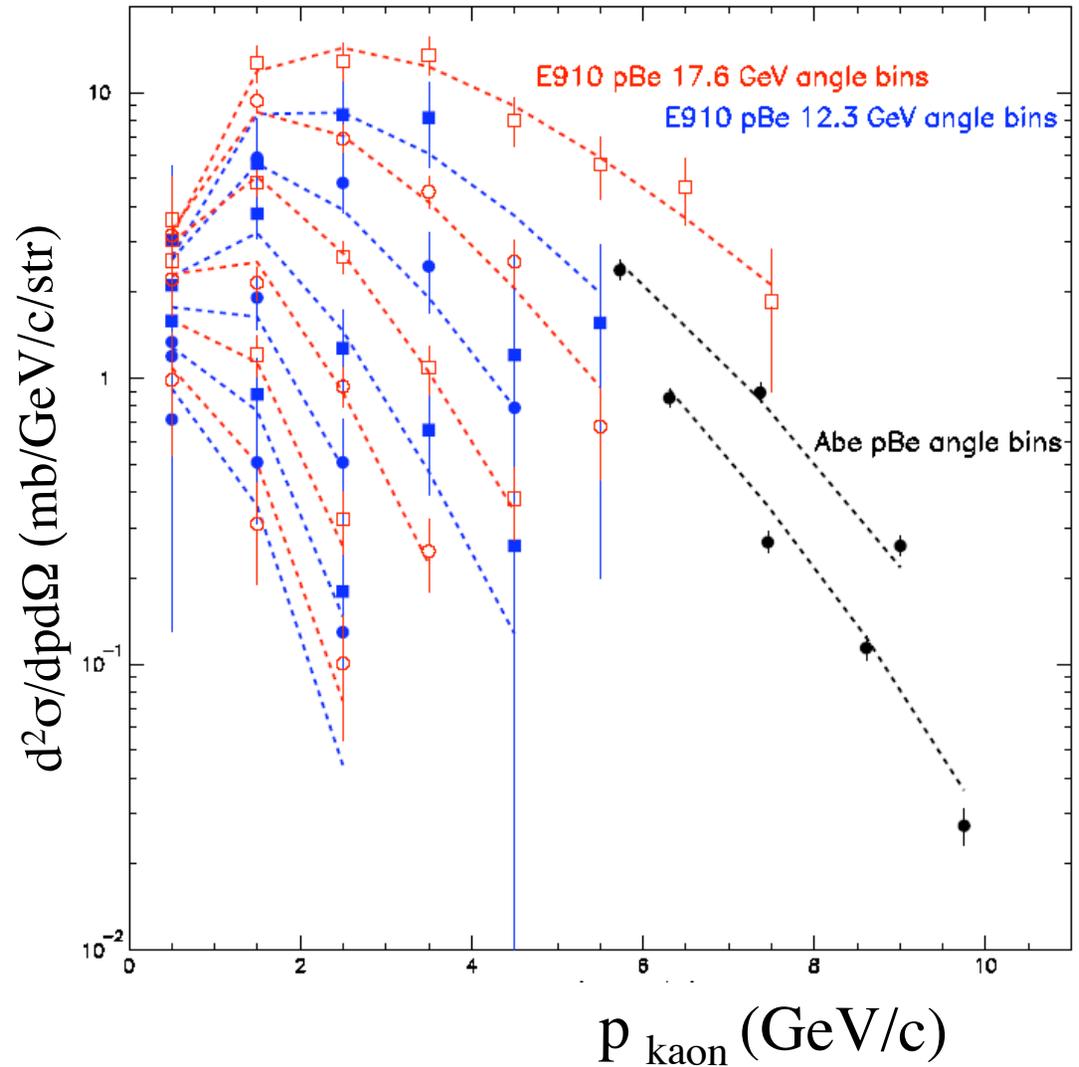


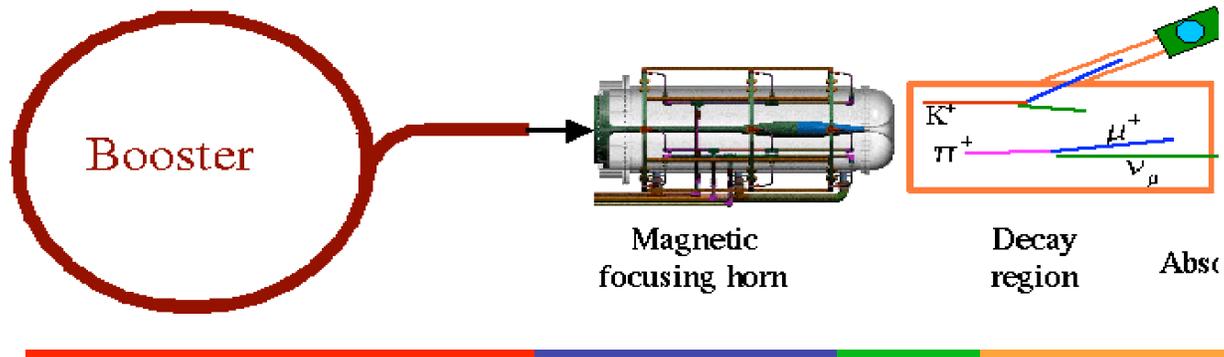
K⁰ external data

S-W fit -----

E910 12.3, 17.6, Abe

- S-W fit constrains K⁰ to 26% level
- K⁰ normalization and shape are set by this fit
 - K⁰ ν_e s only compose <10% of c₁ sample



