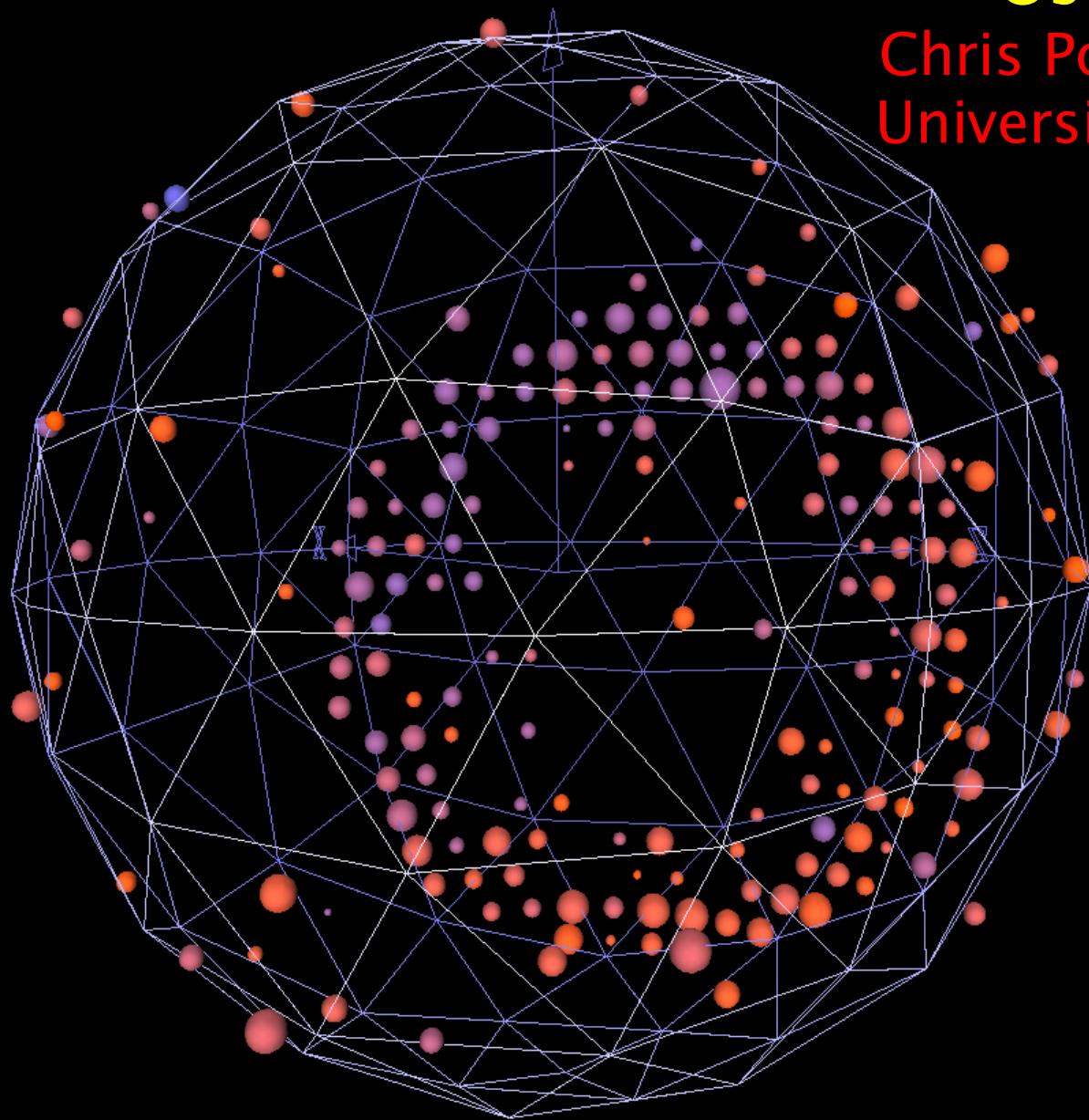


Details of the MiniBooNE Oscillation Results

Chris Polly, Indiana University
University of Chicago Seminar



The MiniBooNE Collaboration

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Z. Djurcic, D. A. Finley, B. T. Fleming, R. Ford, F. G. Garcia,
G. T. Garvey, J. A. Green, C. Green, T. L. Hart, E. Hawker,
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I. Kourbanis, S. Koutsoliotas, J. M. Link, Y. Liu, Y. Liu,
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W. Metcalf, P. D. Meyers, F. Mills, G. B. Mills, J. Monroe,
C. D. Moore, R. H. Nelson, P. Nienaber, S. Ouedraogo,
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University of Alabama
Bucknell University
University of Cincinnati
University of Colorado
Columbia University
Embry Riddle University
Fermilab
Indiana University

Los Alamos National Laboratory
Louisiana State University
University of Michigan
Princeton University
Saint Mary's University of Minnesota
Virginia Polytechnic Institute
Western Illinois University
Yale University



Thanks to Frank Merritt for the invitation...



Neutrino Oscillations

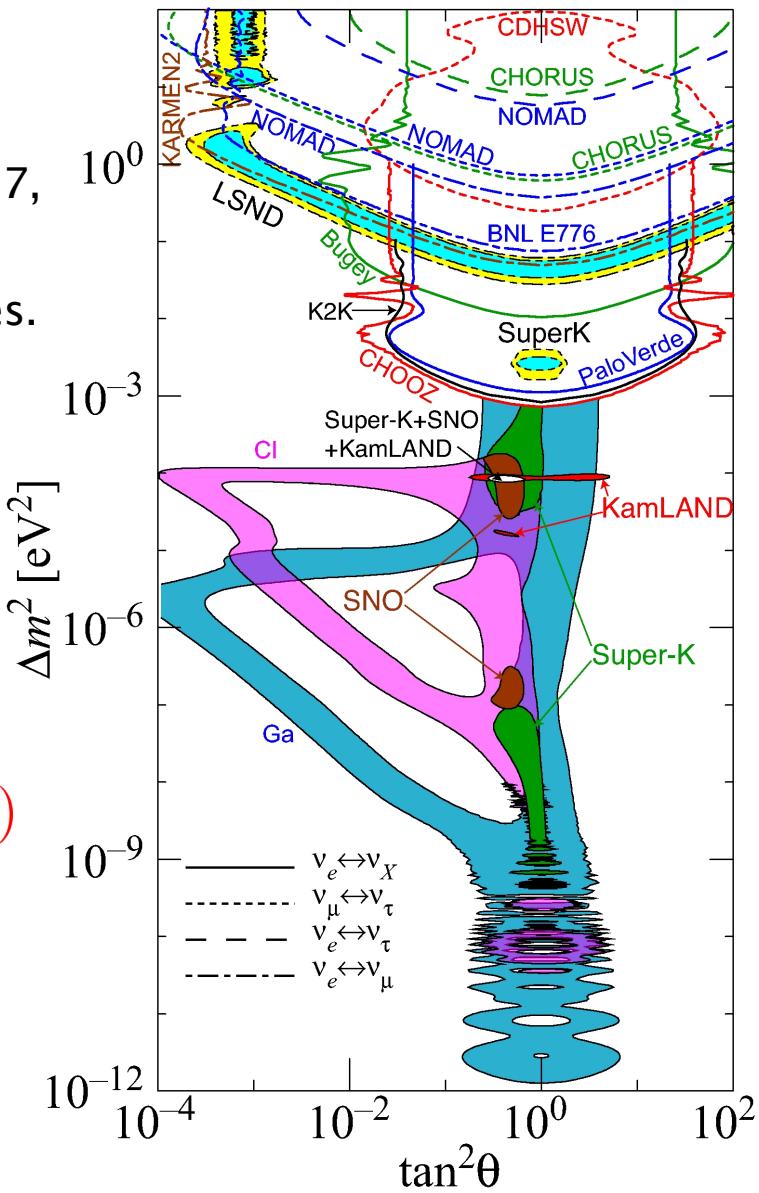
- ν oscillations first postulated by Pontecorvo in 1957, based on analogy to kaons.
- A non-zero ν mass allows for lepton flavor changes.
- mass eigenstates \neq flavor eigenstates:

$$|\nu_\alpha\rangle = \sum_i U_{\alpha i}^* |\nu_i\rangle \quad \alpha = (e, \mu, \tau)$$

- Flavor composition changes as ν propagates.
- Reducing to simple 2-neutrino mixing:

$$P(\nu_\alpha \rightarrow \nu_\beta) = \sin^2(2\theta) \sin^2(1.27\Delta m^2 L/E)$$

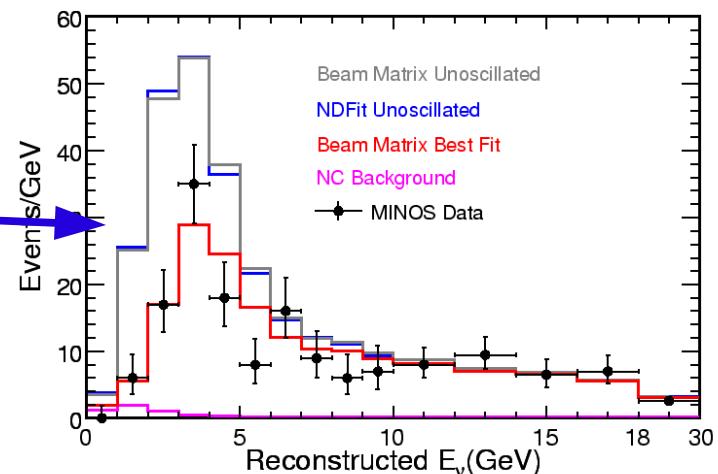
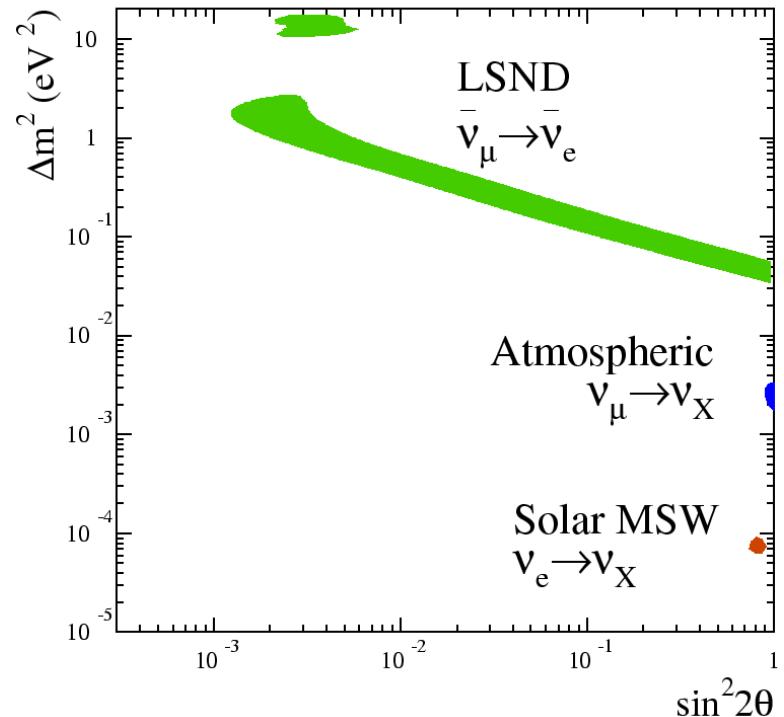
- Many experiments have hunted for ν oscillations, **some have found them!**



<http://hitoshi.berkeley.edu/neutrino>

Evidence for ν oscillations

- First evidence came in 1968 from Davis' solar ν_e experiment
 - found 1/3 of the expected ν_e from sun
 - disappearance $\nu_e \rightarrow \nu_x$
 - $\Delta m_{12}^2 \sim 8 \times 10^{-5} \text{ eV}^2$, $\sin^2(2\theta) \sim 0.8$
 - Confirmed by SNO, Super-K, Kamland
- New mixing found by Super-K through atmospheric ν_μ oscillations
 - found 1/2 as the upward ν_μ as downward
 - disappearance $\nu_\mu \rightarrow \nu_x$
 - $\Delta m_{23}^2 \sim 2 \times 10^{-3} \text{ eV}^2$, $\sin^2(2\theta) \sim 1.0$
 - Confirmed by SNO, IMB, Soudan, K2K, and most recently MINOS
- Only one unconfirmed observation!

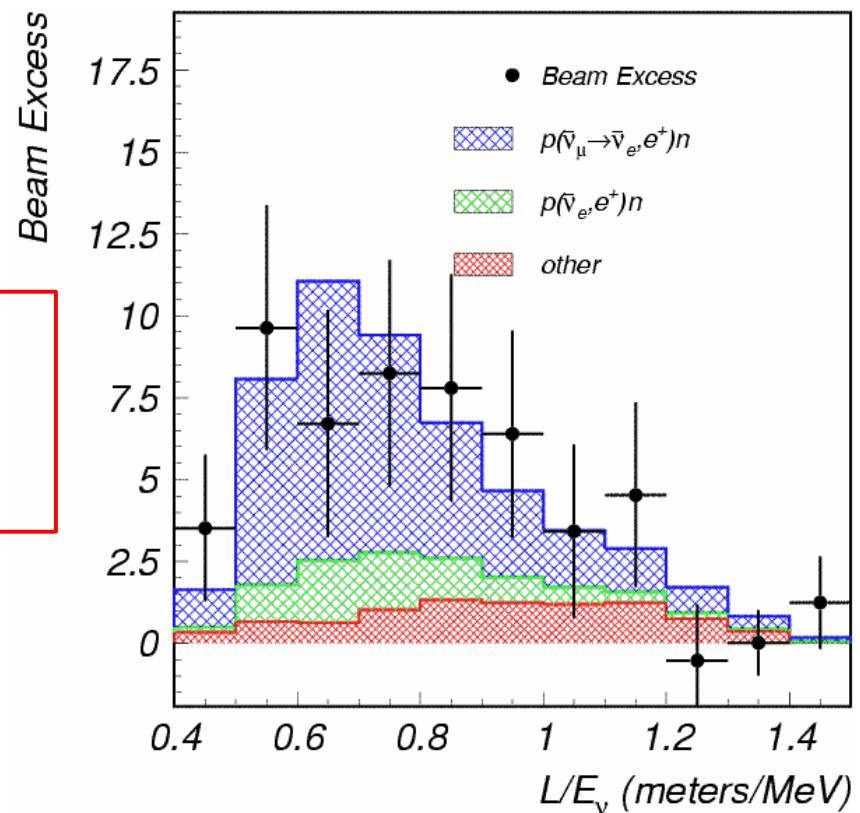


MiniBooNE's motivation...LSND

- LSND found an excess of $\bar{\nu}_e$ in $\bar{\nu}_\mu$ beam
- Signature: Cerenkov light from e^+ with delayed n-capture (2.2 MeV)
- Excess: $87.9 \pm 22.4 \pm 6.0$ (3.8σ)

- Under a 2ν mixing hypothesis:

$$P(\bar{\nu}_\mu \rightarrow \bar{\nu}_e) = \sin^2(2\theta) \sin^2\left(\frac{1.27 L \Delta m^2}{E}\right)$$
$$= 0.245 \pm 0.067 \pm 0.045 \%$$



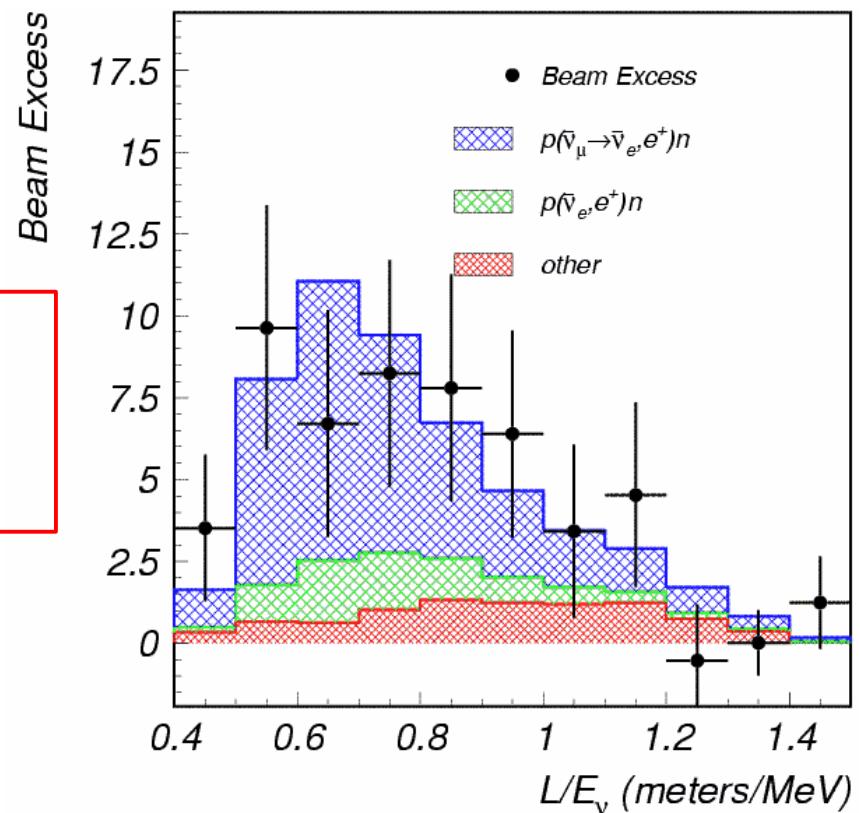
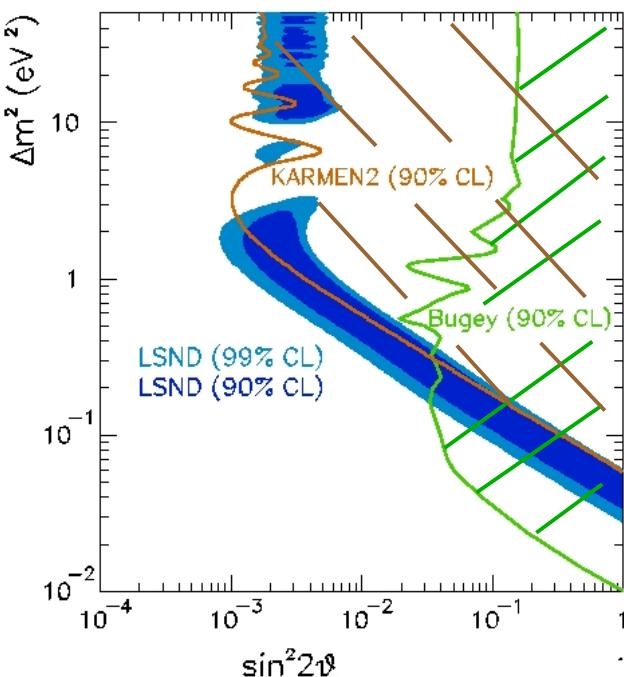
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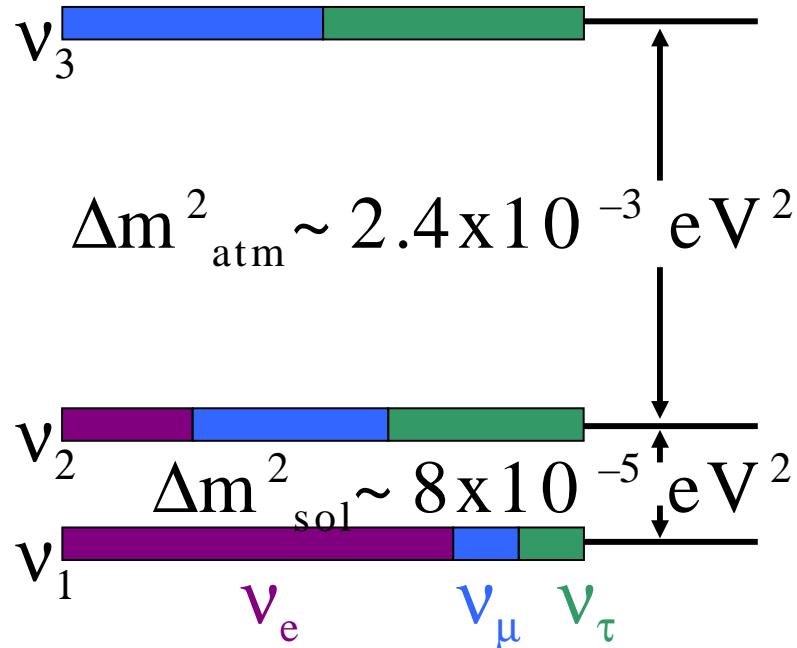
$$= 0.245 \pm 0.067 \pm 0.045 \%$$



- Other experiments, i.e. Karmen and Bugey, have ruled out portions of the LSND signal
- MiniBooNE was designed to cover the entire LSND allowed region

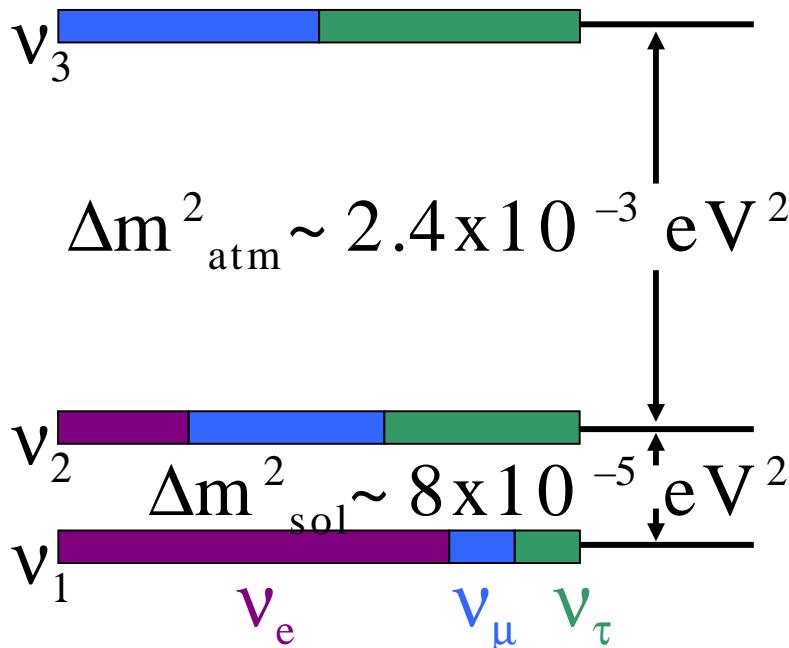


Interpreting the LSND signal



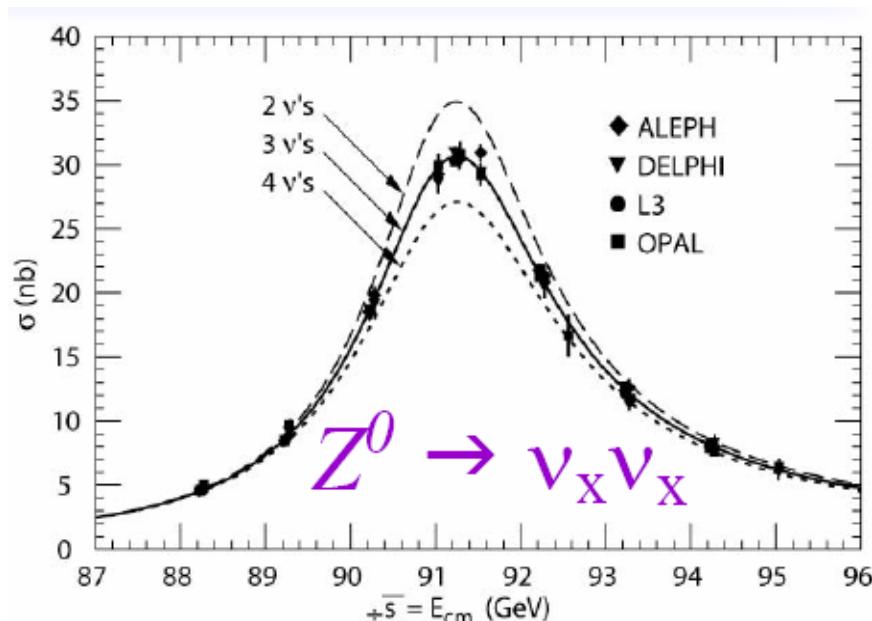
- The other two measured mixings fit conveniently into a 3-neutrino model
- With $\Delta m_{13}^2 = \Delta m_{12}^2 + \Delta m_{23}^2$, the LSND $\Delta m^2 \sim 1 \text{ eV}^2$ does not fit
- 'Simplest' explanation...a 4th neutrino