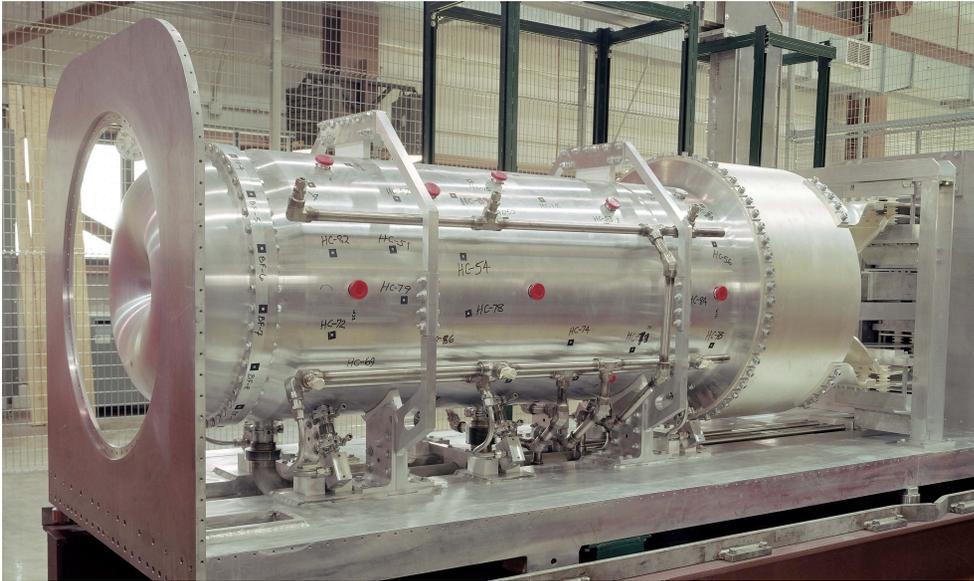


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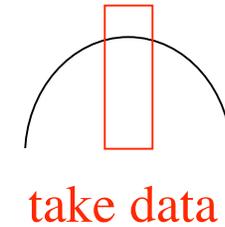
horn
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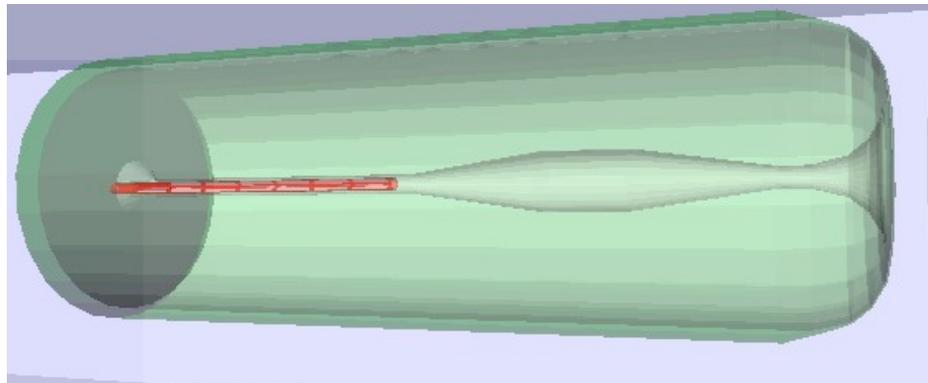
Magnetic horn