Interpreting the LSND signal

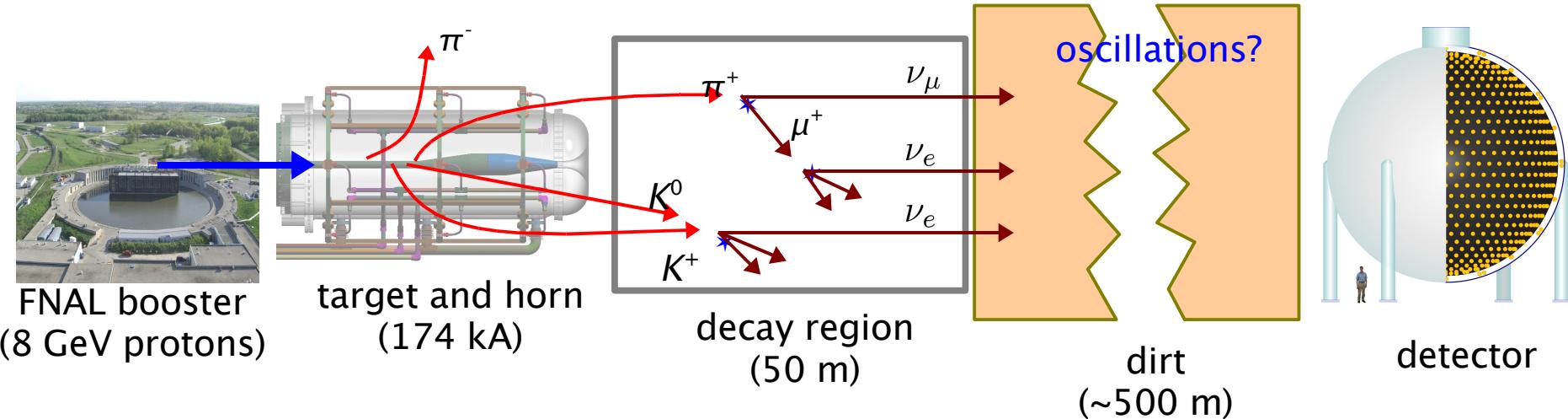


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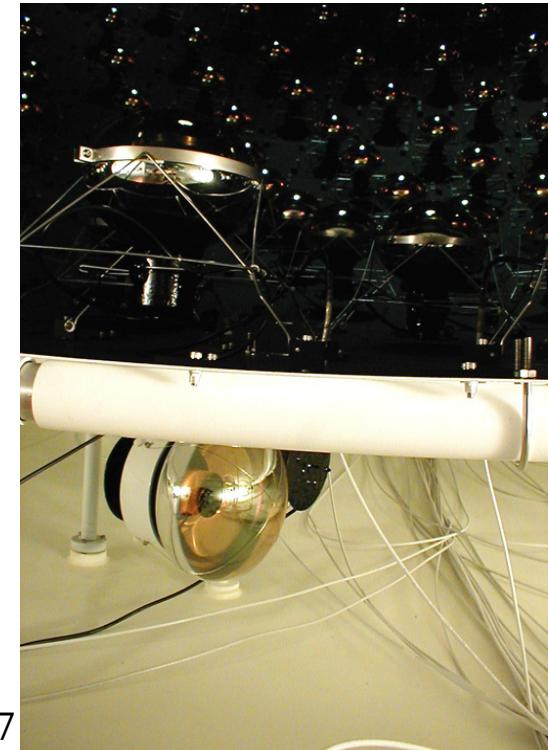
- Width of the Z implies $2.994 + 0.012$ light neutrino flavors
- Requires 4th neutrino to be 'sterile' or an even more exotic solution
 - Sterile neutrinos [hep-ph/0305255](#)
 - Neutrino decay [hep-ph/0602083](#)
 - Lorentz/CPT violation [PRD\(2006\)105009](#)
 - Extra dimensions [hep-ph/0504096](#)



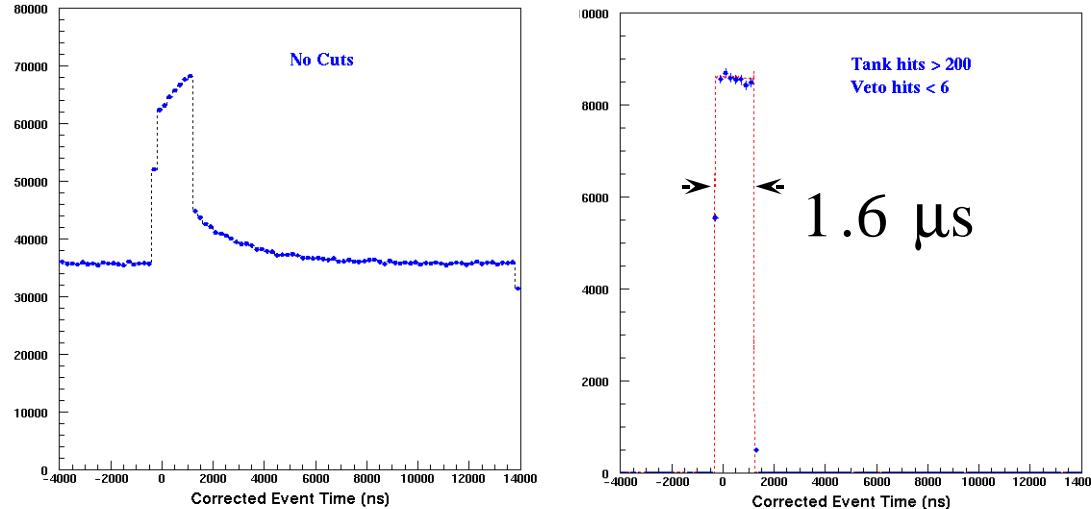
The MiniBooNE design strategy



- Start with 8 GeV proton beam from FNAL Booster
- Add a 174 kA pulsed horn to gain a needed $\times 6$
- Requires running ν (not anti- ν) to get flux
- Pions decay to ν with E_ν in the 0.8 GeV range
- Place detector to preserve LSND L/E:
 - MiniBooNE: (0.5 km) / (0.8 GeV)
 - LSND: (0.03 km) / (0.05 GeV)
- Detect ν interactions in 800T pure mineral oil detector
 - 1280 8" PMTs provide 10% coverage of fiducial volume
 - 240 8" PMTs provide active veto in outer radial shell



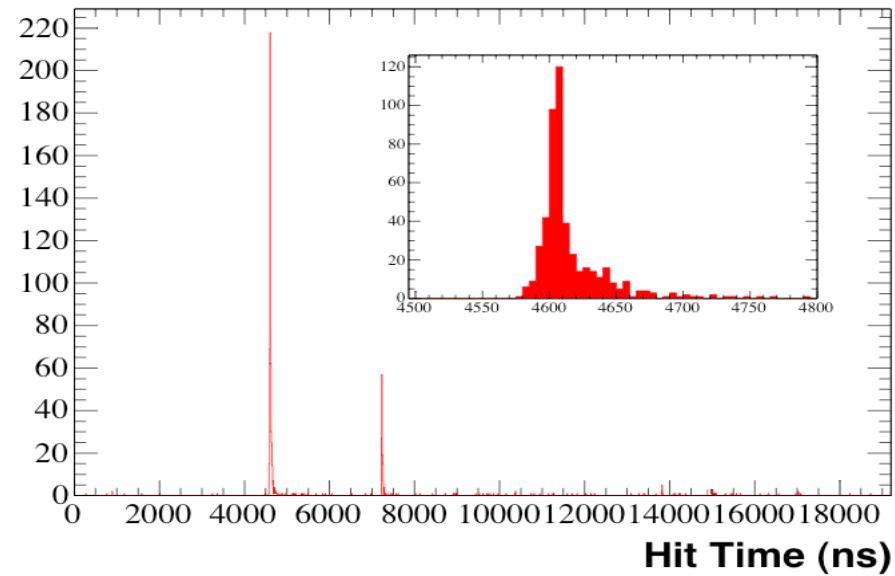
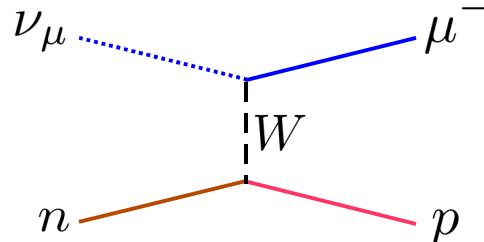
Simple cuts eliminate random backgrounds



- Left: trigger window, no cuts
- Right: Simple cuts applied PMT hits in veto < 6 and tank > 200 show clean beam window
- Removes cosmic μ and their decay electrons

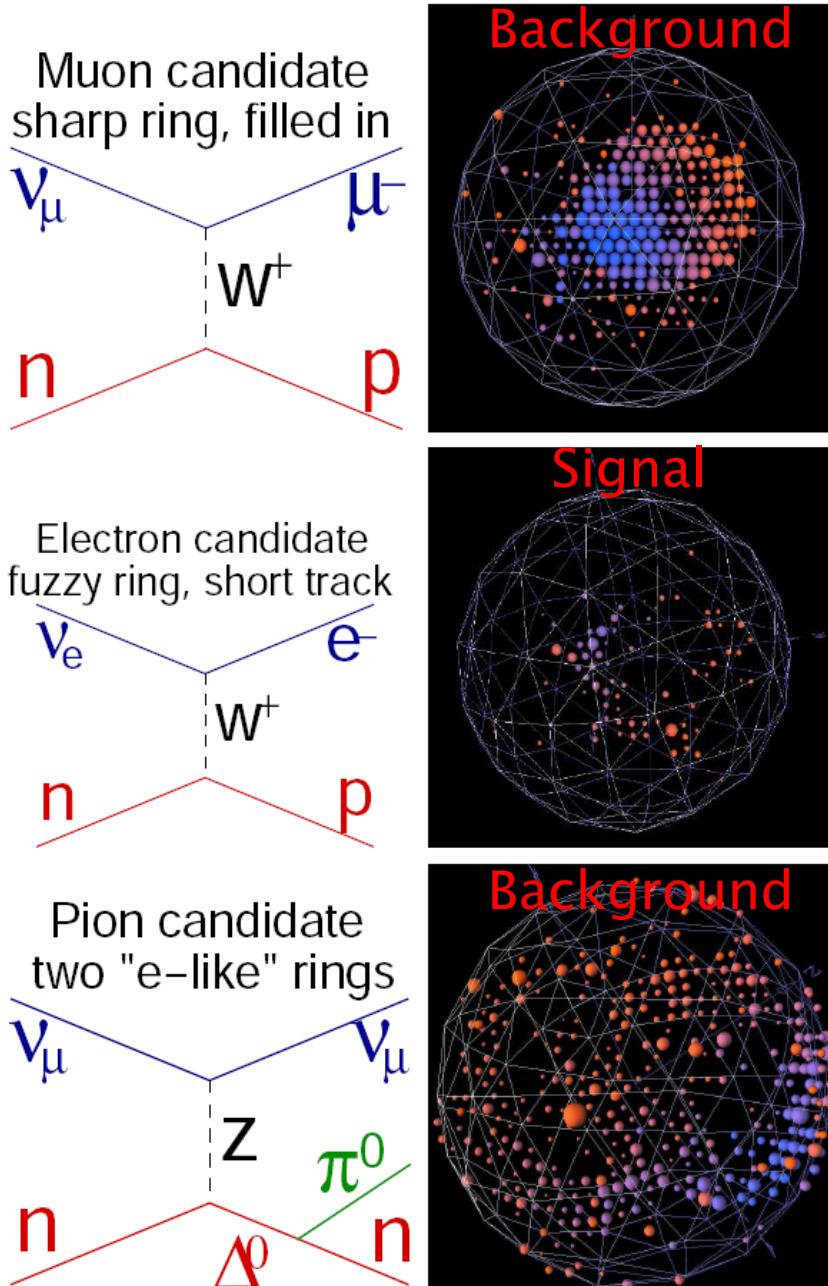
- Subevent structure (clusters in time) can be used for particle identification (PID)
- 2 subevent time structure expected for most common ν interaction in MB:

ν_μ CCQE (charged-current quasi-elastic)

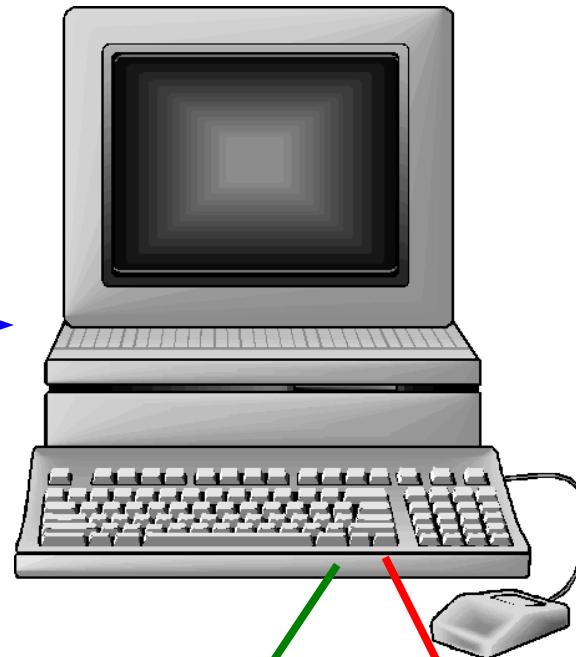
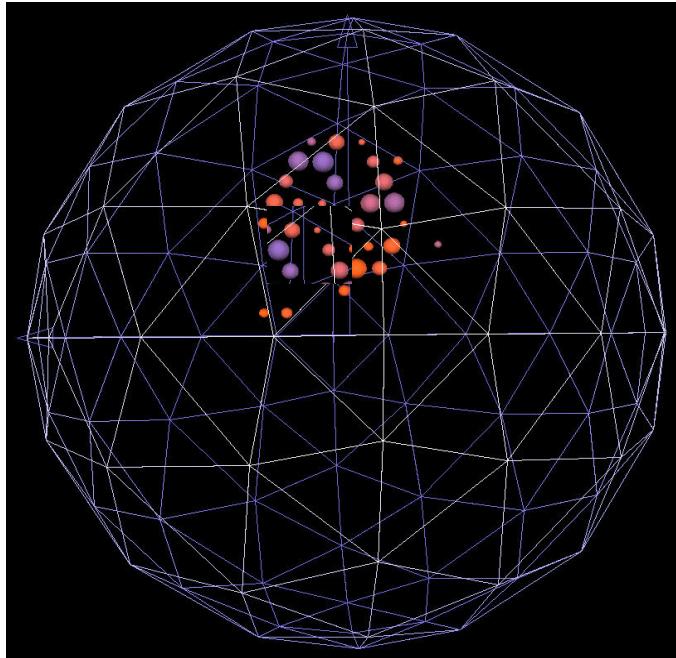


Key points about the signal

- LSND oscillation probability is $< 0.3\%$
- After cuts, MiniBooNE has to be able to find ~300 ν_e CCQE interactions in a sea of ~150,000 ν_μ CCQE
- Intrinsic ν_e background
 - Actual ν_e produced in the beamline from muons and kaons
 - Irreducible at the event level
 - E spectrum differs from signal
- Mis-identified events
 - ν_μ CCQE easy to identify, i.e. 2 "subevents" instead of 1. However, lots of them.
 - Neutral-current (NC) π^0 and radiative Δ are rarer, but harder to separate
 - Can be reduced with better PID
- MiniBooNE is a ratio measurement with the ν_μ constraining flux X cross-section



Blind analysis in MiniBooNE



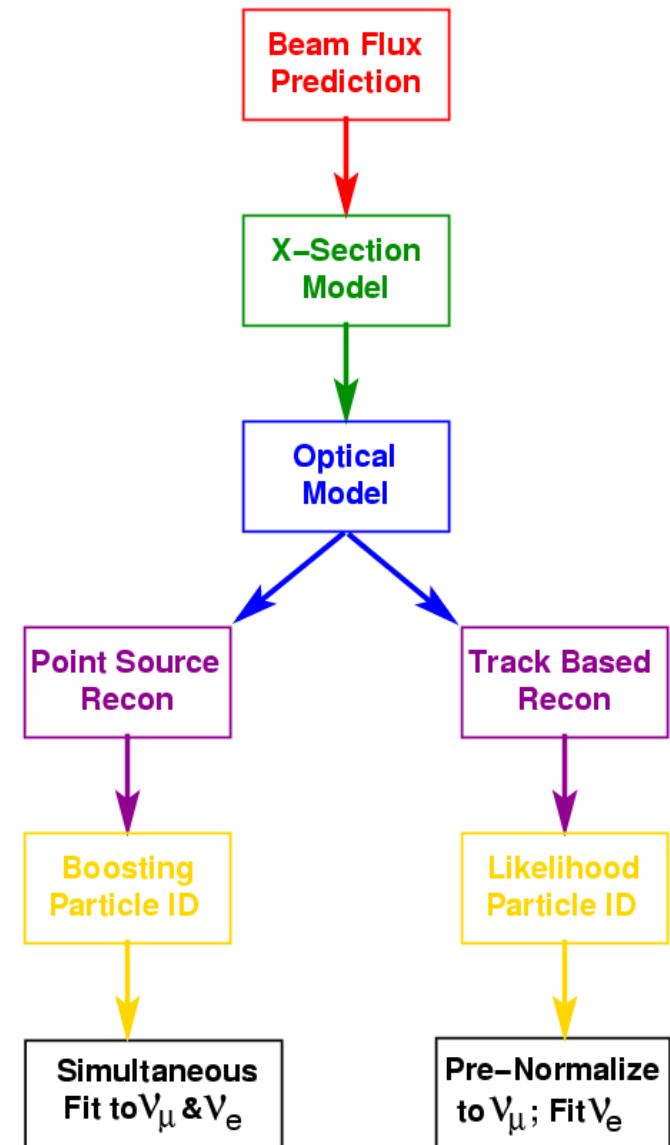
- The MiniBooNE signal is small but relatively easy to isolate
- As data comes in it is classified into 'boxes'
- For boxes to be opened to analysis they must be shown to have a signal $< 1\sigma$
- In the end, 99% of the data were available prior to unblinding...necessary to understand errors

Other

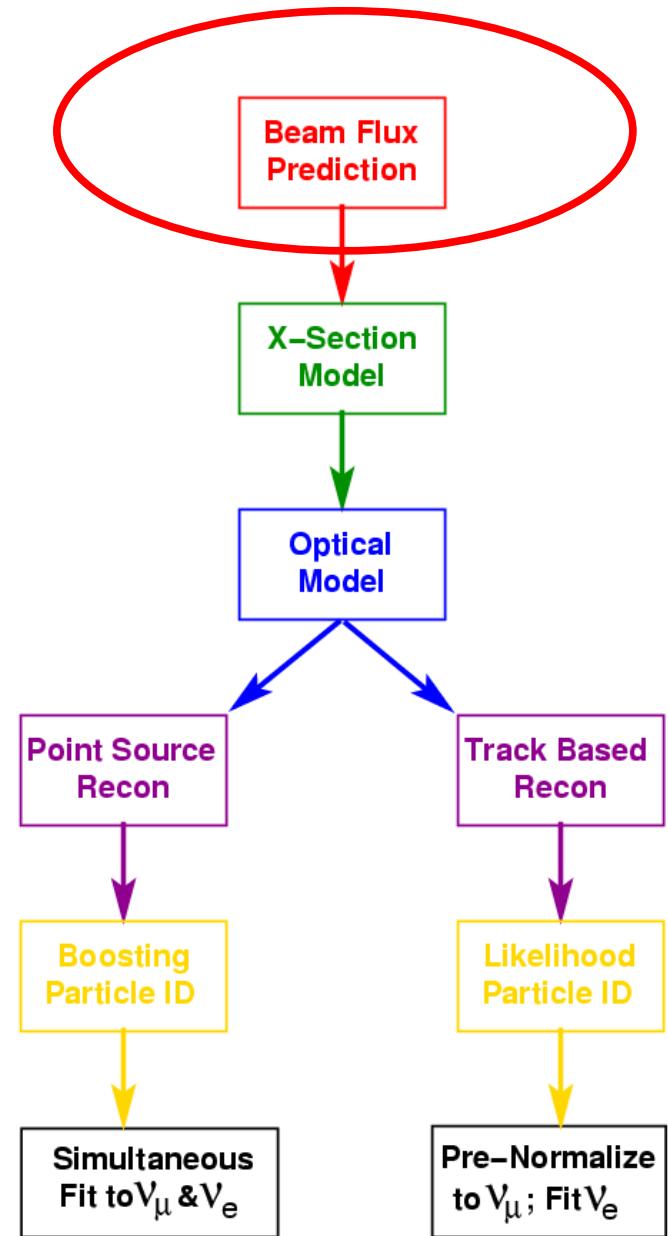
Signal
Box

MiniBooNE analysis structure

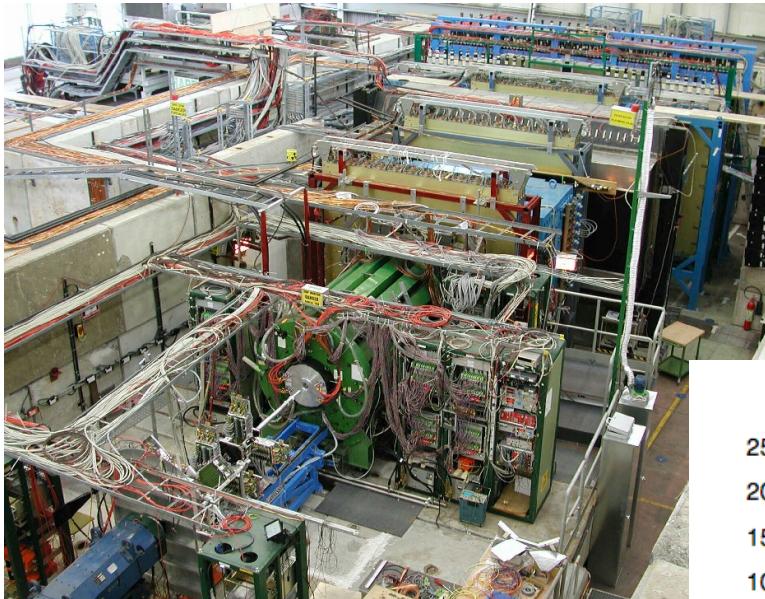
- ✓ Start with a Geant 4 flux prediction for the ν spectrum from π and K produced at the target
- ✓ Predict ν interactions using Nuance
- ✓ Pass final state particles to Geant 3 to model particle and light propagation in the tank
- ✓ Starting with event reconstruction, independent analyses form: Boosted Decision Tree (BDT) and Track Based Likelihood (TBL)
- ✓ Develop particle ID/cuts to separate signal from background
- ✓ Fit reconstructed E_ν spectrum for oscillations



Flux Prediction



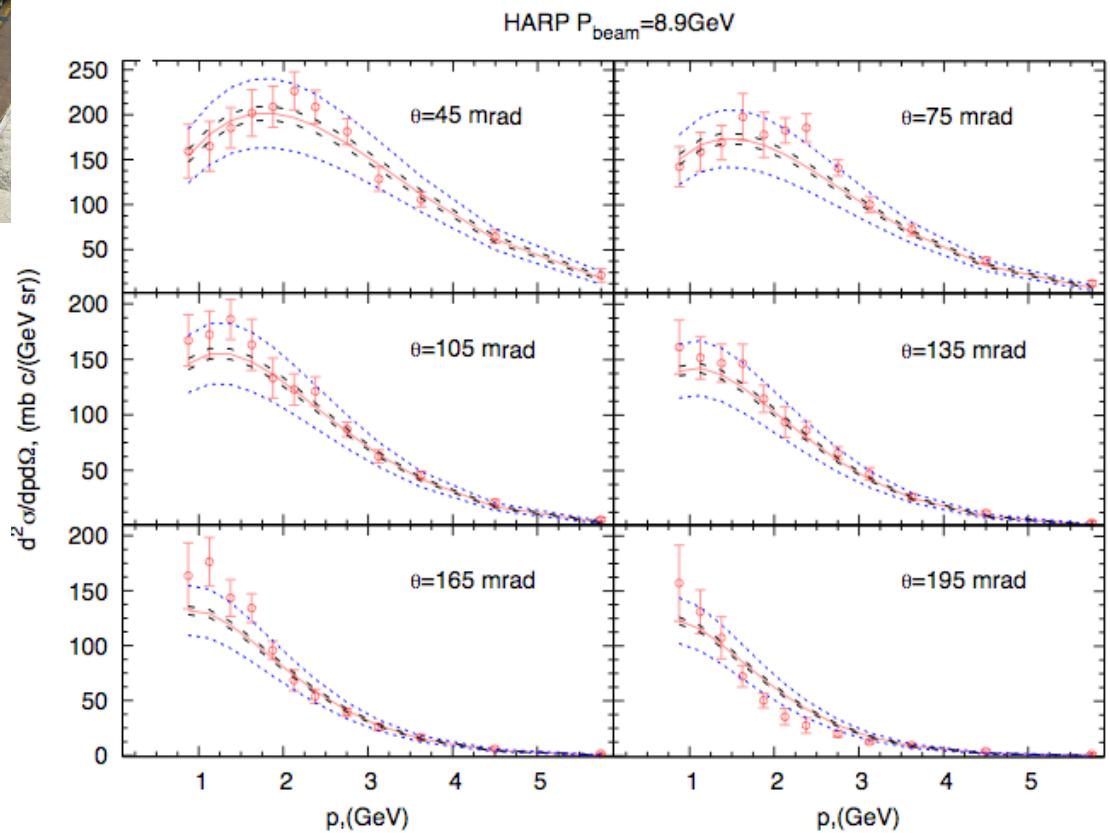
Modeling pion production



- HARP (CERN)
 - 5% λ Beryllium target
 - 8.9 GeV proton beam momentum

Data are fit to
a Sanford–Wang
parameterization.

HARP collaboration,
hep-ex/0702024

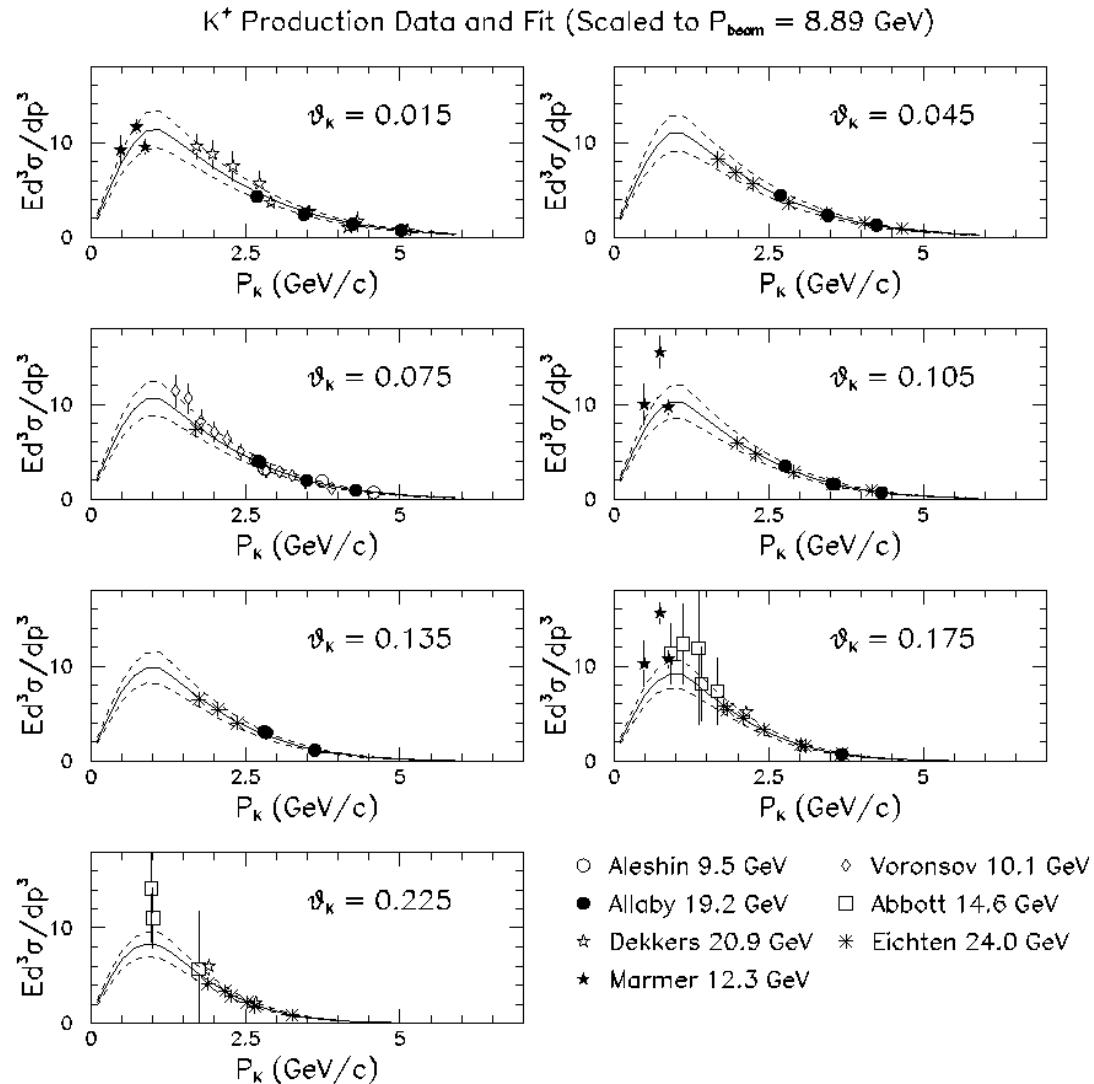


Modeling kaon production

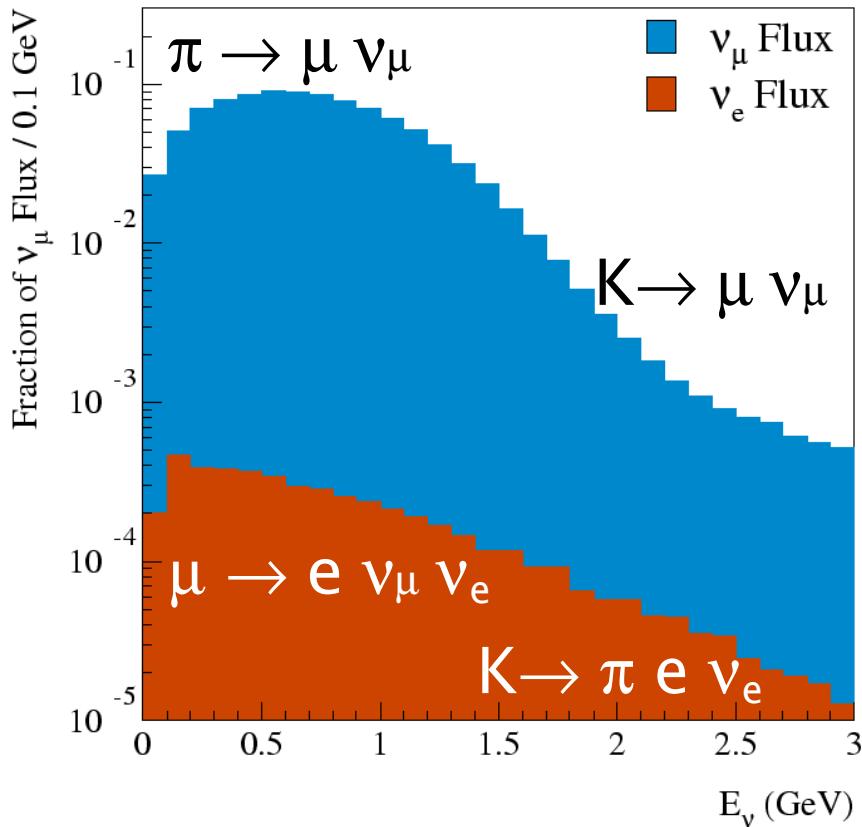
K⁺ Data from 10 – 24 GeV.
uses a Feynman scaling
parameterization.

data -- points
dash --total error
(fit \oplus parameterization)

K⁰ data are also
parameterized.



Final neutrino flux estimation



$$\nu_e / \nu_\mu = 0.5\%$$

“Intrinsic” $\nu_e + \bar{\nu}_e$ sources:

$\mu^+ \rightarrow e^+ \bar{\nu}_\mu \nu_e$ (52%)

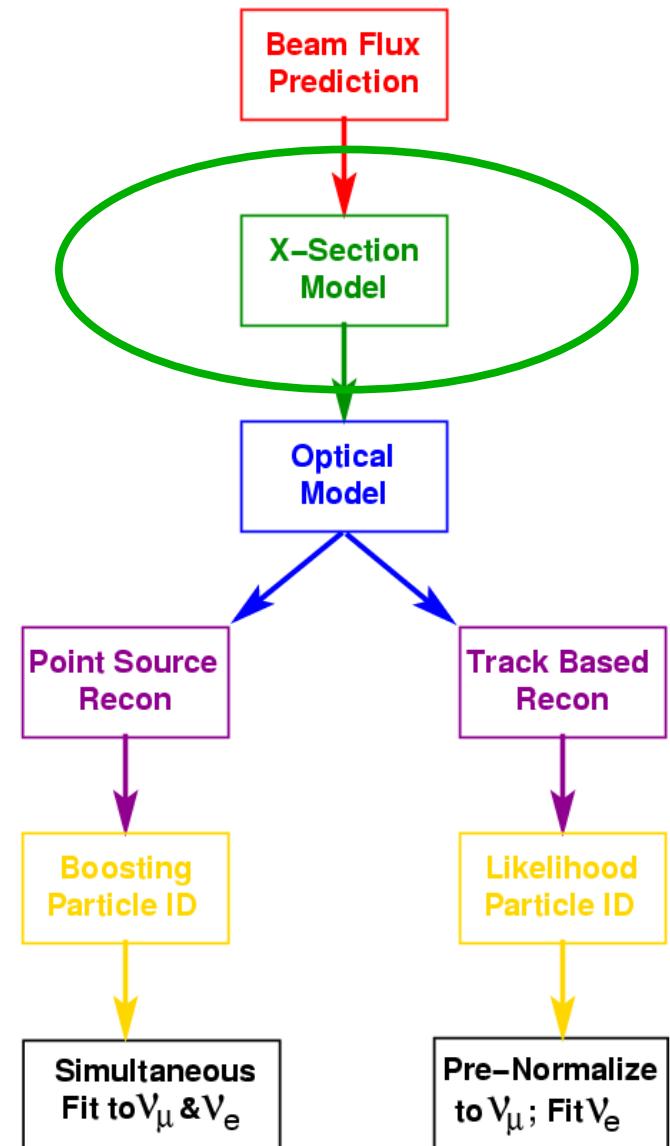
$K^+ \rightarrow \pi^0 e^+ \nu_e$ (29%)

$K^0 \rightarrow \pi^- e^+ \nu_e$ (14%)

Other (5%)

Antineutrino content: 6%

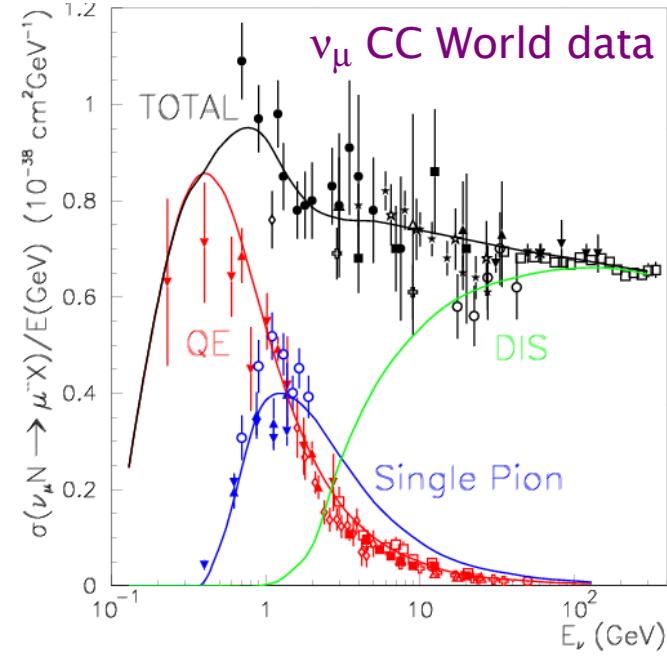
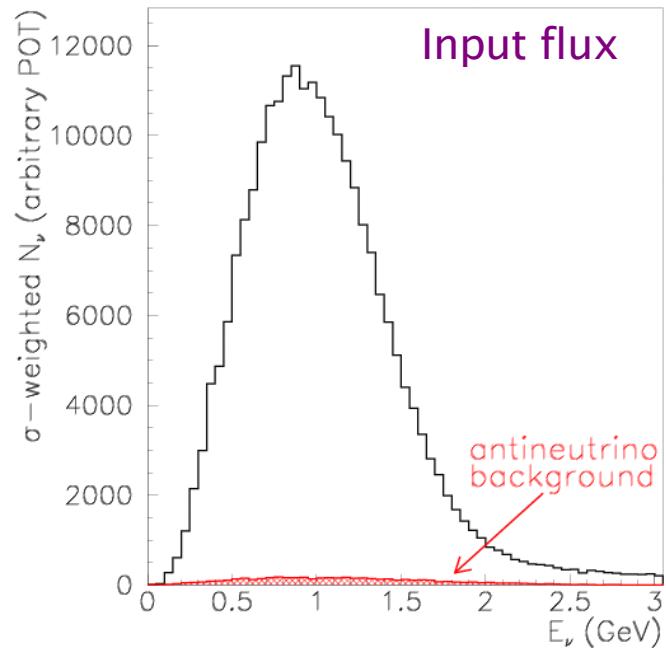
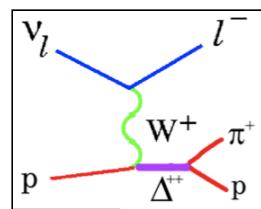
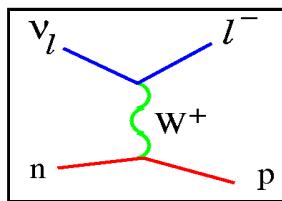
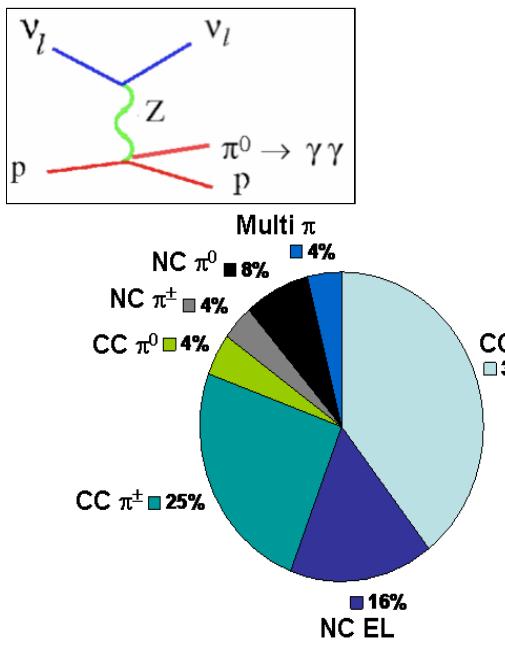
X-Section Model



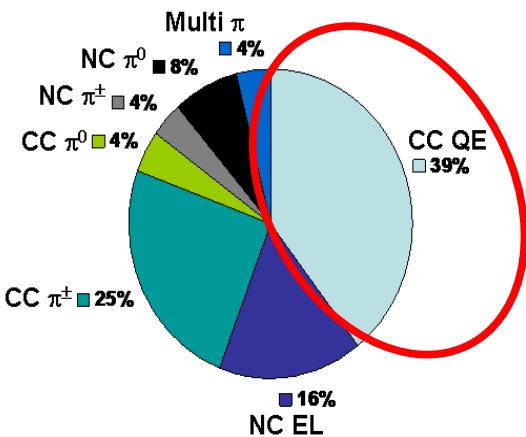
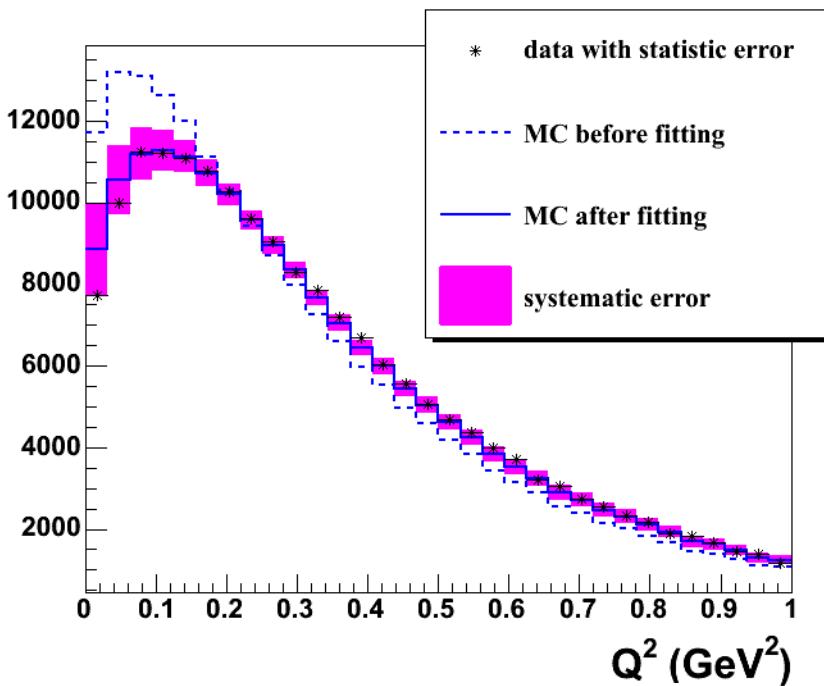
Nuance Monte Carlo

D. Casper, NPS, 112 (2002) 161

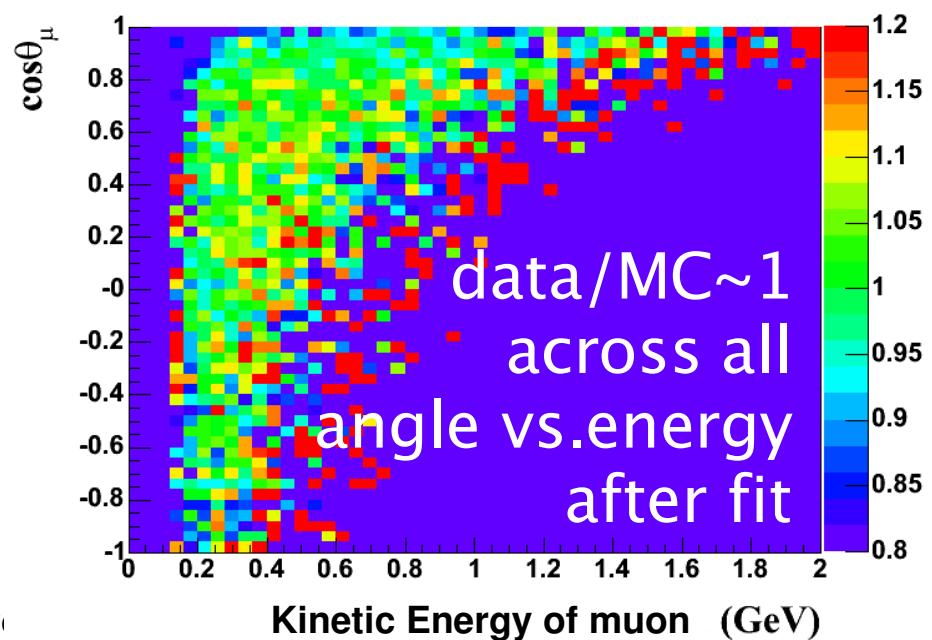
- Comprehensive generator, covers entire E_ν range
- Predicts relative rate of specific ν interactions from input flux
- Expected interaction rates in MiniBooNE (before cuts) shown below
- Based on world data, ν_μ CC shown below right
- Also tuned on internal data



Tuning Nuance on internal ν_μ CCQE data

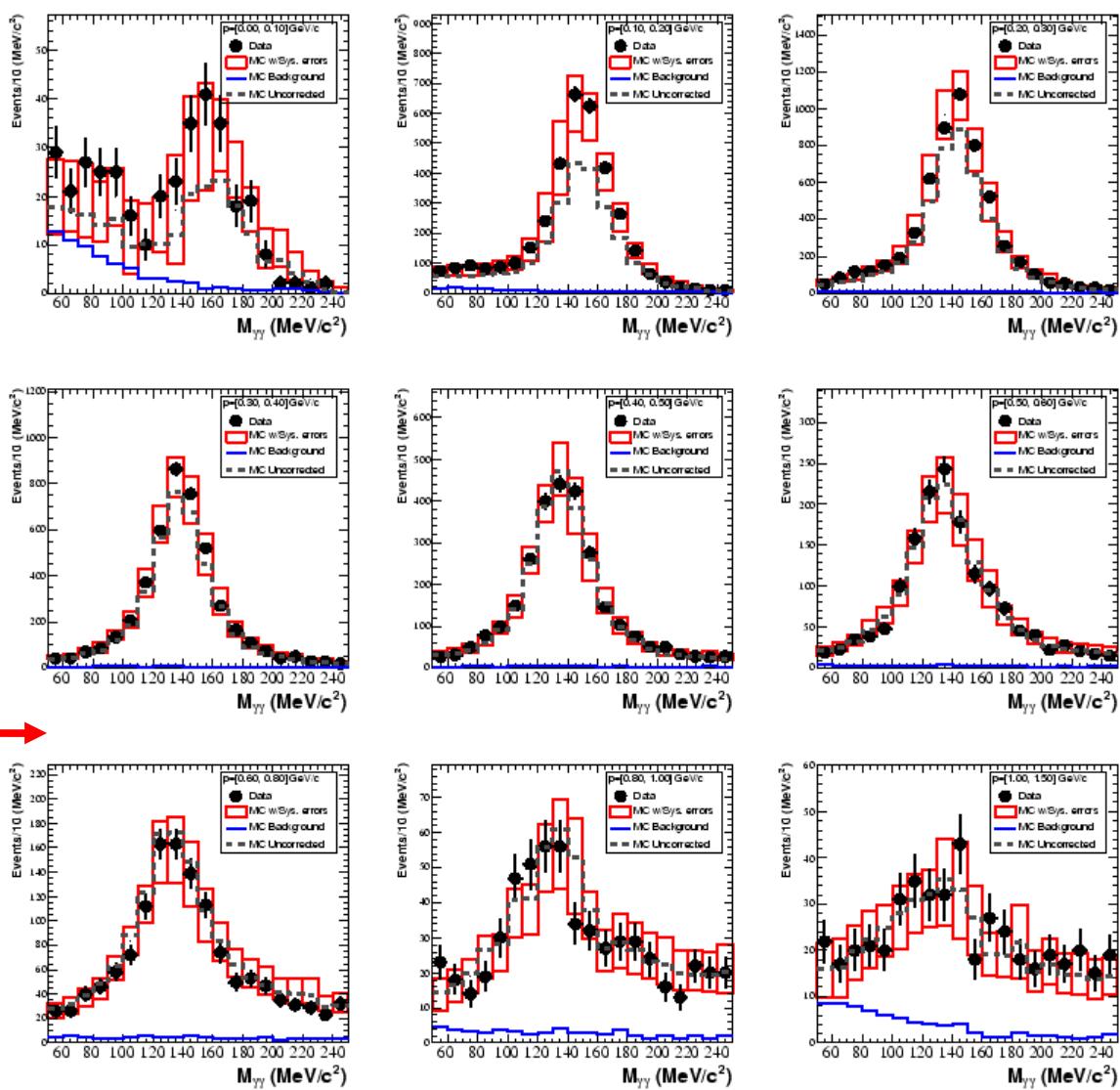
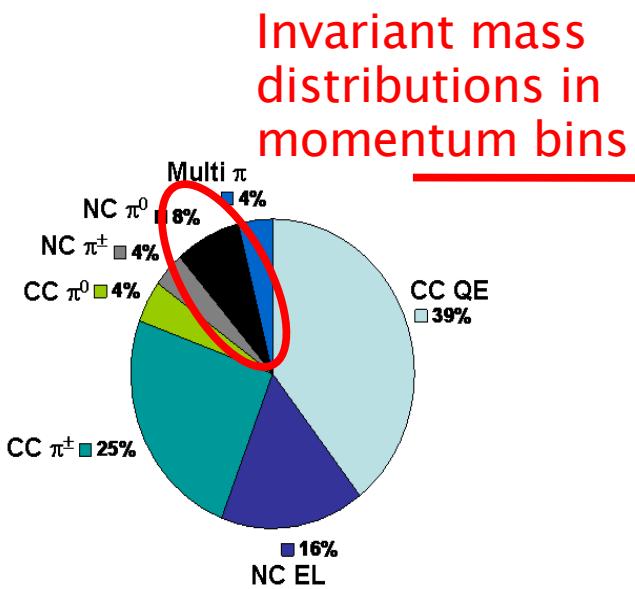