Horn is
pulsed at
174 kA
for 141 μ s



Geometry in
Geant3
(converted to
Geant4)

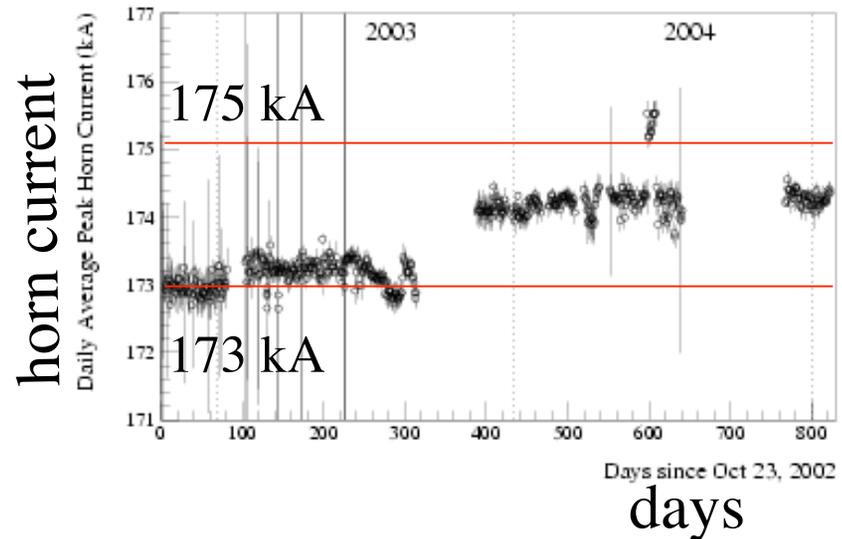


NBI 5-9 Sept 2006

K. Mahn

Horn current

- Absolute current measurement of 174 kA
 - value measured by current transformers to 0.5% level
 - => consider variations of **+/- 1kA**
 - Most effect at high energy



- Horn current pulse timing
 - Horn pulse peak arrives when protons do
 - Current delivery timing is stable over time