- From Q^2 fits to MB ν_μ CCQE data:
 - M_A^{eff} -- effective axial mass
 - $E_{\text{lo}}^{\text{SF}}$ -- Pauli Blocking parameter
- From electron scattering data:
 - E_b -- binding energy
 - p_f -- Fermi momentum
- Model describes CCQE ν_μ data well

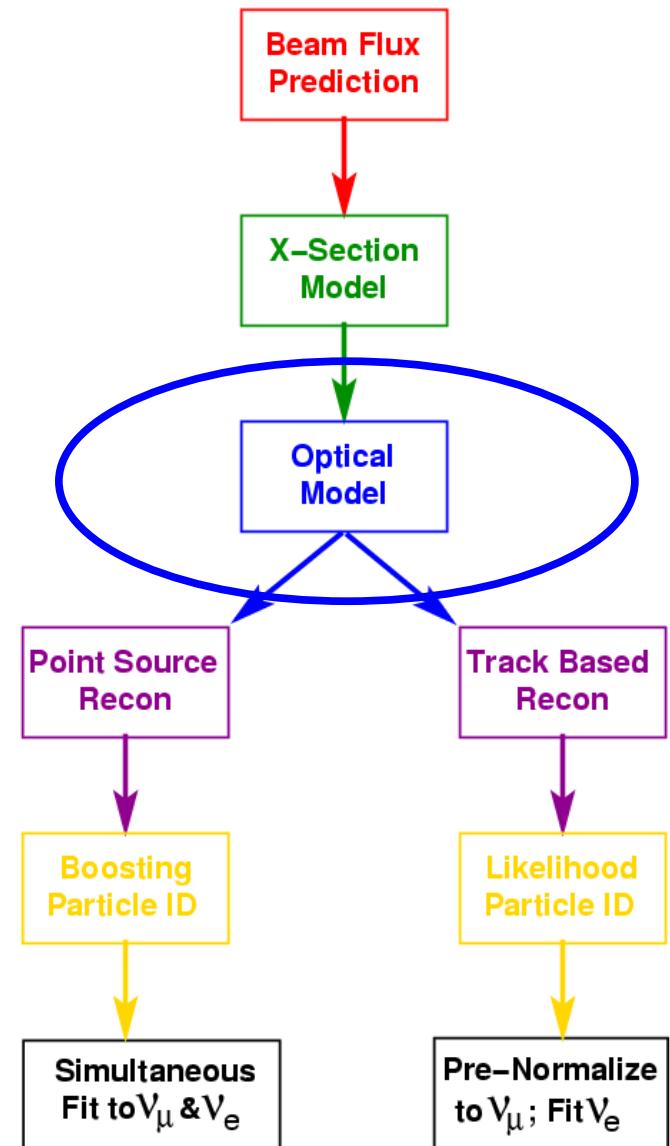


Tuning Nuance on internal NC π^0 data

- 90%+ pure π^0 sample (mainly $\Delta \rightarrow N\pi^0$)
- Measure rate as function of momentum
- Default MC underpredicts rate at low momentum
- analysis reaches 1.5 GeV
- $\Delta \rightarrow N\gamma$ also constrained (though to a lesser extent)

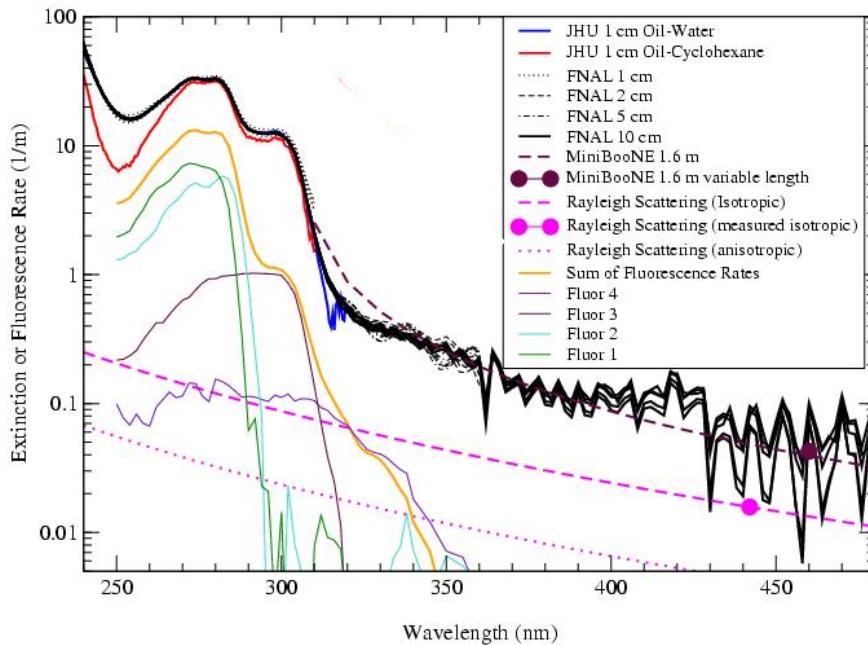


Optical Model

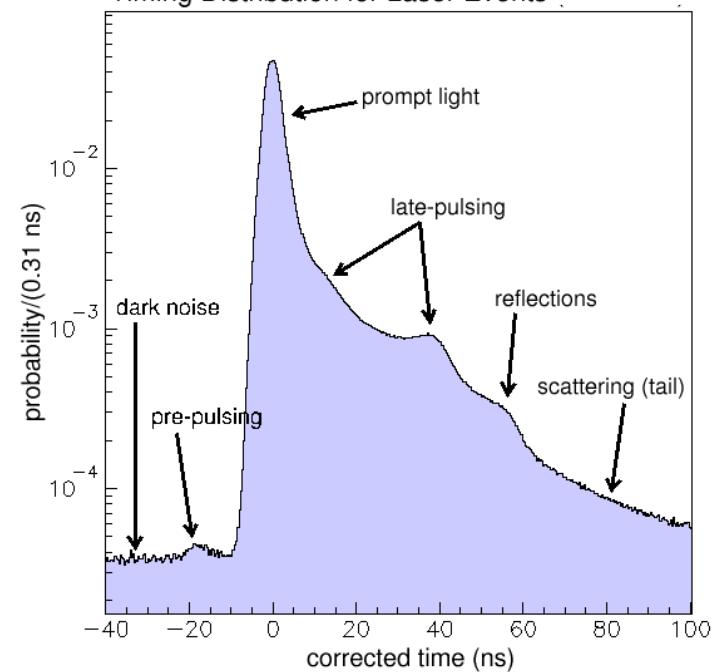


Light propagation in the detector

Extinction Rate for MiniBooNE Marcol 7 Mineral Oil

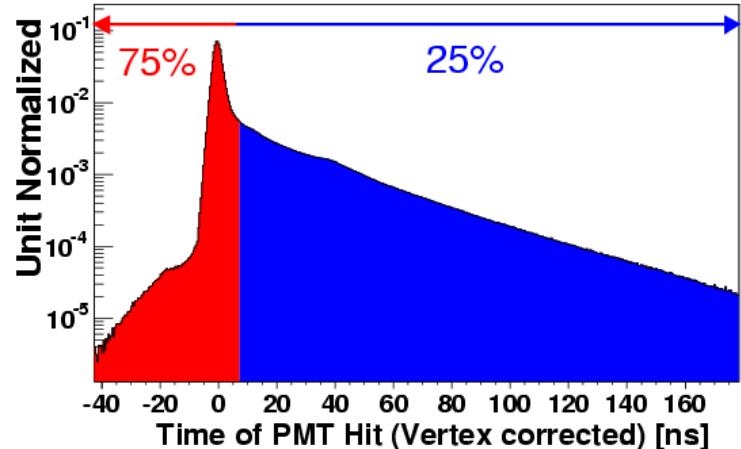


Timing Distribution for Laser Events



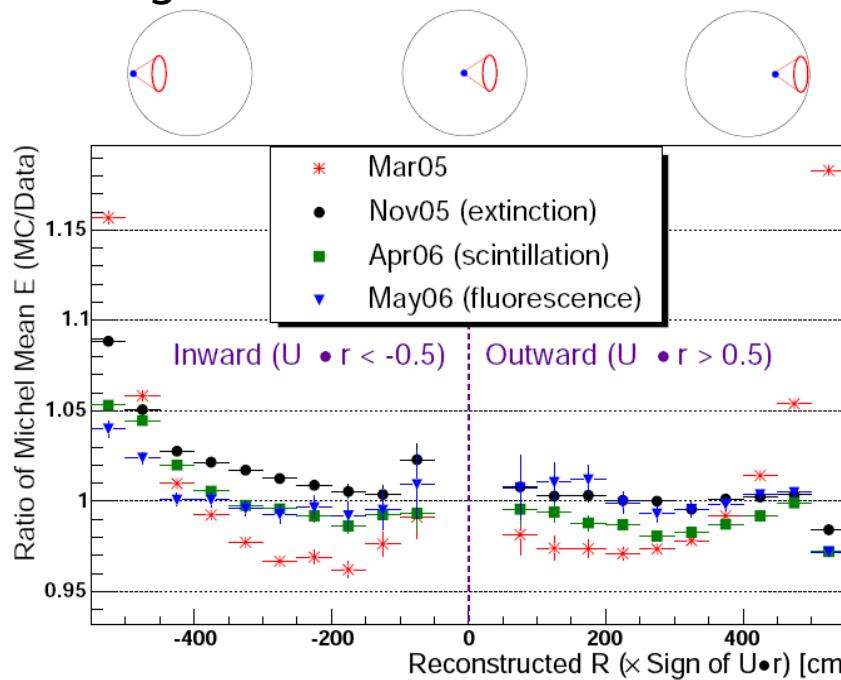
- ➊ Optical model is very complex
 - ➡ Cerenkov, scintillation, fluorescence
 - ➡ PMT Q/t response
 - ➡ Scattering, reflection, prepulses
- ➋ Overall, about 40 non-trivial parameters

Michel electron t distribution

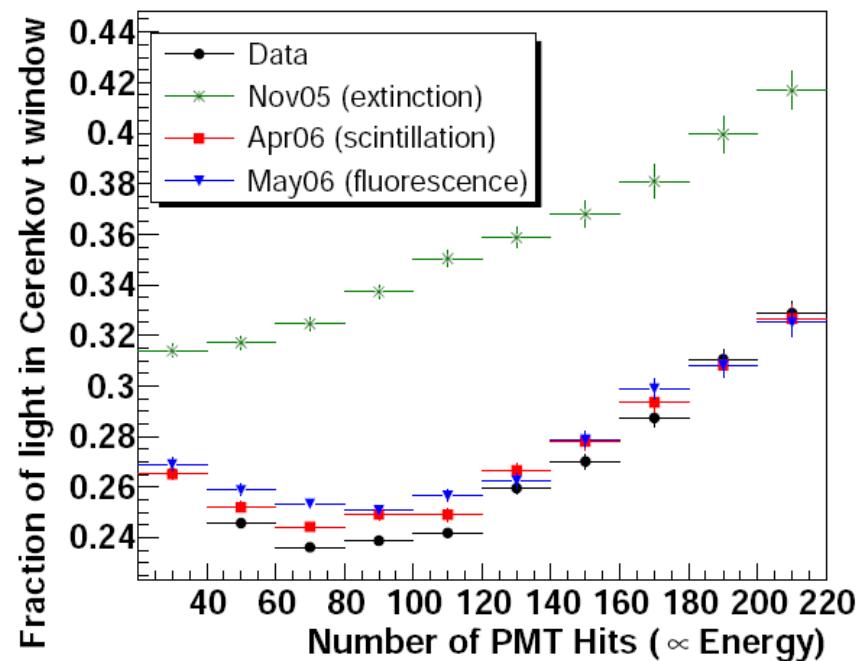


Tuning the optical model

Using Michel electrons...



Using NC elastic ν interactions...



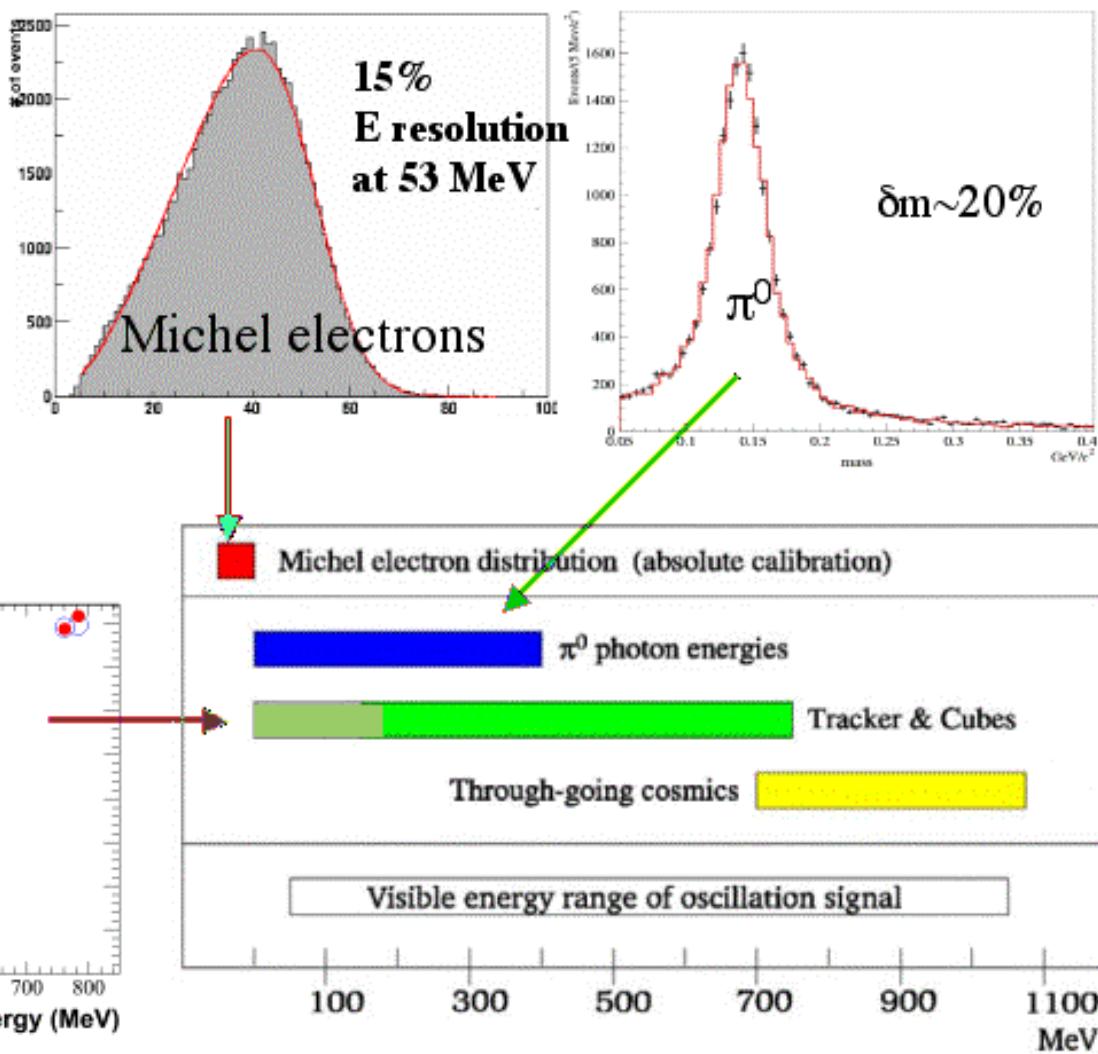
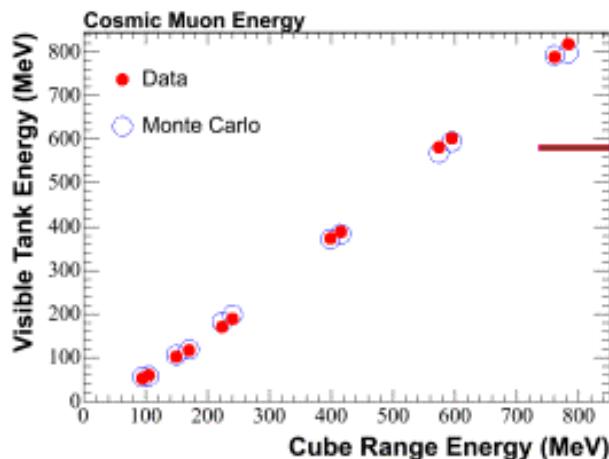
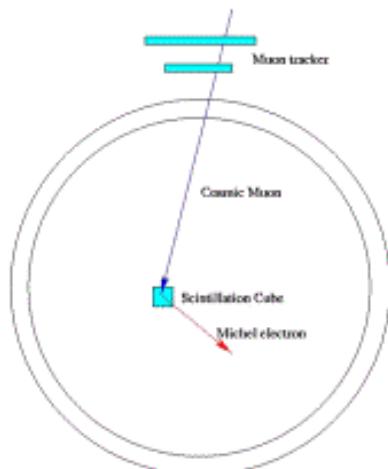
- ➊ Initial optical model defined through many benchtop measurements
- ➋ Subsequently tuned with *in situ* sources, examples
 - Left: Michel e populate entire tank, useful for tuning extinction
 - Right: NC elastic n interactions below Cerenkov threshold useful for distinguishing scintillation from fluorescence



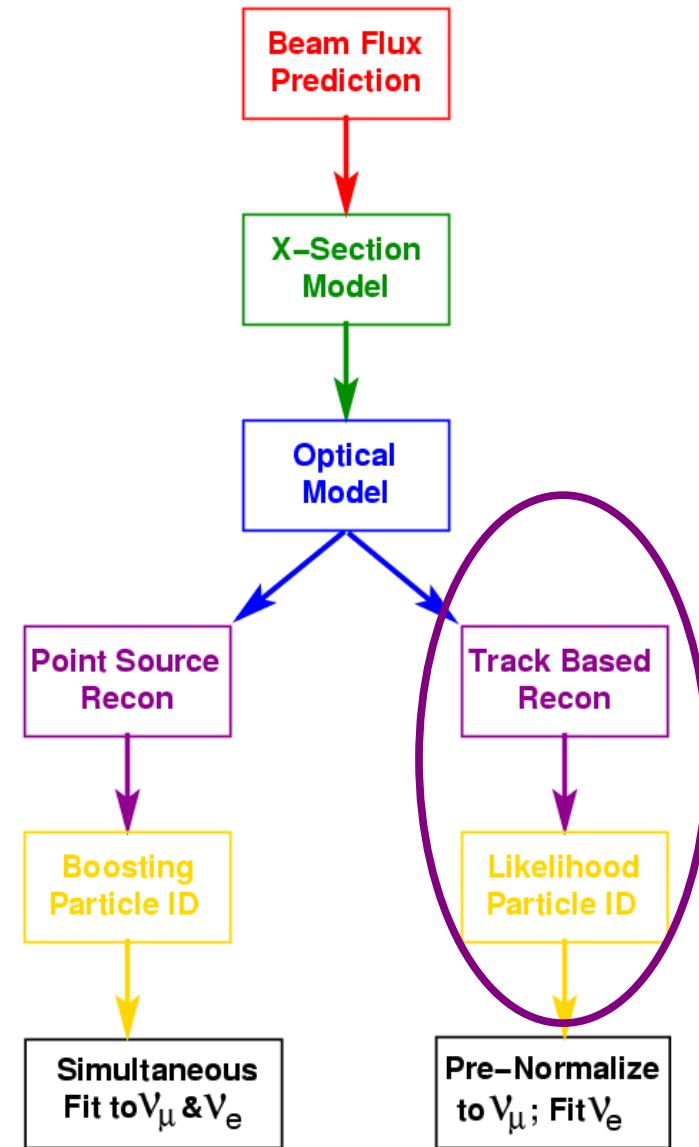
Calibration sources span various energies

Calibration Sources

Tracker system



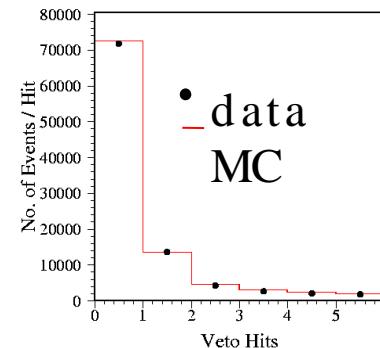
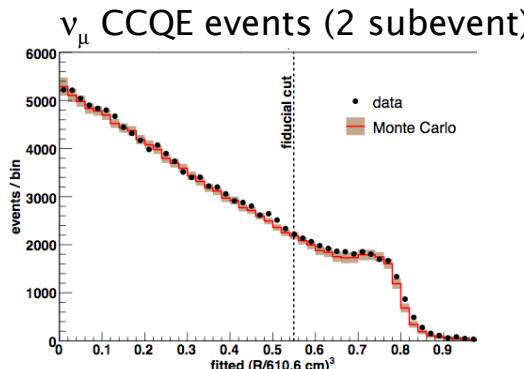
Track-Based Likelihood (TBL) Reconstruction and Particle ID



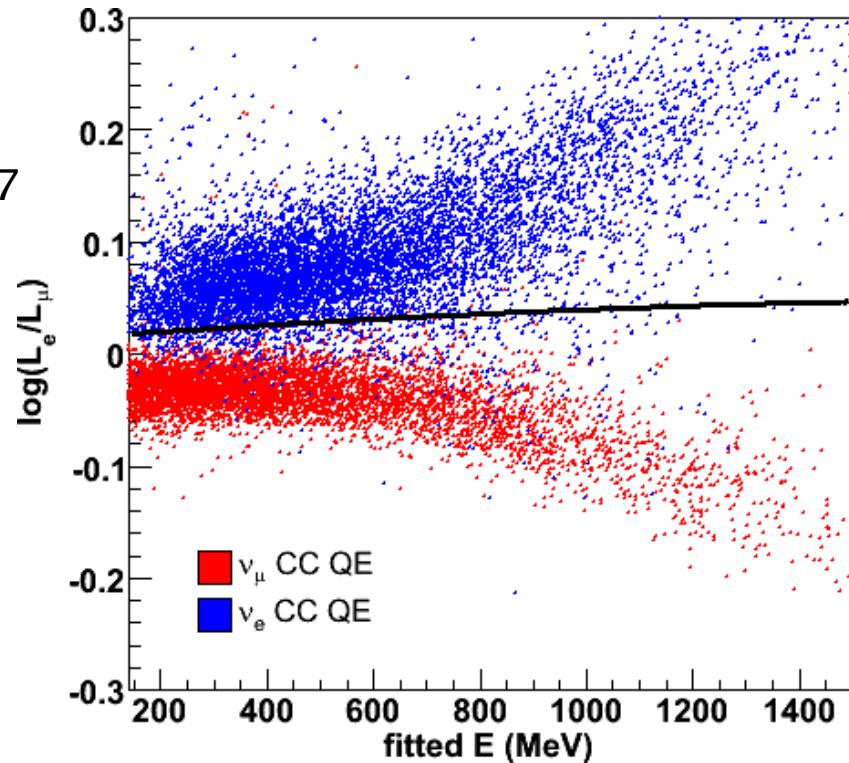
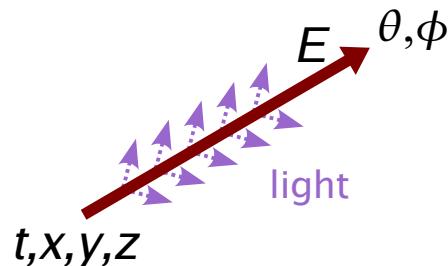
TBL Analysis: Separating e from μ

- Analysis pre-cuts

- Only 1 subevent
- Veto hits < 6
- Tank hits > 200
- Radius < 500 cm

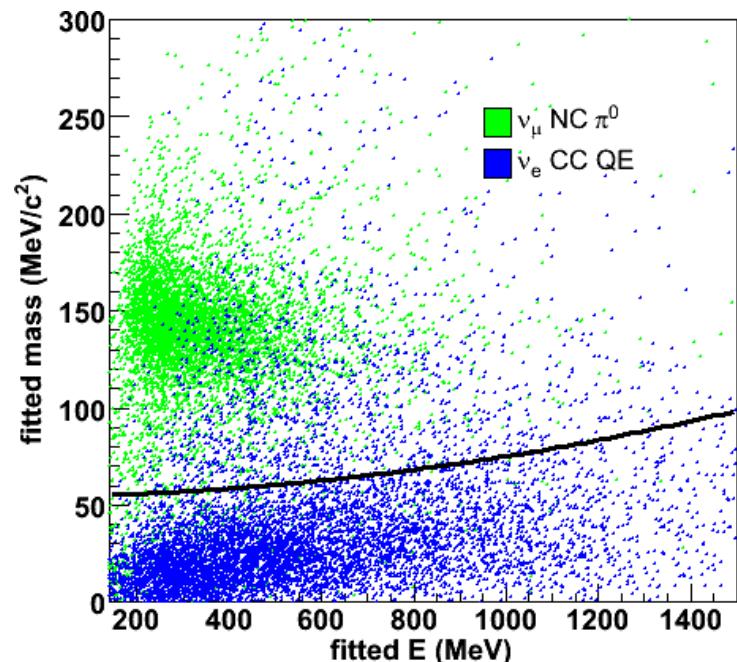
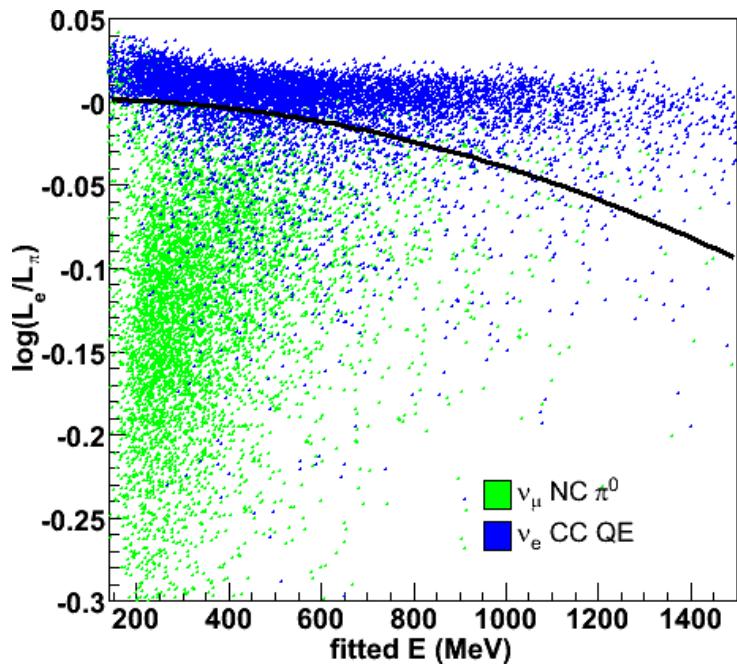
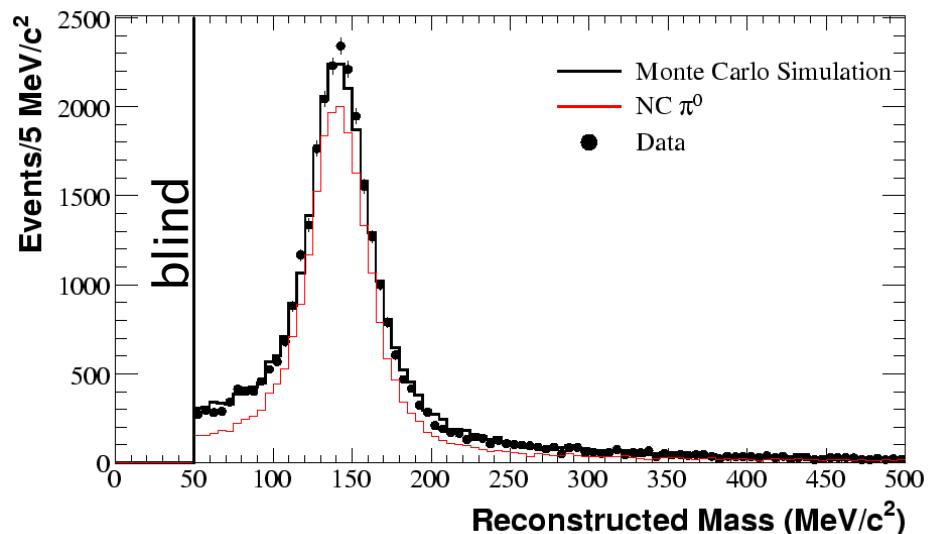
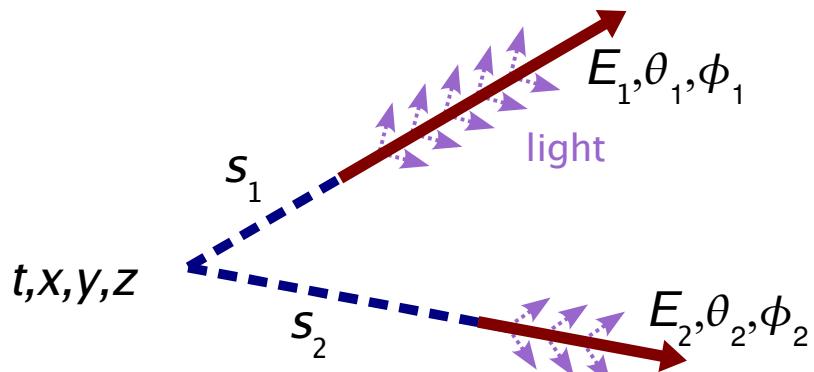


- Event is a collection of PMT-level info (q, t, x)
- Form sophisticated Q and T pdfs, and fit for 7 track parameters under 2 hypotheses
 - The track is due to an electron
 - The track is coming from a muon

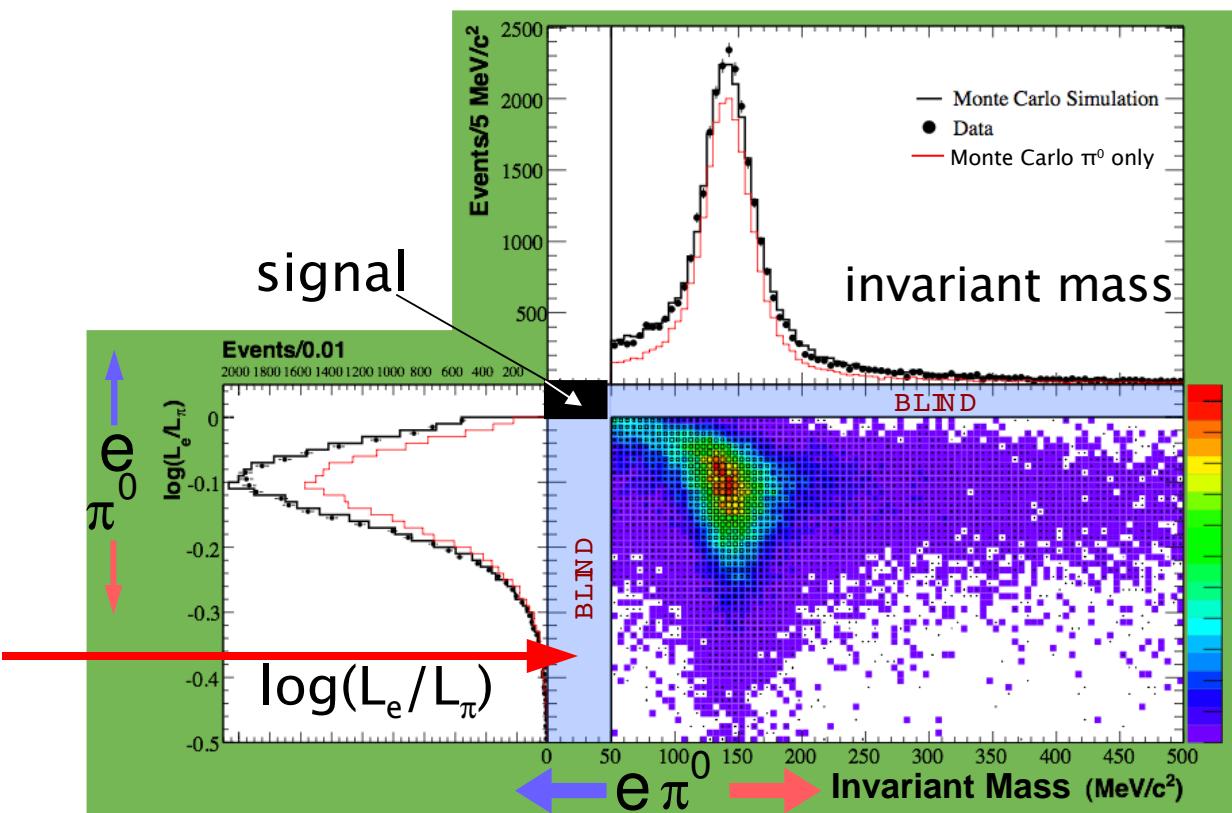


Separating e from π^0

- Extend fit to include two e-like tracks
- Very tenacious fit...8 minutes per event
- Nearly 500k CPU hours used

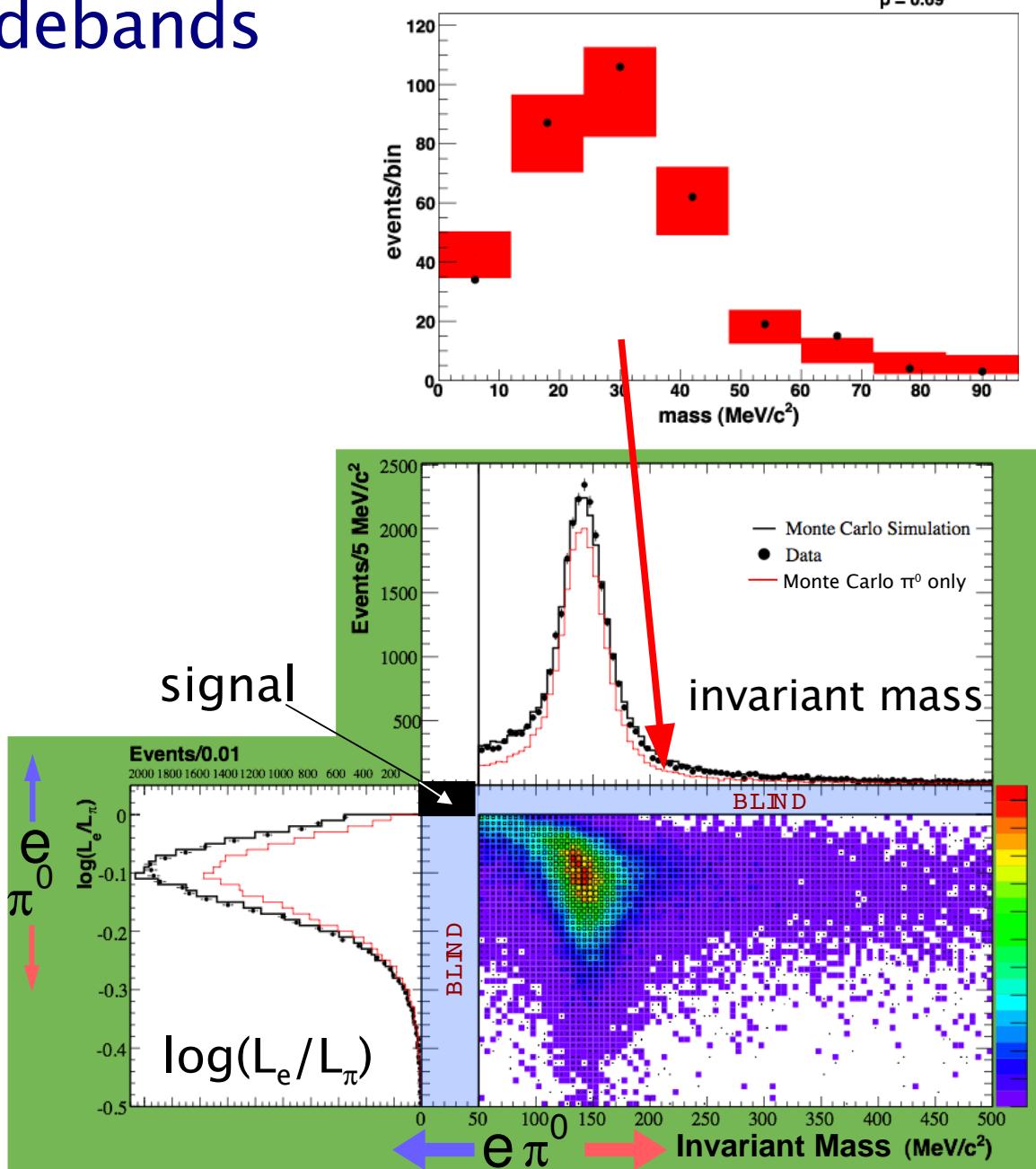


Checking signal sidebands



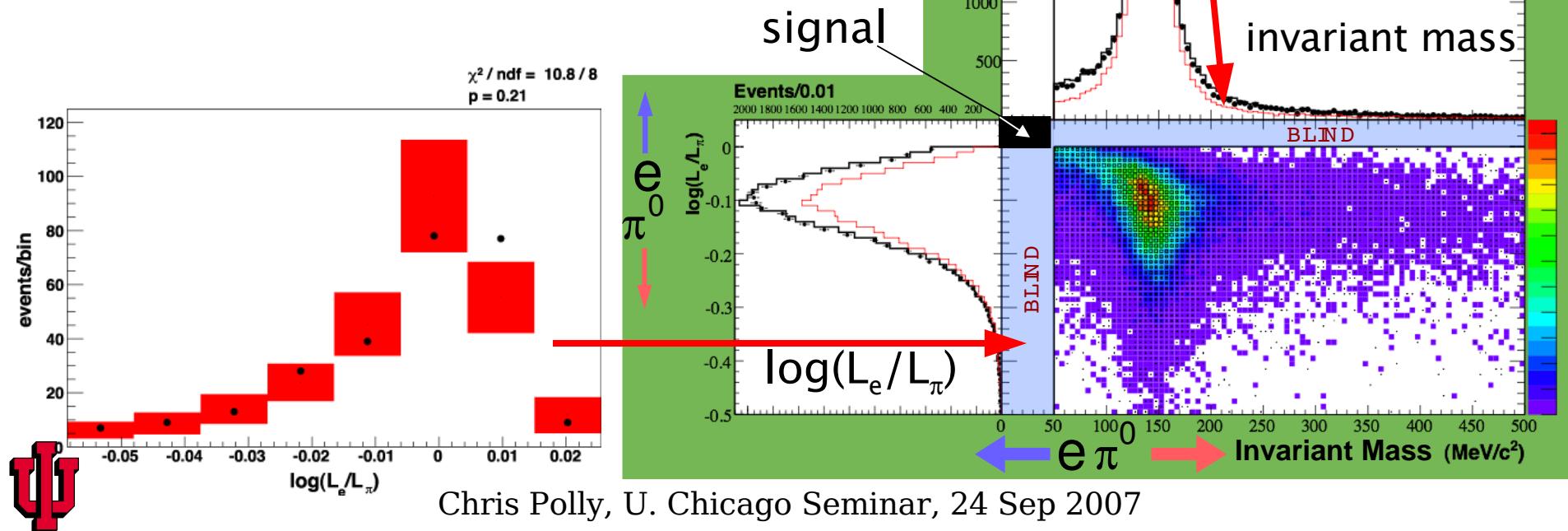
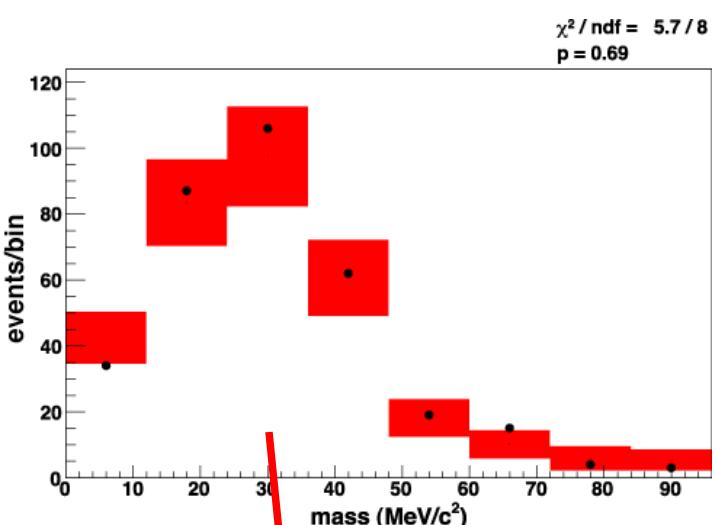
Checking signal sidebands

- Region at low $\log(L_e/L_\pi)$



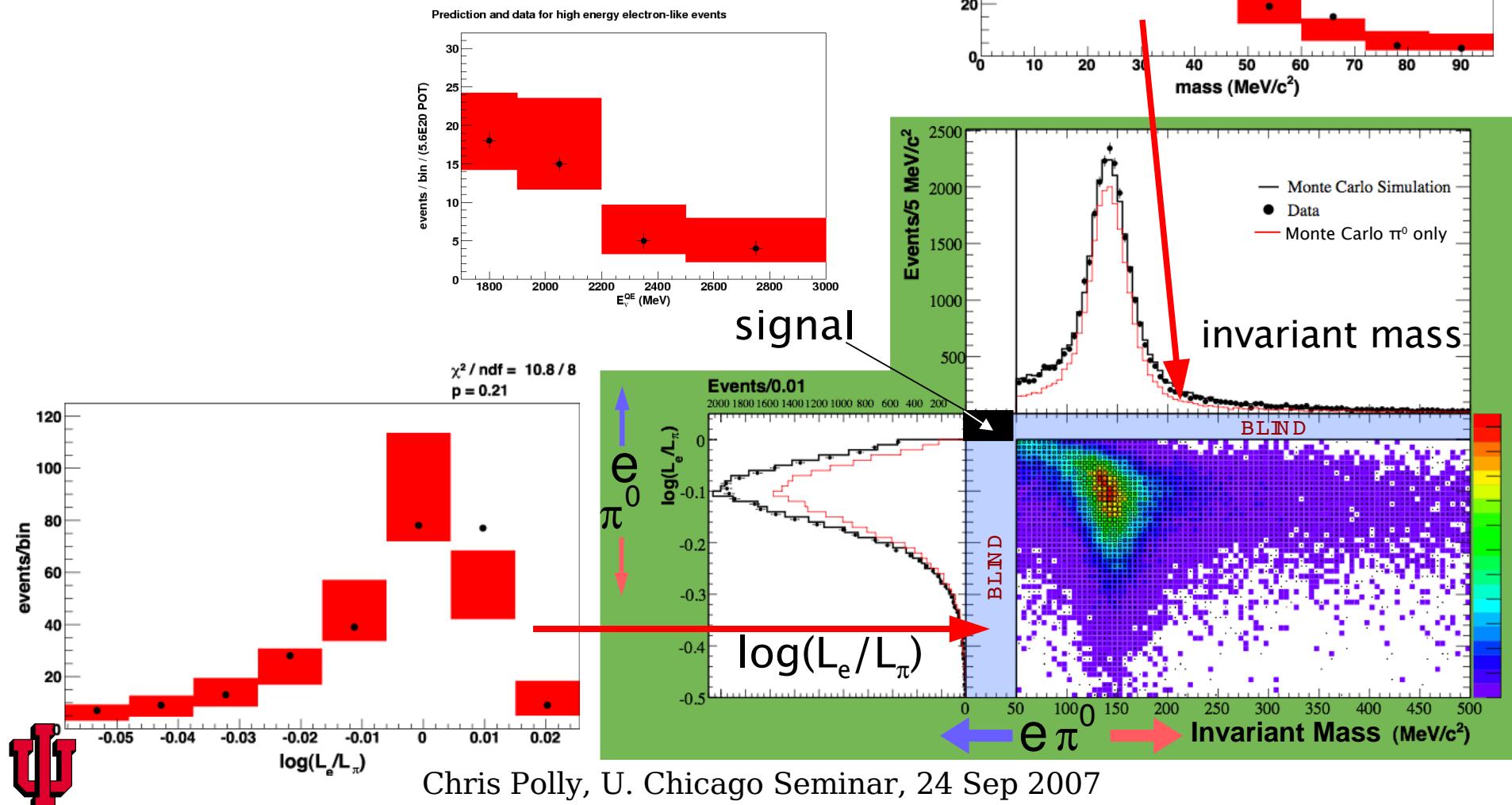
Checking signal sidebands

- Region at low $\log(L_e/L_\pi)$
- Region at low invariant mass

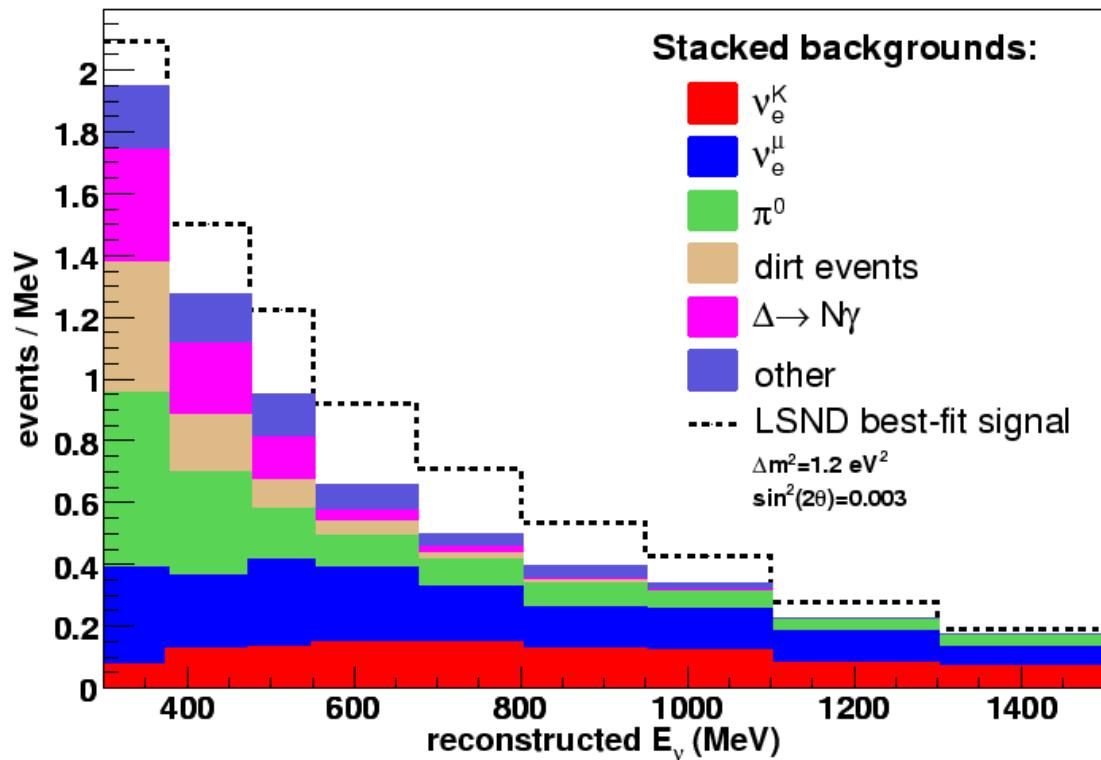


Checking signal sidebands

- Region at low $\log(L_e/L_\pi)$
- Region at low invariant mass
- Region in signal, but at high E_ν