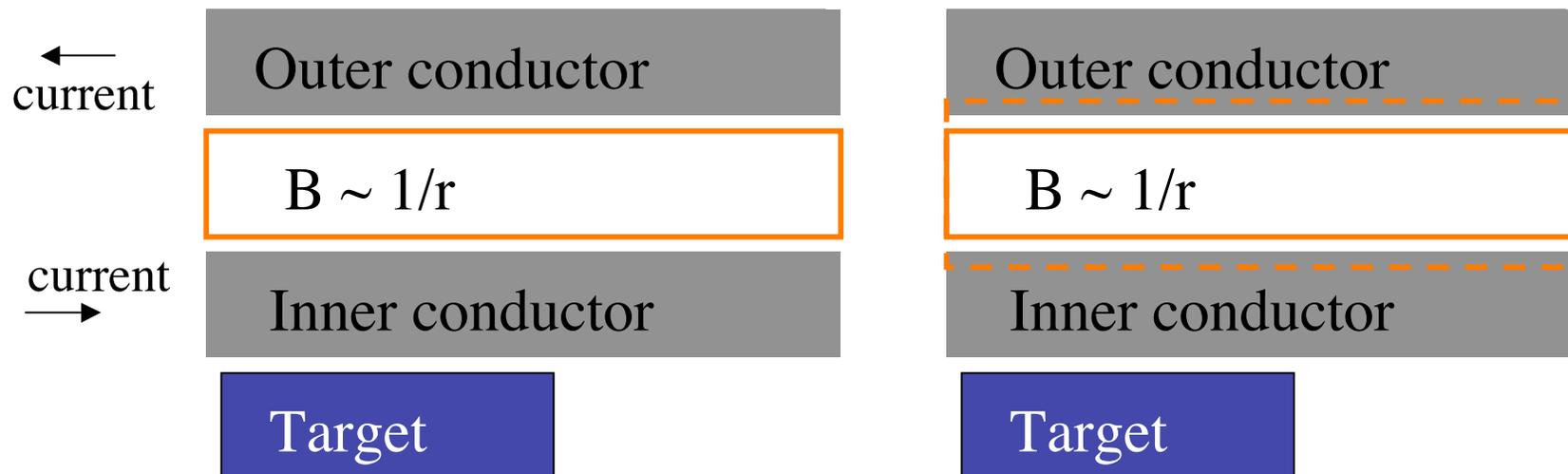
Horn

Electromagnetic field model

- In a perfect conductor, the magnetic field does not enter the conductor
- In reality, the field can be nonzero into the surface of the conductor, this is called “the skin depth effect”

Perfect!