TBL Analysis: Expected event totals

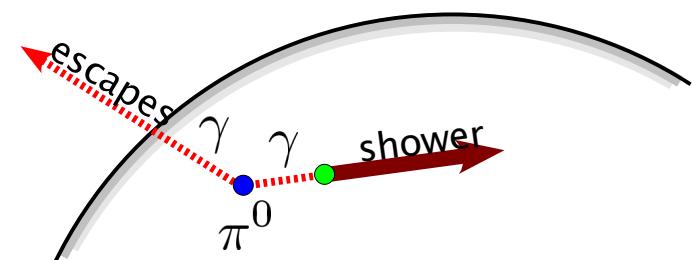
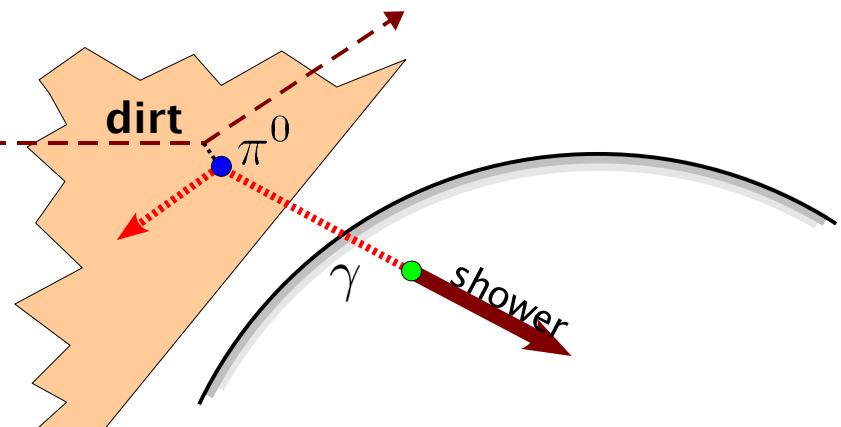


475 MeV - 1250 MeV

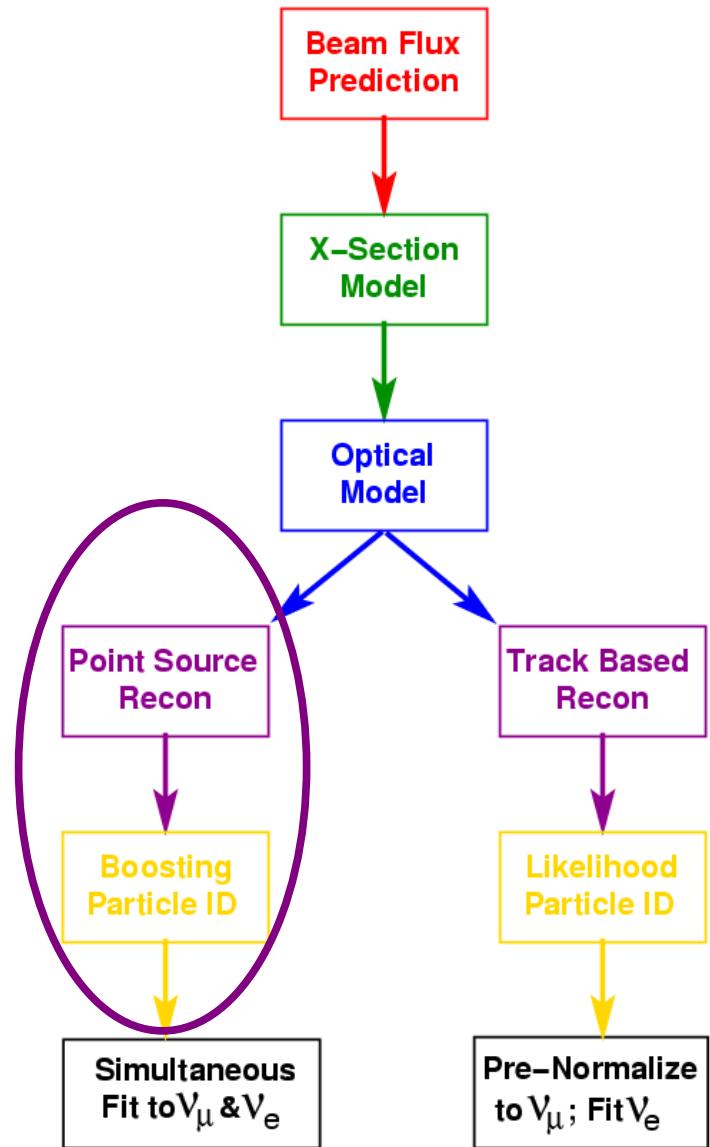
ν_e^K	94
ν_e^μ	132
π^0	62
dirt	17
$\Delta \rightarrow N\gamma$	20
other	33
total	358

LSND best-fit $\nu_\mu \rightarrow \nu_e$ 126

$$S/\sqrt{B} = 6.8$$



Boosted Decision Tree (BDT) Reconstruction and Particle ID

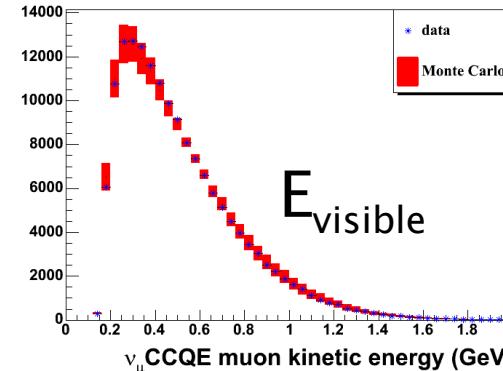


BDT Reconstruction

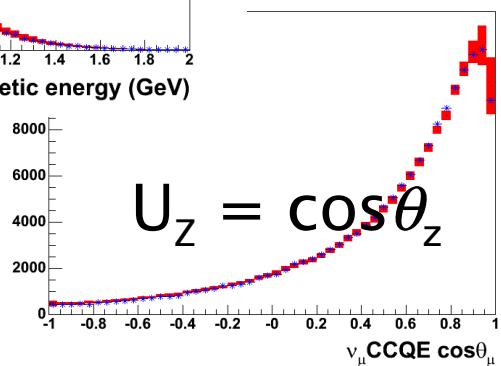
- Same pre-cuts as TBL (taking R from different reconstruction)
- Different reconstruction:
 - Treats particles more like point sources, *i.e.* not as careful about dE/dx
 - Not as tenacious about getting out of local minima, particularly with pion fit
 - Reconstruction runs nearly 10 times faster
- To make up for the simple fit, the BDT analysis relies on a form of machine learning, the boosted decision tree. Byron P. Roe, *et al.*, NIM A543 (2005) 577.
- Boosting Input Variables:
 - Low-level (# tank hits, early light fraction, etc.)
 - High-level (Q^2 , U_z , fit likelihoods, etc.)
 - Topology (charge in anuli, isotropic light, etc.)
- A total of 172 variables were used
- All 172 were checked for agreement within errors in 5 important 'boxes' (ν_μ CCQE, NC π^0 , NC-elastic, Michel decay e, 10% closed)
- Boosting Output: Single 'score', + is signal-like

BDT Resolution:
vertex: 24 cm
direction: 3.8°
energy 14%

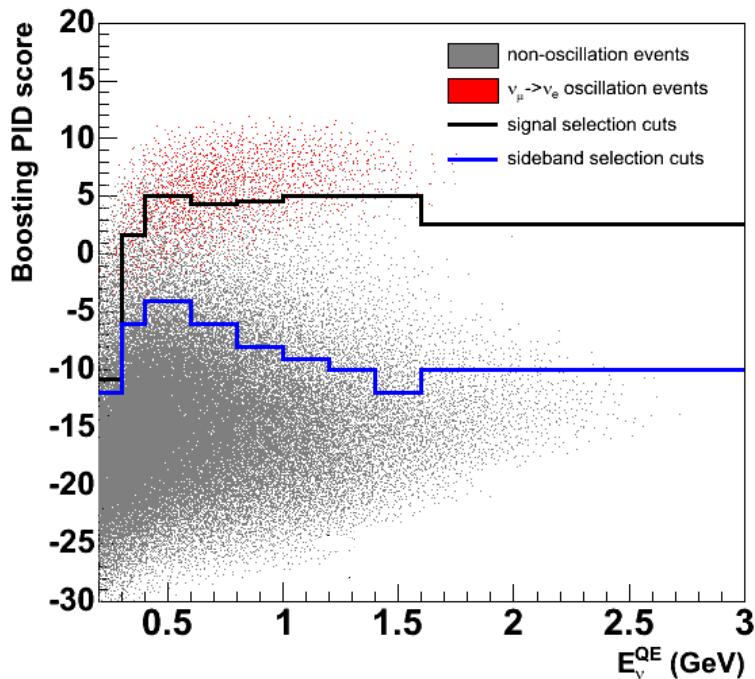
TBL Resolution:
vertex: 22 cm
direction: 2.8°
energy 11%



ν_μ CCQE
Examples

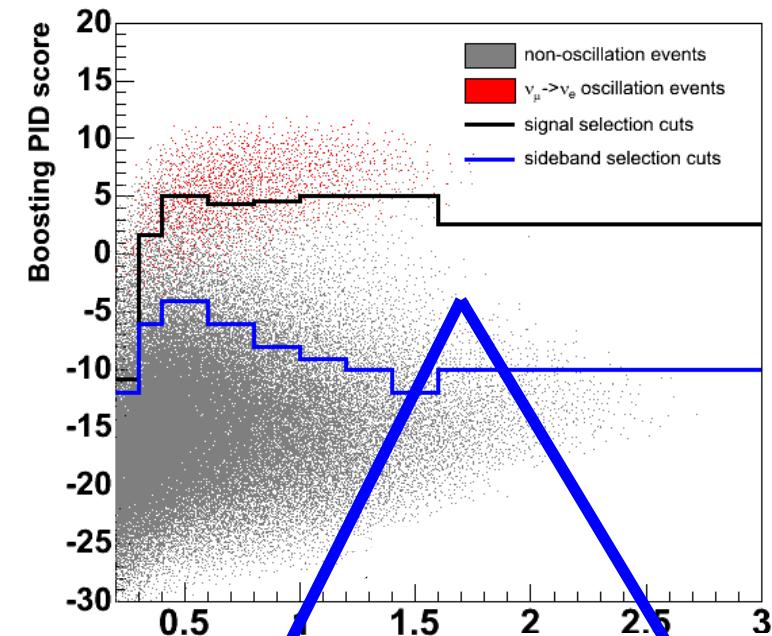


BDT Analysis: Signal/background regions

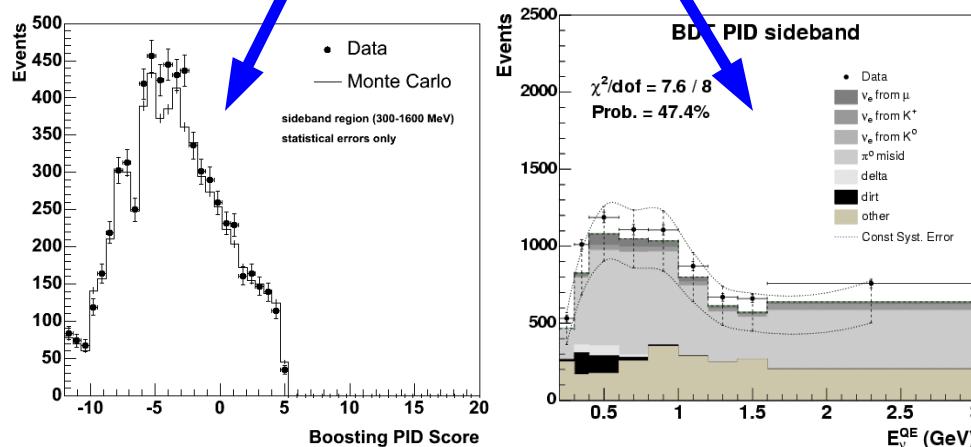


Signal prediction (red) versus all bkg (gray)

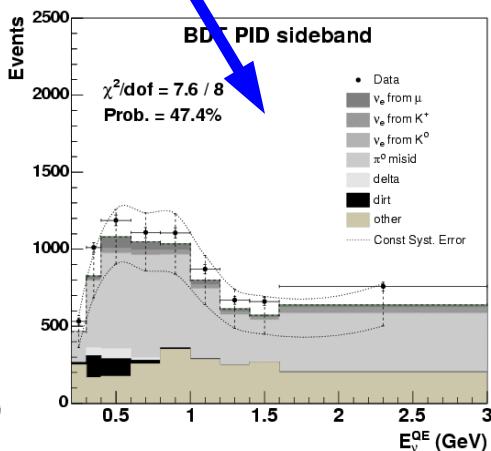
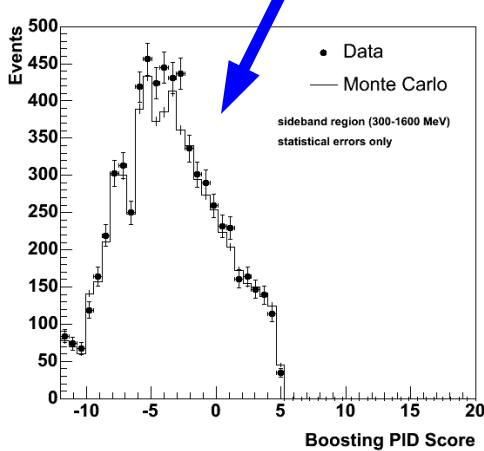
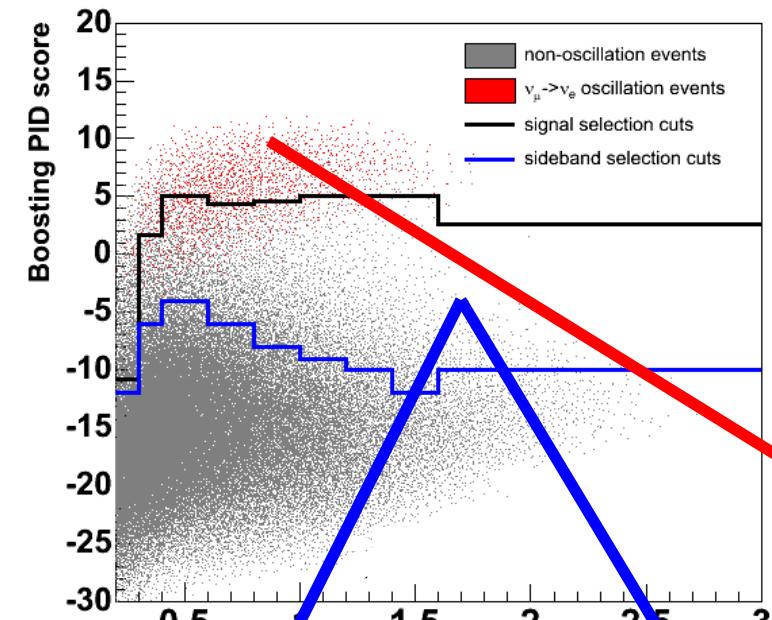
BDT Analysis: Signal/background regions



- Signal prediction (red) versus all bkg (gray)
- Start by looking at data in 'sideband'...region immediately adjacent to signal region

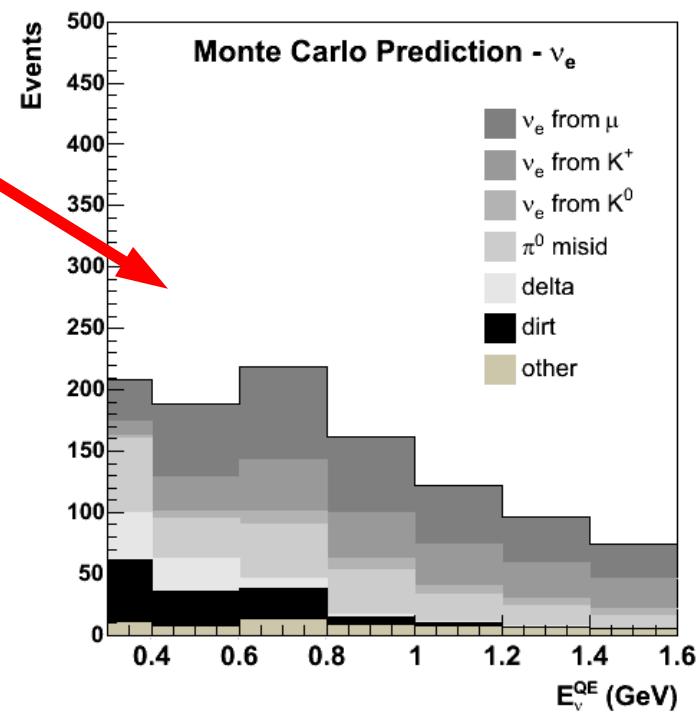


BDT Analysis: Signal/background regions



- Signal prediction (red) versus all bkg (gray)
- Start by looking at data in 'sideband'...region immediately adjacent to signal region
- Satisfied with agreement? Finalize background prediction
- In 500–1200 MeV range: 603 bkg, LSND best-fit $\nu_{\mu} \rightarrow \nu_e$ 203

$$S/\sqrt{B} = 8.3$$

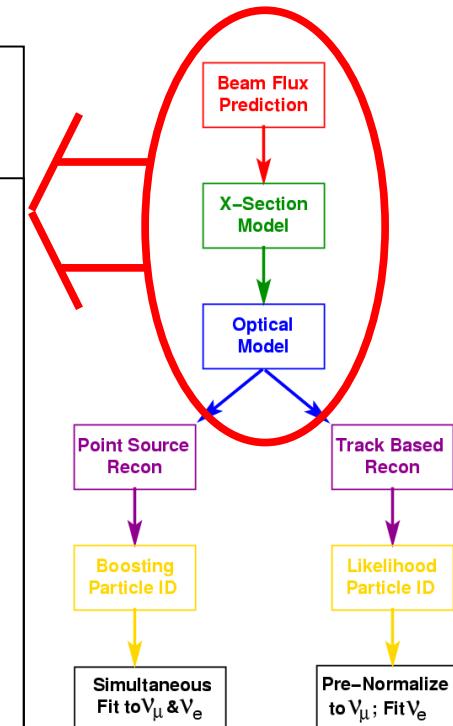


Systematic Error Analysis and Results



Final error budget (diagonals only...greatly simplified)

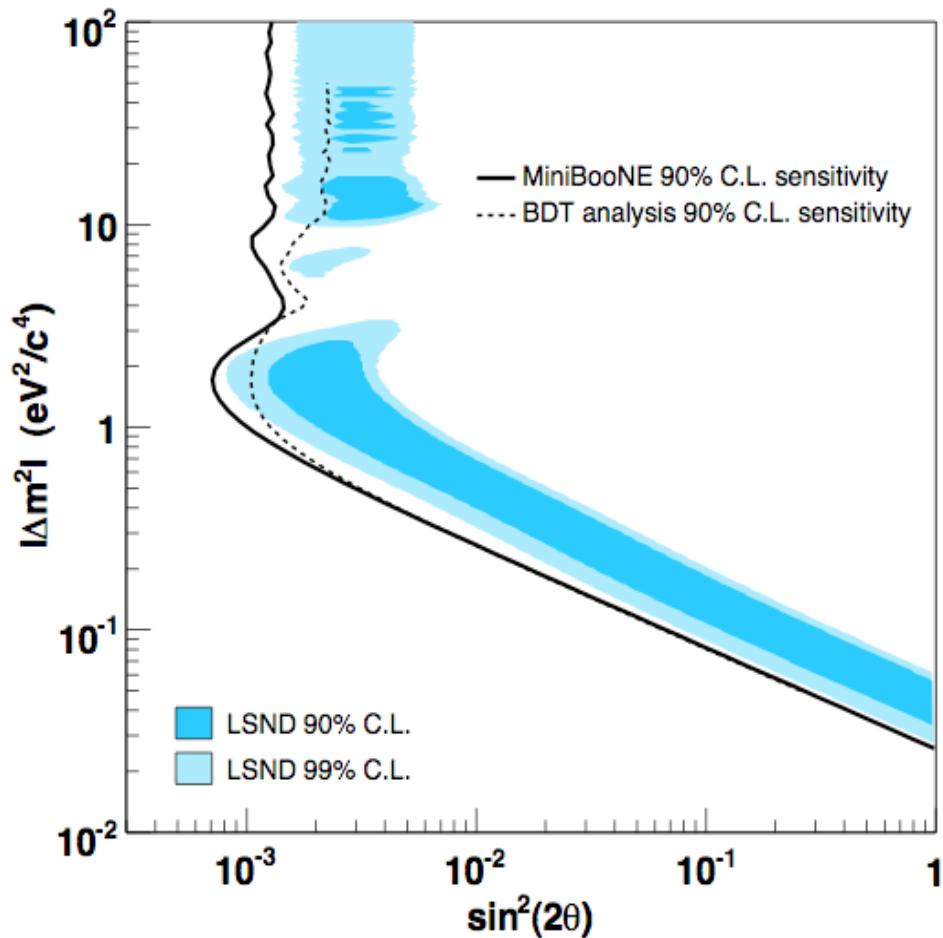
Source of uncertainty on ν_e background	TBL/BDT error in %	Constrained by MB data	Reduced by tying ν_e to ν_μ
Flux from π^+/μ^+ decay	6.2 / 4.3	✓	✓
Flux from K^+ decay	3.3 / 1.0	✓	✓
Flux from K^0 decay	1.5 / 0.4	✓	✓
Target/beam models	2.8 / 1.3	✓	
ν -cross section	12.3 / 10.5	✓	✓
NC π^0 yield	1.8 / 1.5	✓	
Dirt interactions	0.8 / 3.4	✓	
Optical model	6.1 / 10.5	✓	✓
DAQ electronics model	7.5 / 10.8	✓	



- Every checkmark in this table could easily consume a 30 minute talk
 - All error sources had some *in situ* constraint
 - Some reduced by combined fit to ν_μ and ν_e
- Errors arise from common uncertainties in flux, xsec, and optical model
- Reconstruction and PID unique
 - BDT had higher signal-to-background
 - TBL more impervious to systematics
 - About 50% event overlap



BDT/TBL sensitivity comparison



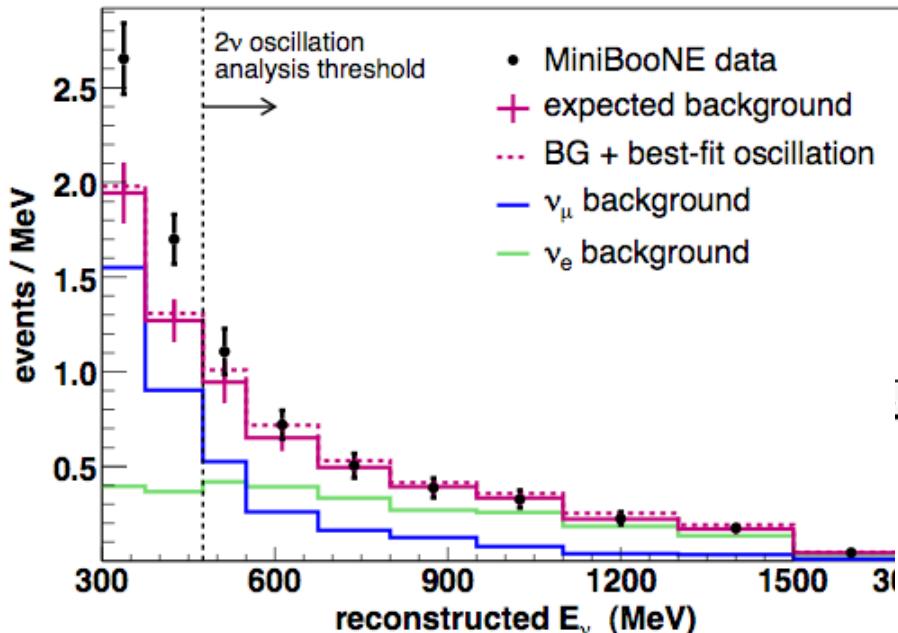
- Sensitivity is determined from simulation only (no data yet!)
- Decided before unblinding:
 - Final PID cuts
 - Region of E_ν to fit
 - Analysis with higher sensitivity would be the final MB result
- TBL (solid) is better at high Δm^2
- 90% CL defined by $\Delta\chi^2 = 1.64$



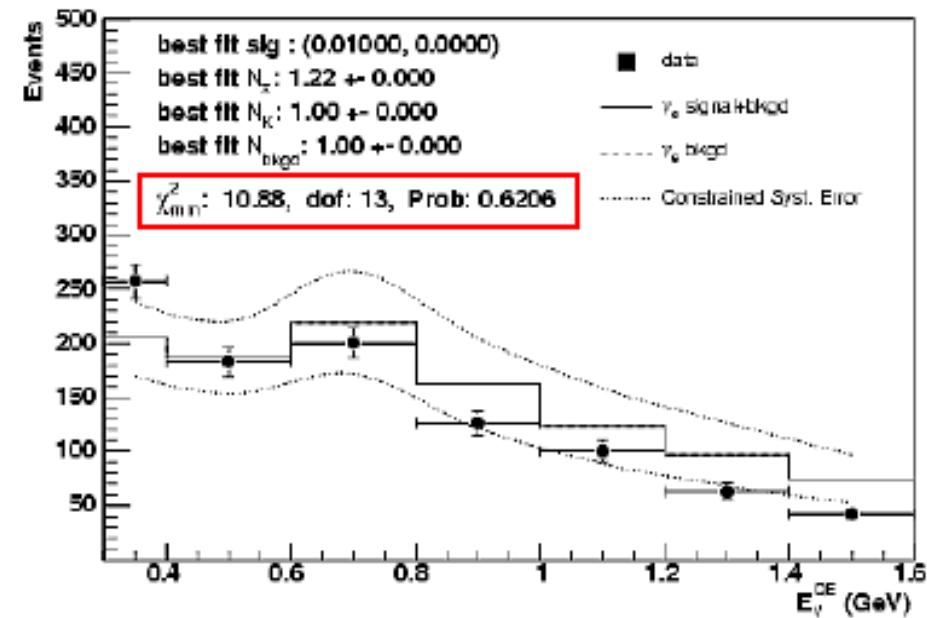
After many man-years and CPU-hours...



Finally we see the data in the signal region...

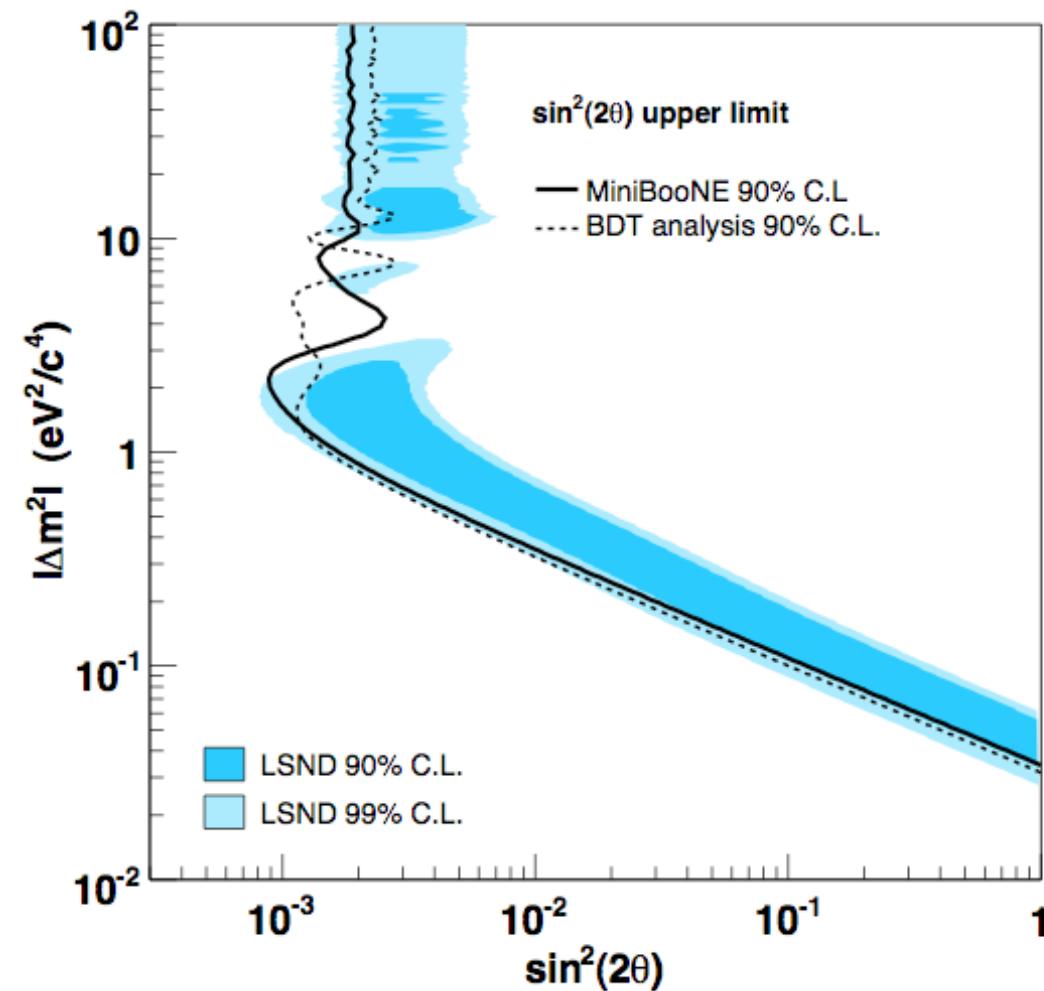


- TBL shows no sign of an excess in the analysis region (where the LSND signal is expected for the 2v mixing hypothesis)
- Visible excess at low E



Neither analysis shows an evidence for $\nu_\mu \rightarrow \nu_e$ appearance in the analysis region

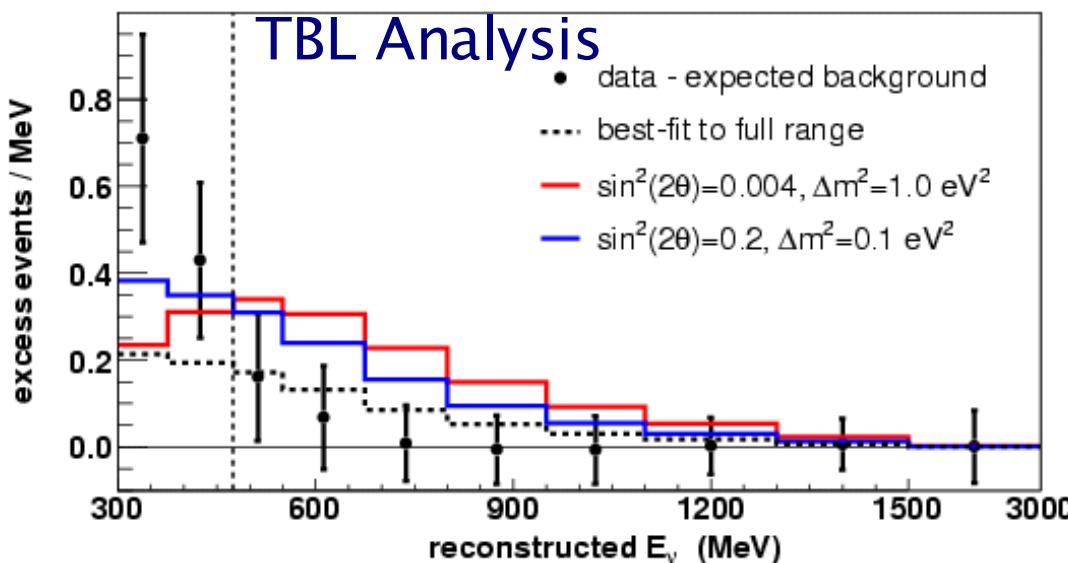
Fit results mapped into $\sin^2(2\theta)$ Δm^2 plane



- Energy-fit analysis:
 - solid: TBL
 - dashed: BDT
- Independent analyses in good agreement
- Looks similar to sensitivity because of the lack of a signal
- Had there been a signal, these curves would have curled around and closed into contours
- MiniBooNE and LSND incompatible at a 98% CL for all Δm^2 under a 2ν mixing hypothesis.

Future work for MiniBooNE

- Papers in support of this analysis
 - NC π^0 background measurement
 - ν_μ CCQE analysis
- Continued improvements of the ν oscillation analysis
 - Combined BDT and TBL
 - More work on reducing systematics
- Re-examine low E backgrounds and significance of low E excess



- Lots of work on cross-sections
- MB has more ν_μ interactions than prior experiments in an energy range useful to future ν expts.
- Event counts before cuts:

ν channel	events
all channels	810k
CC quasielastic	340k
NC elastic	150k
CC π^+	180k
CC π^0	30k
NC π^0	48k
NC $\pi^{+/-}$	27k
CC/NC DIS, multi- π	35k

$\bar{\nu}$ channel	events
all channels	54k
CC quasielastic	24k
NC elastic	10k
CC π^-	8.9k
CC π^0	1.7k
NC π^0	4.9k
NC $\pi^{+/-}$	1.8k
CC/NC DIS, multi- π	1.9k

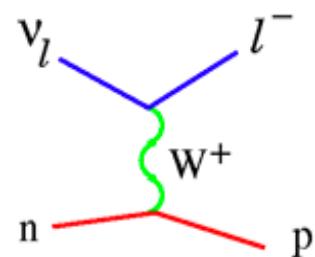
6×10^{20} POT
 ν mode

2×10^{20} POT
 $\bar{\nu}$ mode

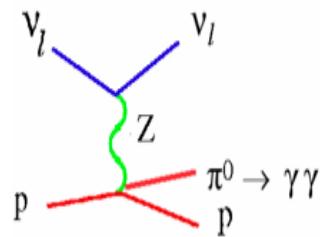
- Currently running in anti- ν mode for anti- ν cross sections

MB cross-section analyses from Nulnt07...

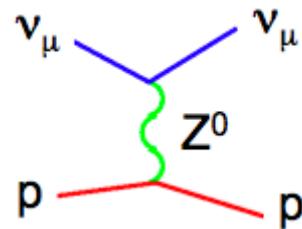
• ν_μ CCQE



• NC π^0

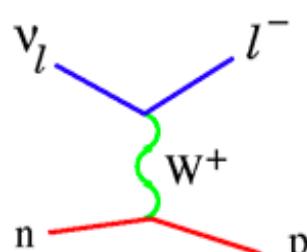


• NC elastic

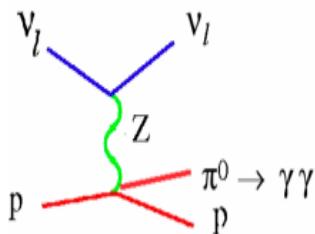


MB cross-section analyses from Nulnt07...

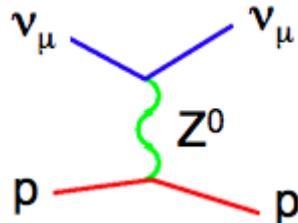
• ν_μ CCQE



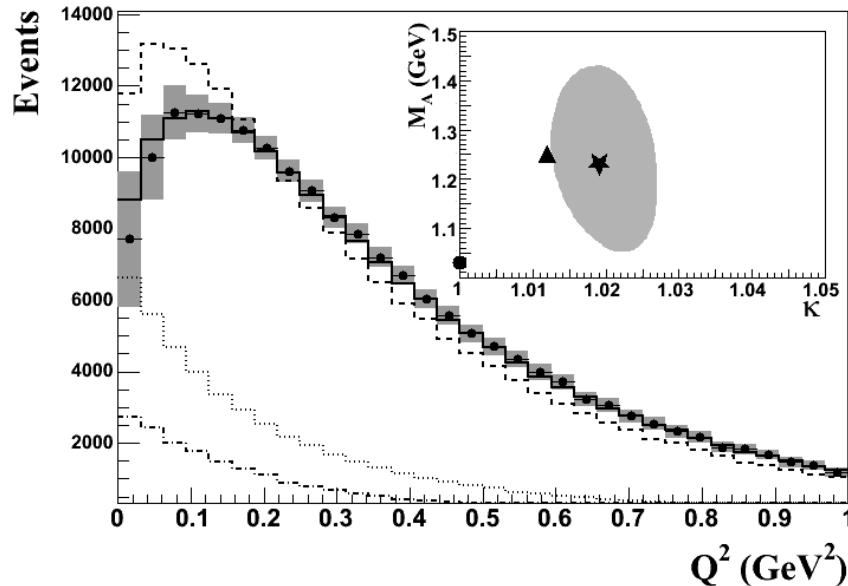
• NC π^0



• NC elastic



ν_μ CCQE Q^2 distribution (hep-ex/0706.0926)

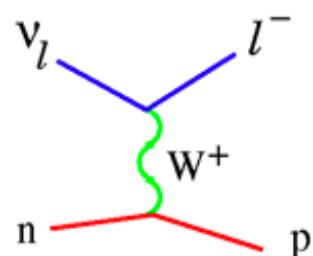


- 198,000 events allows for detailed 1 and 2d kinematic views
- Agreement between data (points) and MC (solid) after fitting for modified Fermi gas parameters
- 'Golden channel' for normalizing flux X xsec in oscillation analysis

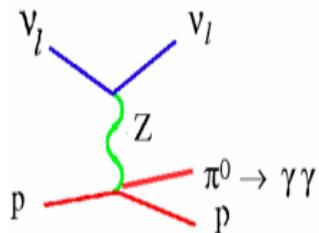
T. Katori, Nulnt07

MB cross-section analyses from NuInt07...

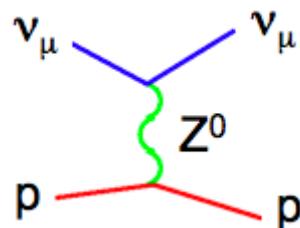
• ν_μ CCQE



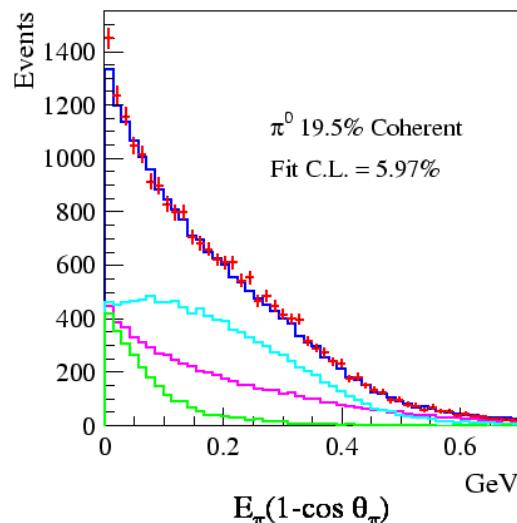
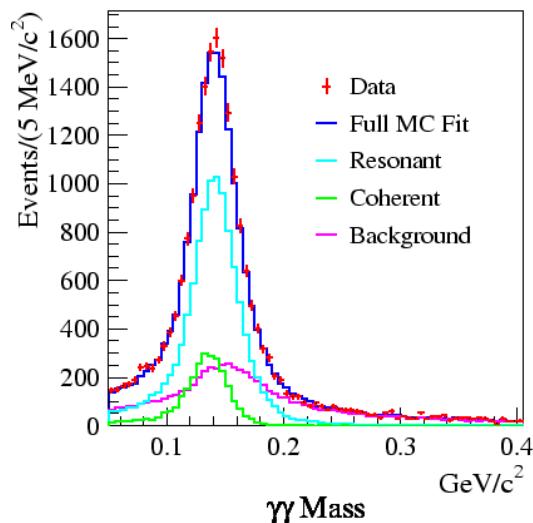
• NC π^0



• NC elastic



NC π^0 fits to resonant/coherent fractions

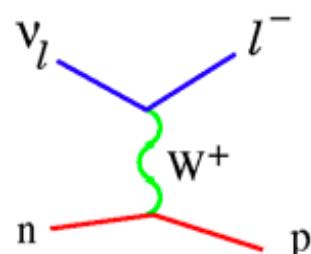


- 28,600 events, largest sample to date
- For MB flux and Nuance model we find that $(19.5 \pm 1.1)\%$ of exclusive NC π^0 production is coherent
- Very important background for oscillation analysis

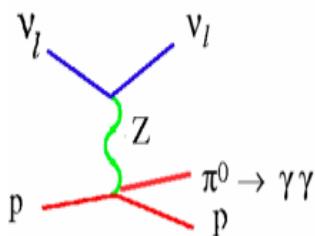
J. Link, NuInt07

MB cross-section analyses from NuInt07...

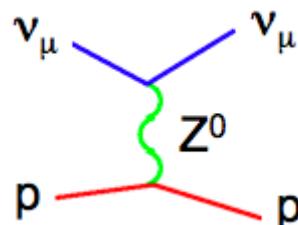
- ν_μ CCQE



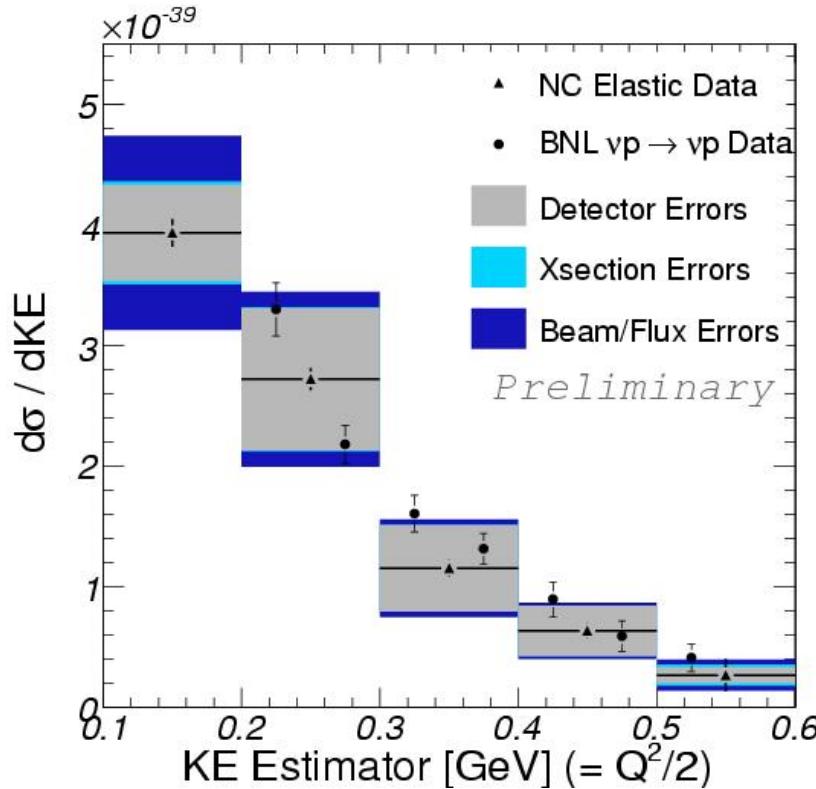
- NC π^0



- NC elastic



NC elastic absolute cross section



- Data shown is 10% of total sample
- Comparison to BNL E734
- First differential cross section from MB

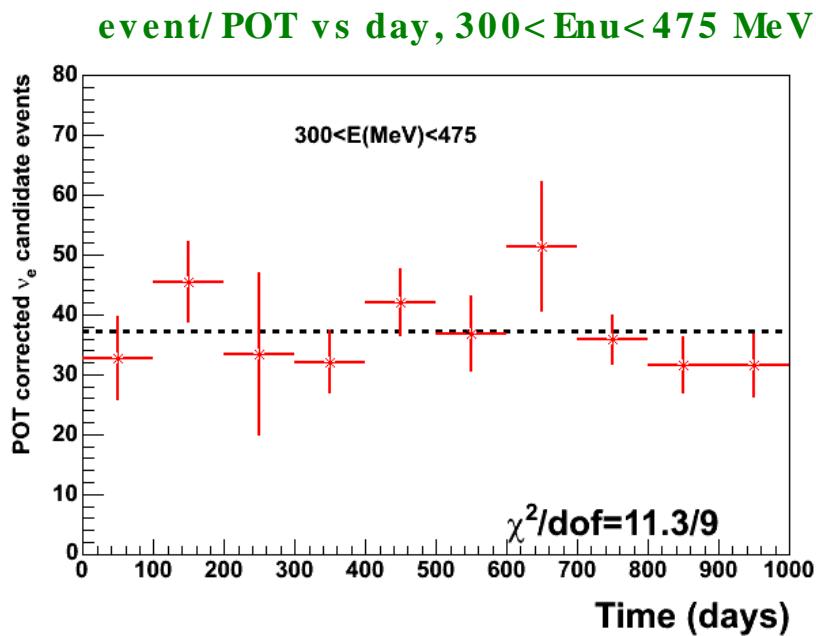
D. Cox, NuInt07



Update on the low E excess...

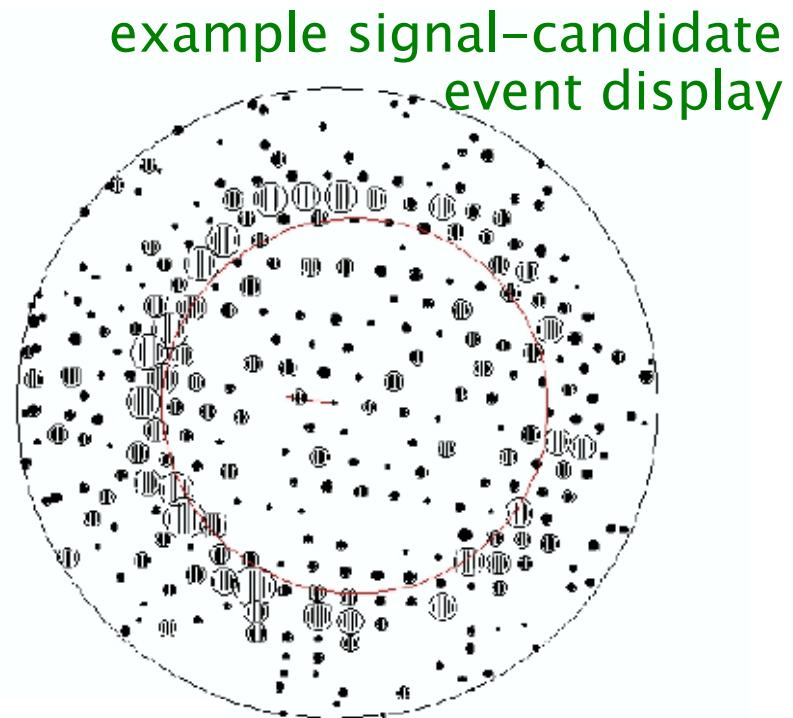
No Detector anomalies found

- Example: rate of electron candidate events is constant (within errors) over course of run



No Reconstruction problems found

- All low-E electron candidate events have been examined via event displays, consistent with 1-ring events



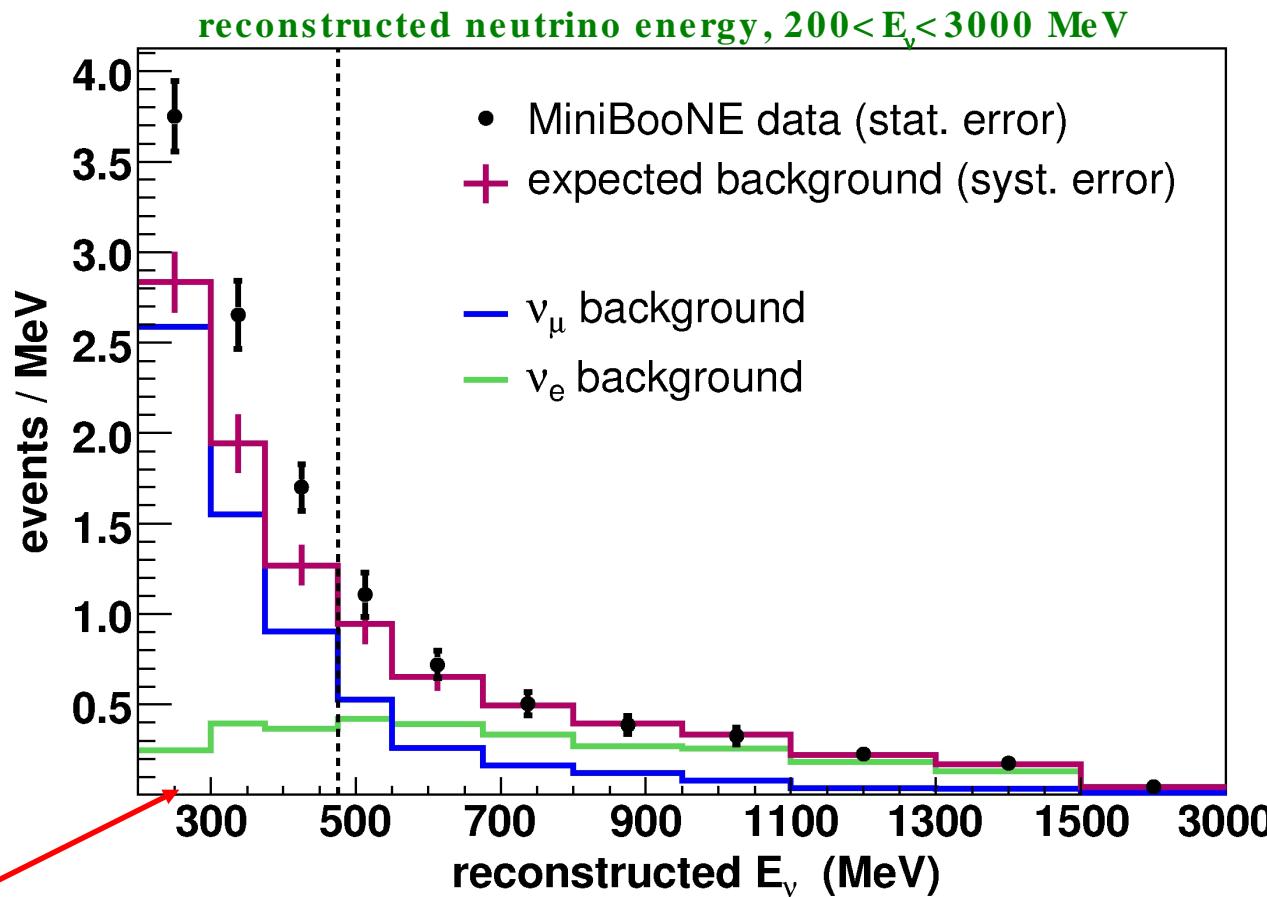
Signal candidate events are consistent with single-ring neutrino interactions

- But could be either electrons or photons



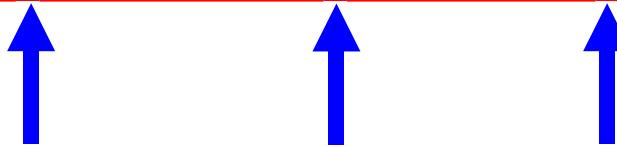
Update on the low E excess...