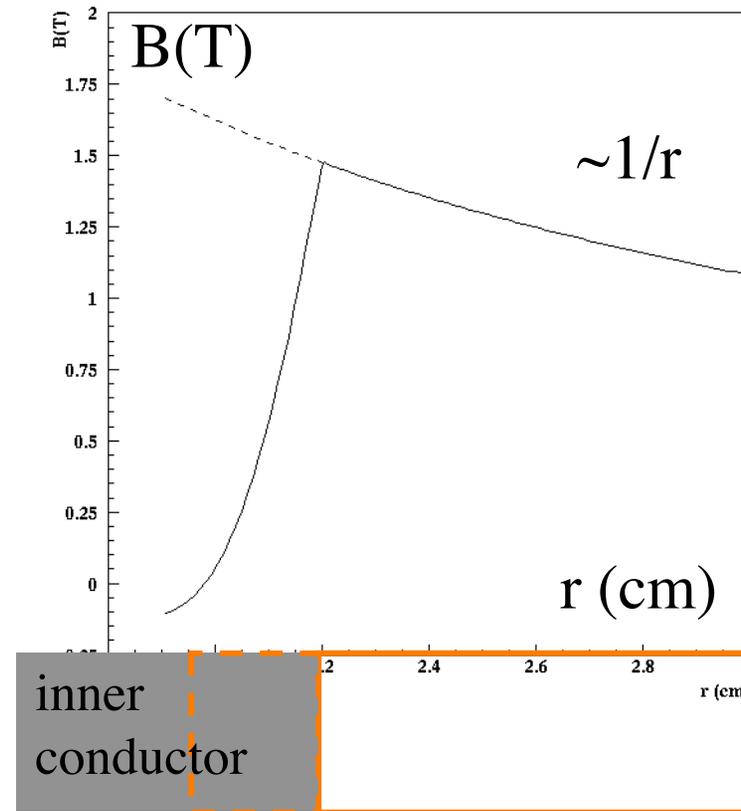
Realistic

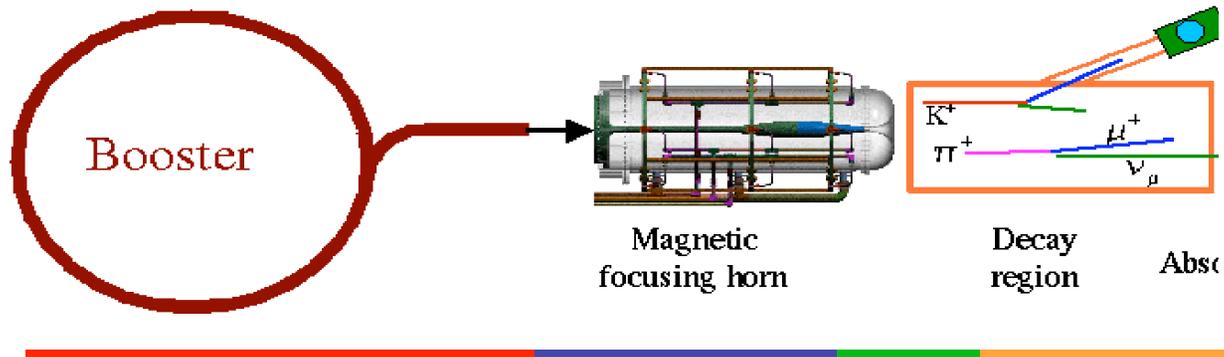


Horn

Electromagnetic field model

- Measurements of MiniBooNE horn across voltage, radius consistent w/ $1/r$
- Measured field on the inner surface of conductor on NuMI horn to be small
- Field penetration (modeled as an exponential decay) in conductor has **no substantial effect on normalization**





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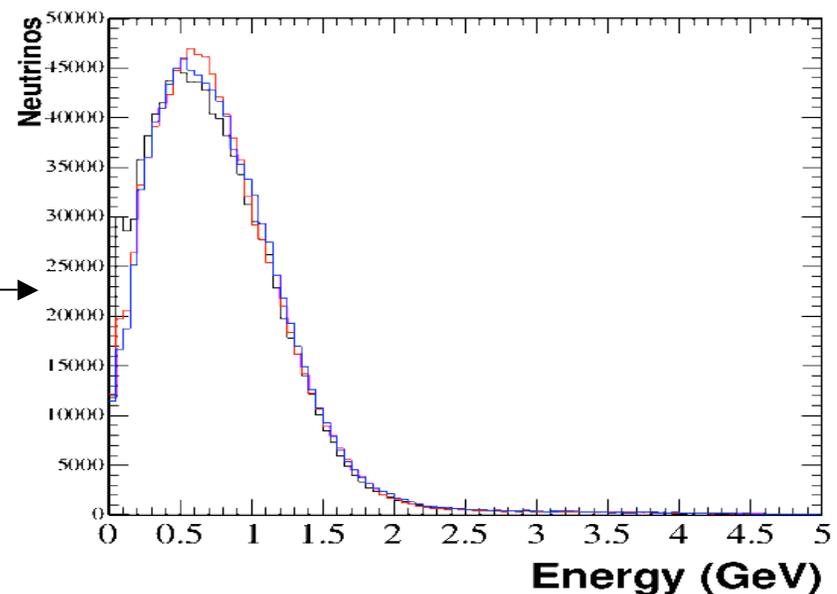
Secondary Interactions

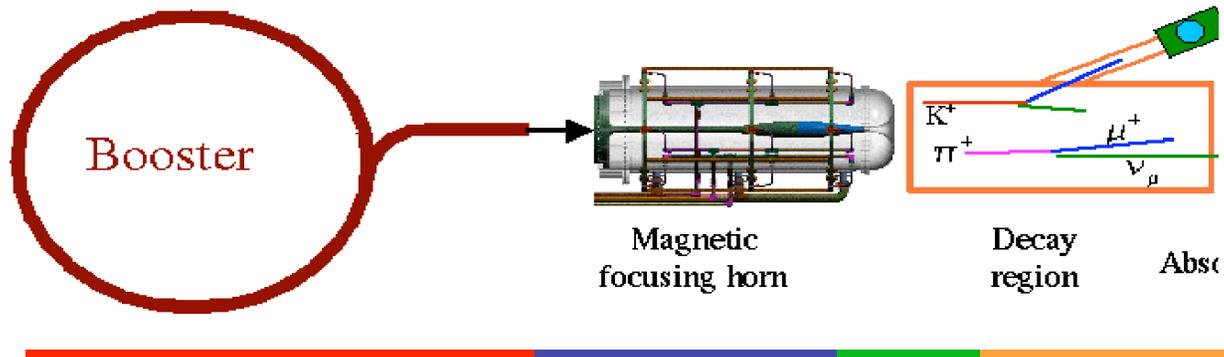
17% of all protons interact twice

7% of ν_μ come from $p \rightarrow p \rightarrow \pi$

Additionally, pions and kaons can interact with the horn, target or concrete

- Changing the secondary production models has a minimal effect on the neutrino flux
 - GHEISHA, Bertini, Binary cascade models similar
- HARP has the ability to measure both proton and meson interactions on Be
- Thick target data will check current model as well





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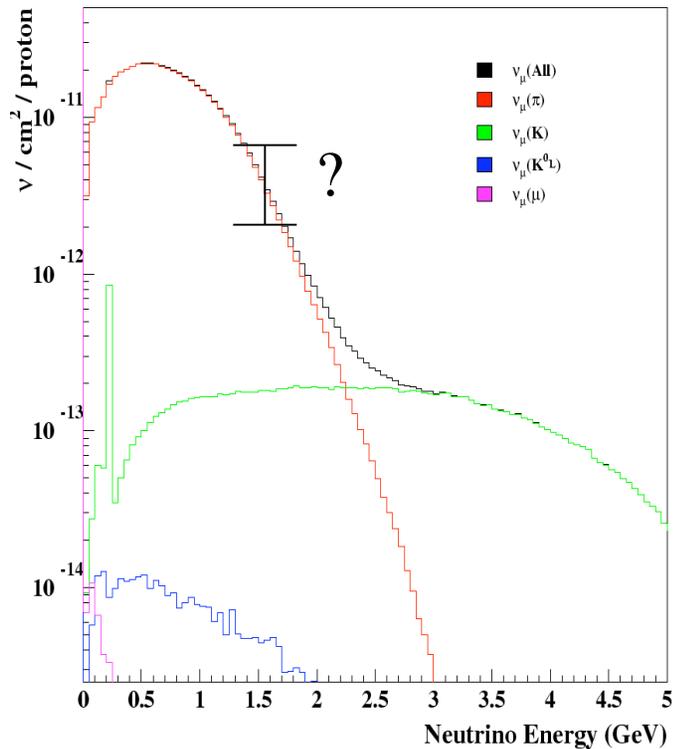
secondary
interactions

neutrino
production

Meson decay to neutrinos

- Mesons don't always decay to neutrinos (absorption, scattering); neutrinos don't always hit our detector
- To help boost statistics, we use “redecay”
 - Every meson that decays to a neutrino is saved
 - It is decayed ~ 1000 s of times with the same meson momentum, position and decay mode
 - Muon polarization is taken into account
 - Neutrino's position, direction is maintained when it interacts at detector
- More events are produced for sparse kinematic regions, but with a corresponding lower weight
 - Statistics can cause fluctuations which redecay can amplify
 - One pion producing a neutrino at 7 GeV, but no neutrinos from pions of slightly different momentum, angle, now there's 1000 of them
 - Reweight events after redecay to produce a smooth flux

Beam Monte Carlo Predicted ν_μ Fluxes



Lots of work put into understanding the primary parts of neutrino production

– Hadron production by HARP extremely valuable

A neutrino flux only has meaning with an associated error and scale of that error

– absolute p.o.t, beam optics, p+Be cross sections, Sanford-Wang parametrization, horn current, skin depth, secondary interactions and geometry all considered
– Still working!

Geometry of beamline

- Distance from target/horn to detector verified by:
 - surveyors
 - walking
 - driving
 - Google Maps
- Only “large” (noticeable) shifts would produce a significant effect on the flux
 - Shifting the target by 23 cm -> 8% change in flux
 - Shifting collimator by 1 m further down -> 1% change in flux
 - Increasing decay pipe diameter by 4 inches -> 4% change in flux
 - Increasing the length of the horn by 10cm -> 1% change in flux

References

- Toroid calibration/checks: J. Monroe thesis
- Sanford-Wang parameterization: J. R. Sanford and C.L.Wang “Empirical formulas for particle production in p-Be collisions between 10 and 35 BeV/c”, Brookhaven National Laboratory, AGS internal report, (1967) (unpublished)
- p+Be cross sections (total)
 - Bellettini et al., Nucl. Phys. 79 (1966) 609-624
- p+Be cross sections (inelastic)
 - V. V. Gachurin et al., ITEP-59-1985
 - B.M. Bobchenko et al., Sov. J. Nucl. Phys. 30, 805 (1979) [Yad. Fiz. 30, 1553 (1979)].
- E910, HARP: publications in progress