Excess persists below 300 MeV but background is also rising



Update on the low E excess...

E_ν^{QE} MeV]	200–300	300–475	475–1250
<u>total background</u>	284 ± 25	274 ± 21	358 ± 35 (syst.error)
ν_e <i>intrinsic</i>	26	67	229
ν_μ <i>induced</i>	258	207	129
<i>NC</i> π^0	115	76	62
<i>NC</i> $\Delta \rightarrow N\gamma$	20	51	20
<i>Dirt</i>	99	50	17
<i>other</i>	24	30	30
Data	375 ± 19	369 ± 19	380 ± 19 (stat.error)
<i>Data+MC</i>	91 ± 31	95 ± 28	22 ± 40 (stat+syst)

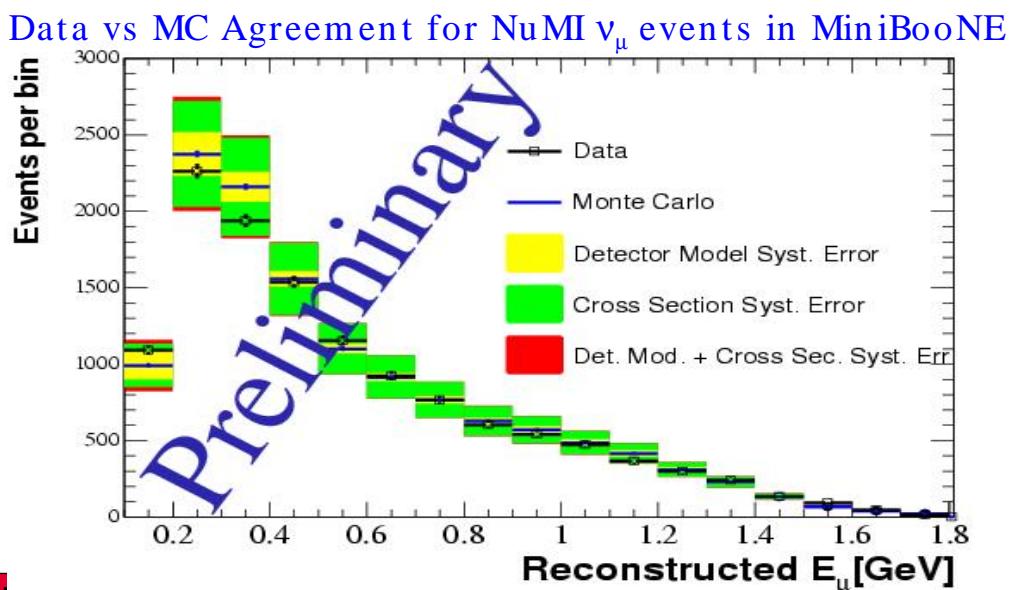
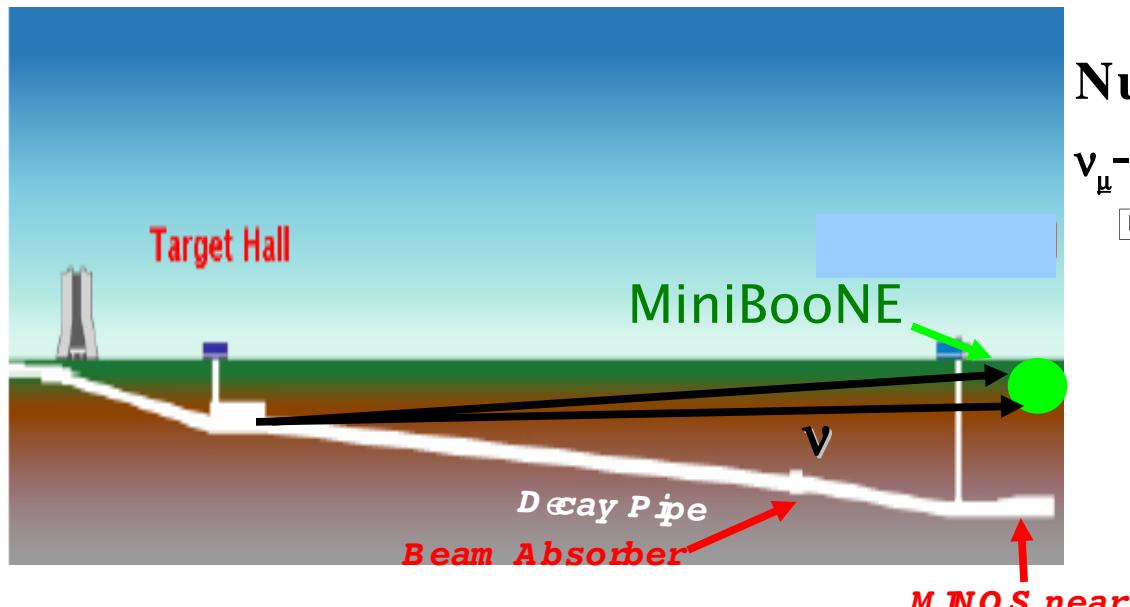


- NC π^0 largest
- Dirt background significant
- NC $\Delta \rightarrow N\gamma$ falling off
- Intrinsic ν_e negligible
- Three main:
 - NC π^0
 - Dirt bkgnd
 - NC $\Delta \rightarrow N\gamma$
- Intrinsic ν_e small

★ Systematics/backgrounds at low E still under study...



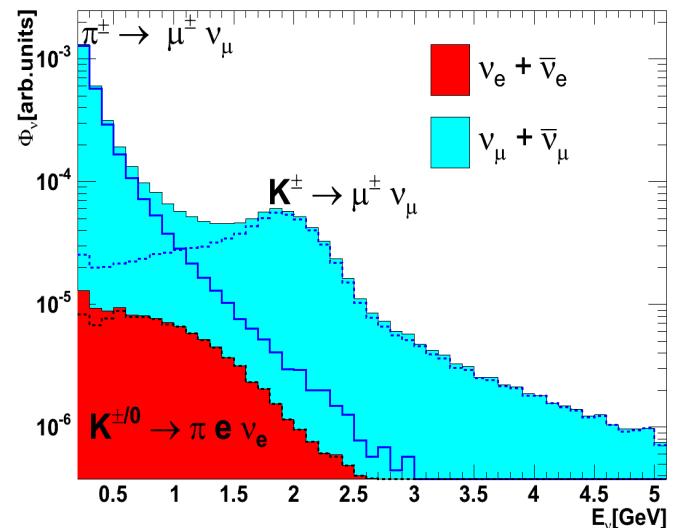
NuMI neutrinos in the MB detector...



NuMI event composition:

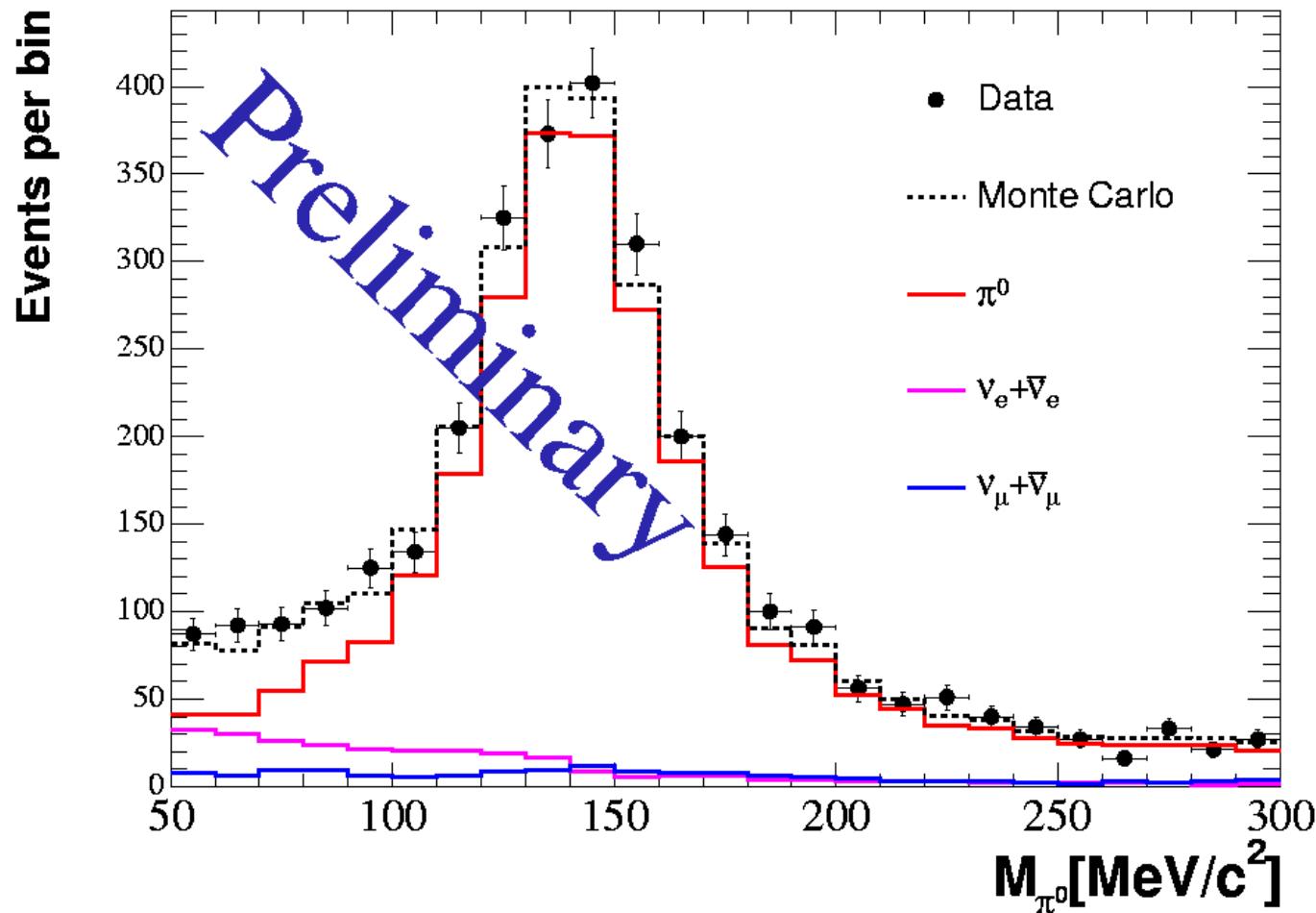
ν_μ - 81 %, ν_e - 5 %, $\bar{\nu}_\mu$ - 13 %, $\bar{\nu}_e$ - 1 %

NuMI v Flux at MiniBooNE



The beam at MiniBooNE from NuMI is significantly **enhanced** in ν_e from K decay because of the off-axis position.

Analysis of π^0 events from NuMI beam



- Good data/MC agreement for π^0 events
- Ready to finalize background predictions/systematics
- Final step: Look for ν_e oscillation or excess

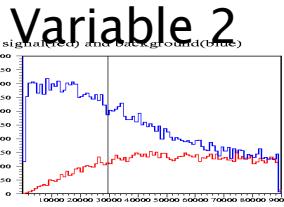


Backup Slides



Decision tree example

(sequential series of cuts
based on MC study)



Variable 2

1906/11828

9755/23695

7849/11867

20455/3417

9790/12888

$(N_{\text{signal}}/N_{\text{bkgd}})$

sig-like

9755/23695

bkgd-like

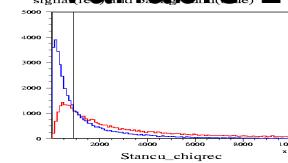
30,245/16,305

20455/3417

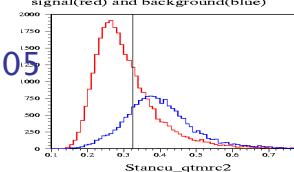
9790/12888

etc.

Variable 1



Variable 3



- Optimal cuts on each variable are determined
- An event gets a weight of 1 if signal
-1 if background
- Hard to identify backgrounds are iteratively given more weight
- Many trees built
- PID 'score' established from ensemble

This tree is one of many possibilities...

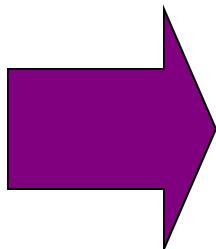


Handling uncertainties in the analysis

What we begin with...

For a given source
of uncertainty,

Errors on a wide range
of parameters
in the underlying model



... what we need

For a given source
of uncertainty,

Errors in bins of
 E_v^{QE}
and information on
the correlations
between bins

Incorporating the ν_μ constraint into the errors

Two Approaches

TBL: Reweight MC prediction to match measured ν_μ result
(accounting for systematic error correlations)

BDT: include the correlations of ν_μ to ν_e in the error matrix:

$$\chi^2 = \begin{pmatrix} \Delta_i^{\nu_e} & \Delta_i^{\nu_\mu} \end{pmatrix} \begin{pmatrix} M_{ij}^{e,e} & M_{ij}^{e,\mu} \\ M_{ij}^{\mu,e} & M_{ij}^{\mu,\mu} \end{pmatrix}^{-1} \begin{pmatrix} \Delta_j^{\nu_e} \\ \Delta_j^{\nu_\mu} \end{pmatrix}$$

where $\Delta_i^{\nu_e} = \text{Data}_i^{\nu_e} - \text{Pred}_i^{\nu_e}(\Delta m^2, \sin^2 2\theta)$ and $\Delta_i^{\nu_\mu} = \text{Data}_i^{\nu_\mu} - \text{Pred}_i^{\nu_\mu}$

Systematic (and statistical) errors are included in $(M_{ij})^{-1}$,
where i, j are bins of E_v^{QE}



Example: Underlying X-section parameter errors

(Many are common to ν_μ and ν_e and cancel in the fit)

M_A^{QE} , e_{lo}^{sf}	6%, 2% (stat + bkg only)	determined from MiniBooNE ν_μ QE data
QE σ norm	10%	
QE σ shape	function of E_ν	
ν_e/ν_μ QE σ	function of E_ν	

NC π^0 rate	function of π^0 mom	determined from MiniBooNE ν_μ NC π^0 data
M_A^{coh} , coh σ	$\pm 25\%$	
$\Delta \rightarrow N\gamma$ rate	function of γ mom + 7% BF	

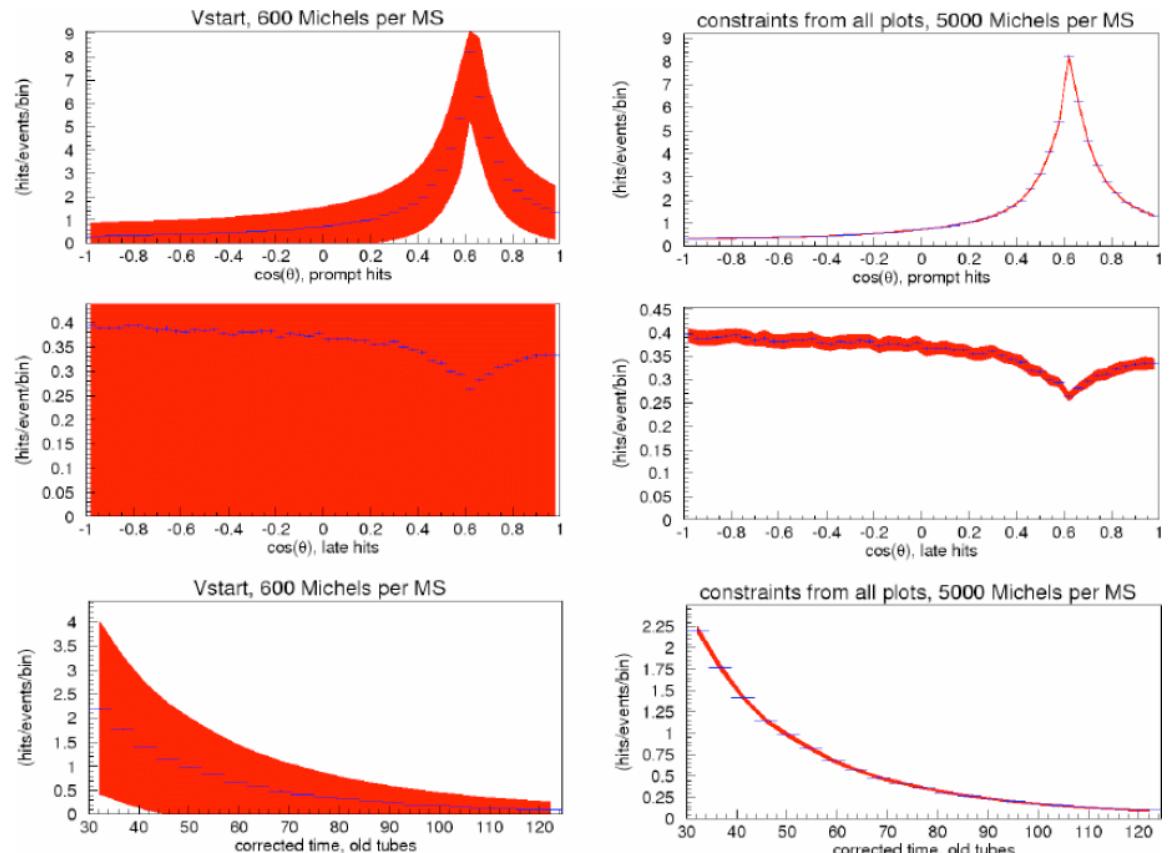
E_B , p_F	9 MeV, 30 MeV	determined from other experiments
Δs	10%	
$M_A^{1\pi}$	25%	
$M_A^{N\pi}$	40%	
DIS σ	25%	



Extracting the OM systematic error

- external measurements essential
- **finish with μ decay events (low-energy electrons)**
(~unlimited supply and fast to simulate)

- use a Monte Carlo method to reduce uncertainty:
- compare data/MC events in relevant distributions for many allowed models
- de-weight disallowed regions of model space
- NC elastic events help out with scintillation



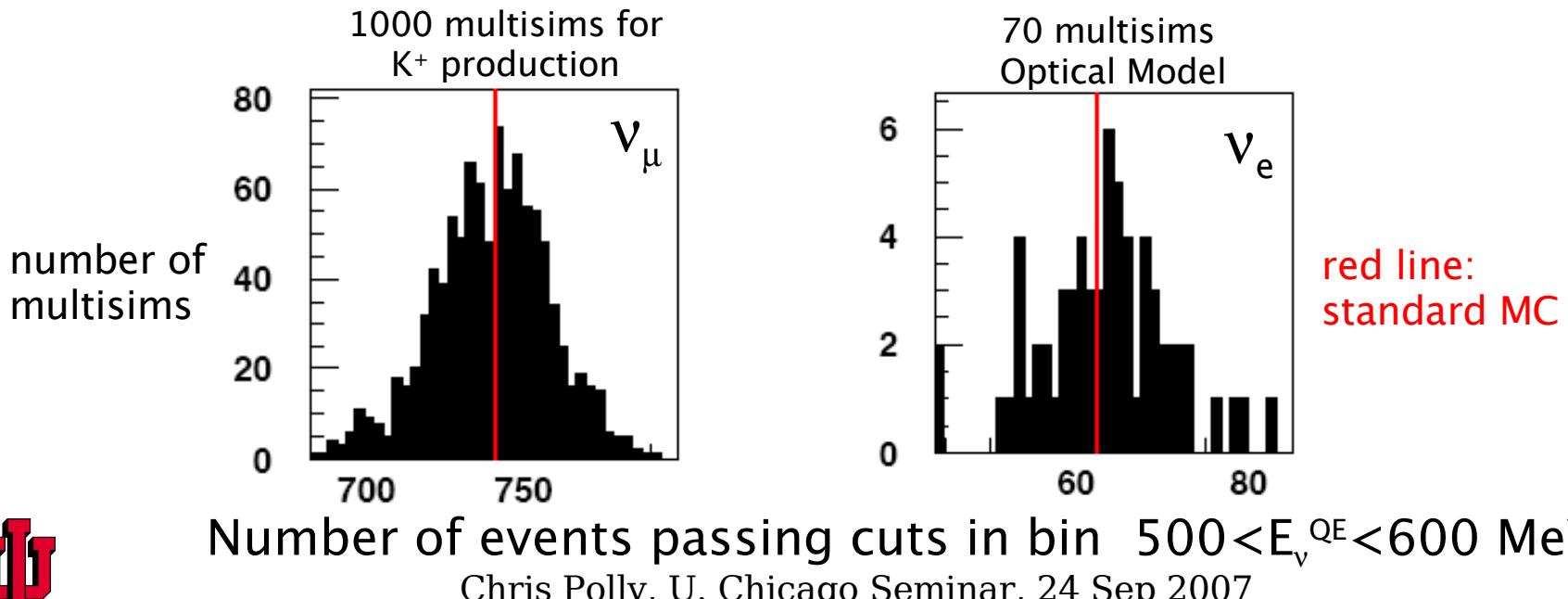
Chris Polly, U. Chicago Seminar, 24 Sep 2007
starting uncertainties in
three of the distributions

(near) ending uncertainties
60



“Multisim” approach to assessing systematics

- A multisim is defined as a random draw from the underlying parameter that is considered allowed
- Allowed means the draw does not violate internal or external constraints
- Draws are taken from covariance matrices that dictate how parameters are allowed to change in combination, imagine Cerenkov and scintillation as independent sources of light but requiring the Michel energy to be conserved
- For flux and X-section multisims can be done via reweighting, optical model requires running hit level simulation



Optical model error matrix

$$E_{ij} = \frac{1}{M} \sum_{a=1}^M \left(N_i^a - N_i^{CV} \right) \left(N_j^{MC} - N_j^{CV} \right)^{MC}$$

- N is number of events passing cuts
- MC is standard monte carlo
- α represents a given multisim
- M is the total number of multisims
- i,j are E_ν^{QE} bins

Total error matrix is calculated from the sum of 9 independent sources

TB: ν_e -only total error matrix
BDT: $\nu_\mu - \nu_e$ total error matrix

Correlations between E_ν^{QE} bins from the optical model:

