

Lectures on Neutrino Physics

Lake Louise School

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Lecture 1:

Neutrino Interactions

Example: NuTeV $\sin^2\theta_W$ Measurement

Direct Neutrino Mass Measurements

Neutrino Oscillation Phenomenology

Solar Neutrinos (part 1)

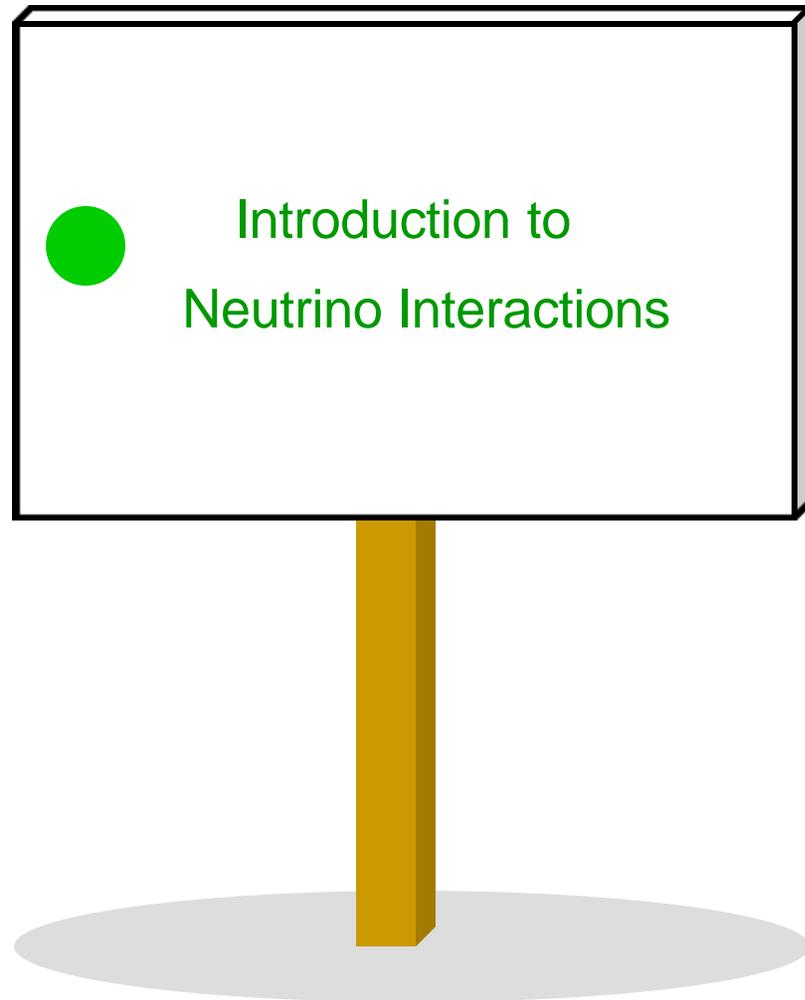
Lecture 2:

Solar Neutrinos (part 2)

Atmospheric and Longbaseline Exps.

LSND Region Experiments

Summary and Conclusions



● Introduction to
Neutrino Interactions

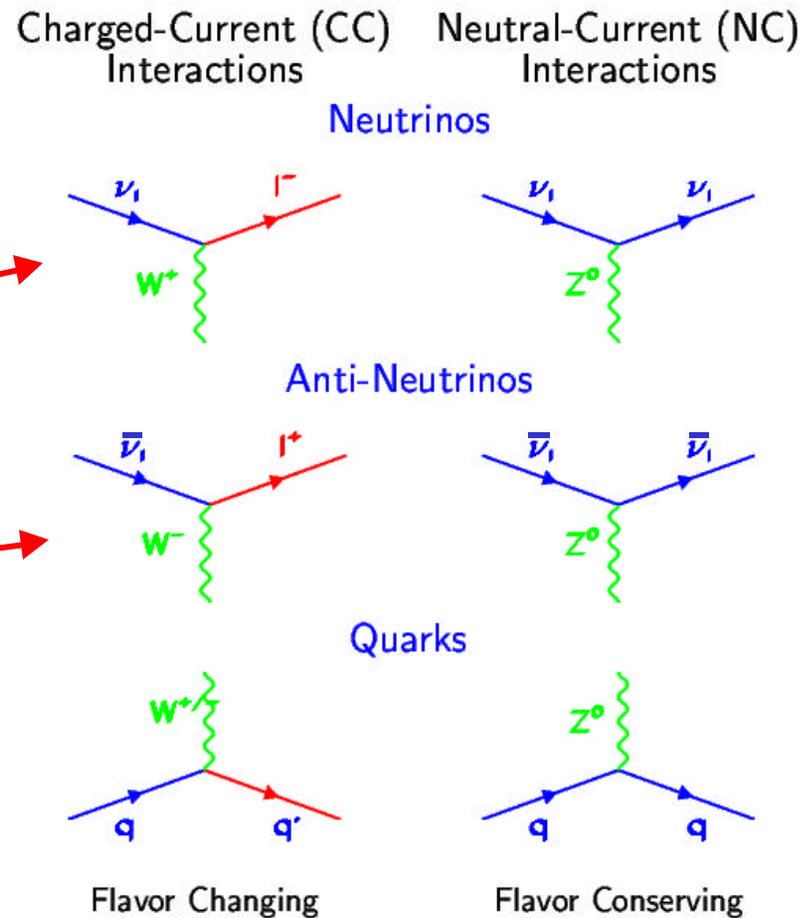
Neutrino Interactions

- W exchange gives Charged-Current (CC) events and Z exchange gives Neutral-Current (NC) events

In CC events the outgoing lepton determines if neutrino or antineutrino

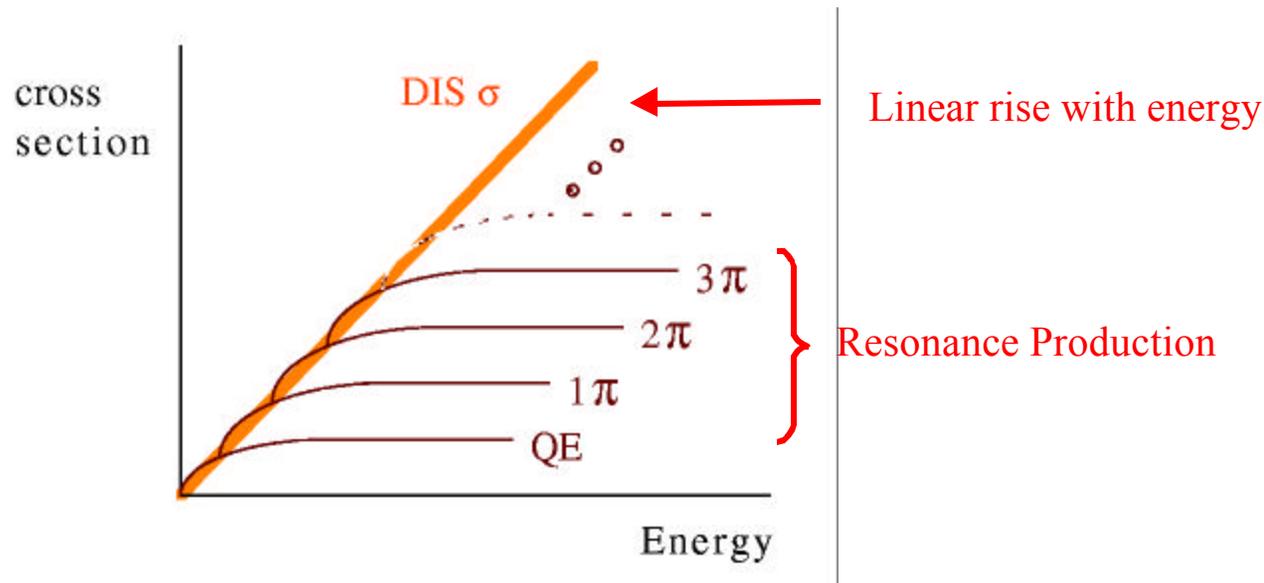
$$l^- \rightarrow n$$

$$l^+ \rightarrow \bar{n}$$



Neutrino-Nucleon Processes

- Charged - Current: W^\pm exchange
 - Quasi-elastic Scattering:
(Target changes but no break up)
 $\nu_\mu + n \rightarrow \mu^- + p$
 - Nuclear Resonance Production:
(Target goes to excited state)
 $\nu_\mu + n \rightarrow \mu^- + p + \pi^0$ (N^* or Δ)
 $n + \pi^+$
 - Deep-Inelastic Scattering:
(Nucleon broken up)
 $\nu_\mu + \text{quark} \rightarrow \mu^- + \text{quark}'$
- Neutral - Current: Z^0 exchange
 - Elastic Scattering:
(Target doesn't break up or change)
 $\nu_\mu + N \rightarrow \nu_\mu + N$
 - Nuclear Resonance Production:
(Target goes to excited state)
 $\nu_\mu + N \rightarrow \nu_\mu + N + \pi$ (N^* or Δ)
 - Deep-Inelastic Scattering
(Nucleon broken up)
 $\nu_\mu + \text{quark} \rightarrow \nu_\mu + \text{quark}$



Neutrinos Are Left-Handed (Helicity and Handedness)

- **Helicity** is projection of spin along the particles direction
 - Frame dependent (if massive)

The operator: $\sigma \cdot \mathbf{p}$



- Neutrinos only interact weakly with a (V-A) interaction
 - All **neutrinos** are **left-handed**
 - All **antineutrinos** are **right-handed**

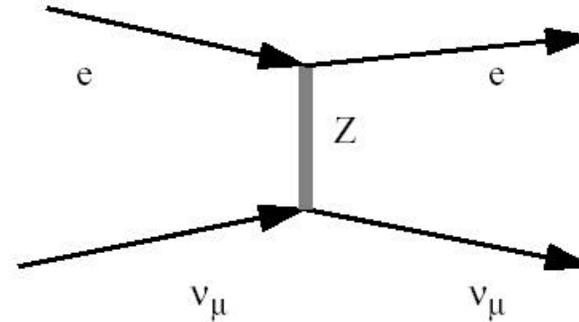
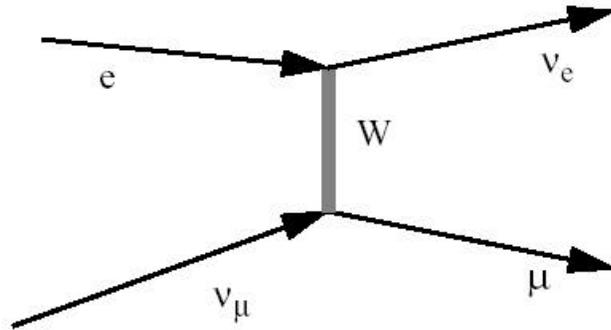
- If neutrinos have mass then left-handed neutrino is:
 - Mainly left-helicity
 - But also small right-helicity component $\propto m/E$

- **Handedness (or chirality)** is Lorentz-invariant
 - Only same as helicity for massless particles.

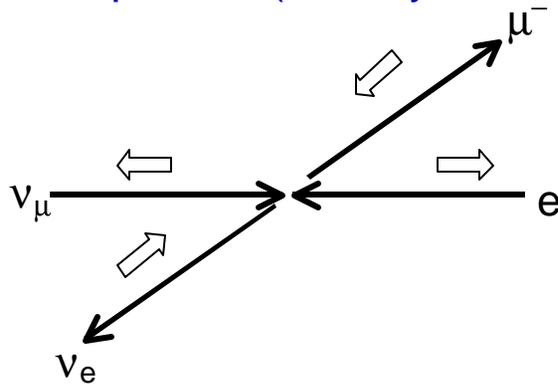
- Only left-handed charged-leptons (e^-, μ^-, τ^-) interact weakly but mass brings in right-helicity:

$$\begin{aligned}
 R_{theory} &= \frac{\Gamma(\pi^\pm \rightarrow e^\pm \nu_e)}{\Gamma(\pi^\pm \rightarrow \mu^\pm \nu_\mu)} \\
 &= \left(\frac{m_e}{m_\mu}\right)^2 \left(\frac{m_\pi^2 - m_e^2}{m_\pi^2 - m_\mu^2}\right)^2 \\
 &= 1.23 \times 10^{-4}
 \end{aligned}$$

Neutrino-Electron Scattering



- **Inverse μ -decay:** $\nu_\mu + e^- \rightarrow \mu^- + \nu_e$
 - Total spin $J=0$ (Helicity conserved)



- Point scattering $\Rightarrow \sigma \propto s = 2m_e E_\nu$

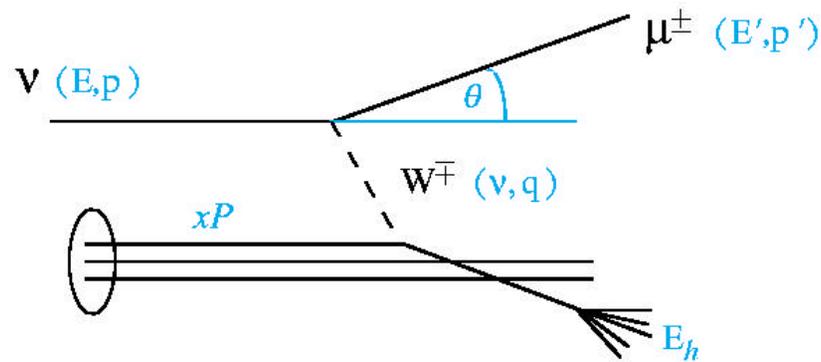
$$\mathbf{s}_{TOT} = \frac{G_F^2 s}{p} = 17.2 \pm 10^{-42} \text{ cm}^2 / \text{GeV} \cdot E_n (\text{GeV})$$

- **Elastic Scattering:** $\nu_\mu + e^- \rightarrow \nu_\mu + e^-$
 - Point scattering $\Rightarrow \sigma \propto s = 2m_e E_\nu$
 - Electron coupling to Z^0
 - (V-A): $-1/2 + \sin^2\theta_W$ $J=0$
 - (V+A): $\sin^2\theta_W$ $J=1$

$$\mathbf{s}_{TOT} = \frac{G_F^2 s}{p} \left(\frac{1}{4} - \sin^2 \theta_W + \frac{4}{3} \sin^4 \theta_W \right)$$

Scattering: Scaling Variables

DEEP INELASTIC NEUTRINO SCATTERING



Measured quantities: E_h, E', θ

Kinematic Quantities (Use 4 - vector invariants)

$$\text{4 - momentum Transfer}^2: Q^2 = -(p_l - p_n)^2 \approx (4E_n E_l \sin^2(\mathbf{q}/2))_{Lab}$$

$$\text{Energy Transfer: } \mathbf{n} = ((p_l - p_n) \cdot p_T) / M_T = (E_n - E_l)_{Lab} = (E_h - M_T)_{Lab}$$

$$\text{Fractional Energy Transfer: } y = ((p_l - p_n) \cdot p_T) / (p_n \cdot p_T) = (E_h - M_T) / (E_h + E_l)_{Lab}$$

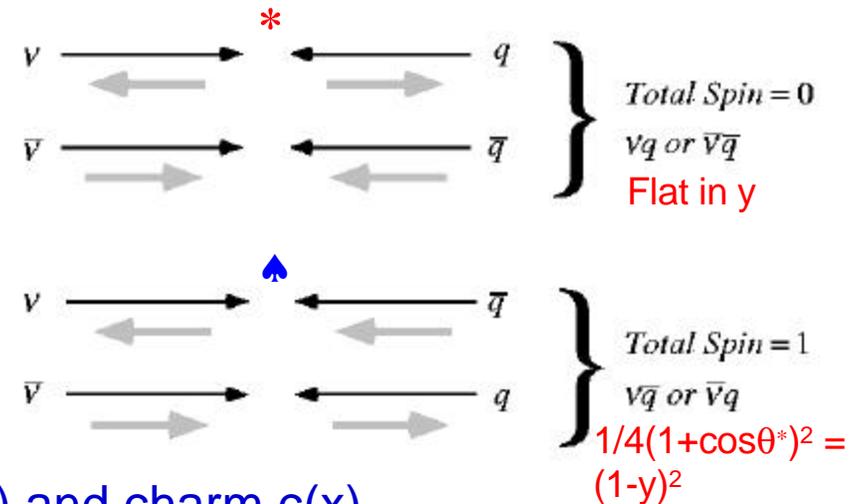
$$\text{Fractional Momentum of Struck Quark: } x = Q^2 / 2M_T \mathbf{n}$$

Neutrinos Probe Quark Structure

(Nucleon Structure Functions)

$$\frac{d\mathbf{S}^{np}}{dxdy} = \frac{G_F^2 S}{\mathbf{p}} \left(x d^p(x) + x \bar{u}^p(x) (1-y)^2 \right)$$

$$\frac{d\mathbf{S}^{nn}}{dxdy} = \frac{G_F^2 S}{\mathbf{p}} \left(x d^n(x) + x \bar{u}^n(x) (1-y)^2 \right)$$



– Need to add scattering off strange $s(x)$ and charm $c(x)$

- For an isoscalar target (# protons = # neutrons):

$$\frac{d^2 \mathbf{S}^{n(\bar{n})N}}{dxdy} = \frac{G_F^2 S}{2\mathbf{p}} \left\{ \left(1 + (1-y)^2 \right) F_2(x) \pm \left(1 - (1-y)^2 \right) x F_3^{n(\bar{n})}(x) \right\}$$

$$F_2^{n(\bar{n})N}(x) = x(u(x) + d(x) + \bar{u}(x) + \bar{d}(x) + s(x) + \bar{s}(x) + c(x) + \bar{c}(x)) = xq(x) + x\bar{q}(x)$$

$$xF_3^{n(\bar{n})N}(x) = xu_{val}(x) + xd_{val}(x) \pm 2x(s(x) - c(x))$$

$$\text{where } u_{val}(x) = u(x) - \bar{u}(x)$$

Neutrino Cross Section is Very Small

- Weak interactions are weak because of the massive W and Z boson exchange $\Rightarrow \sigma^{\text{weak}} \propto (1/M_W)^4$

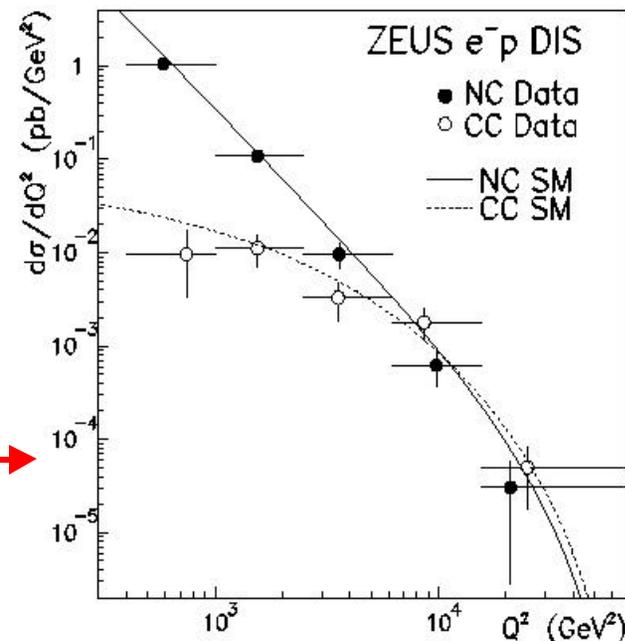
$$G_F = \frac{\sqrt{2}}{8} \left(\frac{g_W}{M_W} \right)^2 = 1.166 \times 10^{-5} / \text{GeV}^2 \quad (g_W \approx 0.7)$$

- For 100 GeV Neutrinos:

- $\sigma(\nu e) \sim 10^{-40}$ and $\sigma(\nu N) \sim 10^{-36} \text{ cm}^2$
vs. $\sigma(pp) \sim 10^{-26} \text{ cm}^2$
- Mean free path length in Steel*
 $\sim 3 \cdot 10^9$ meters!
(Need big detectors)

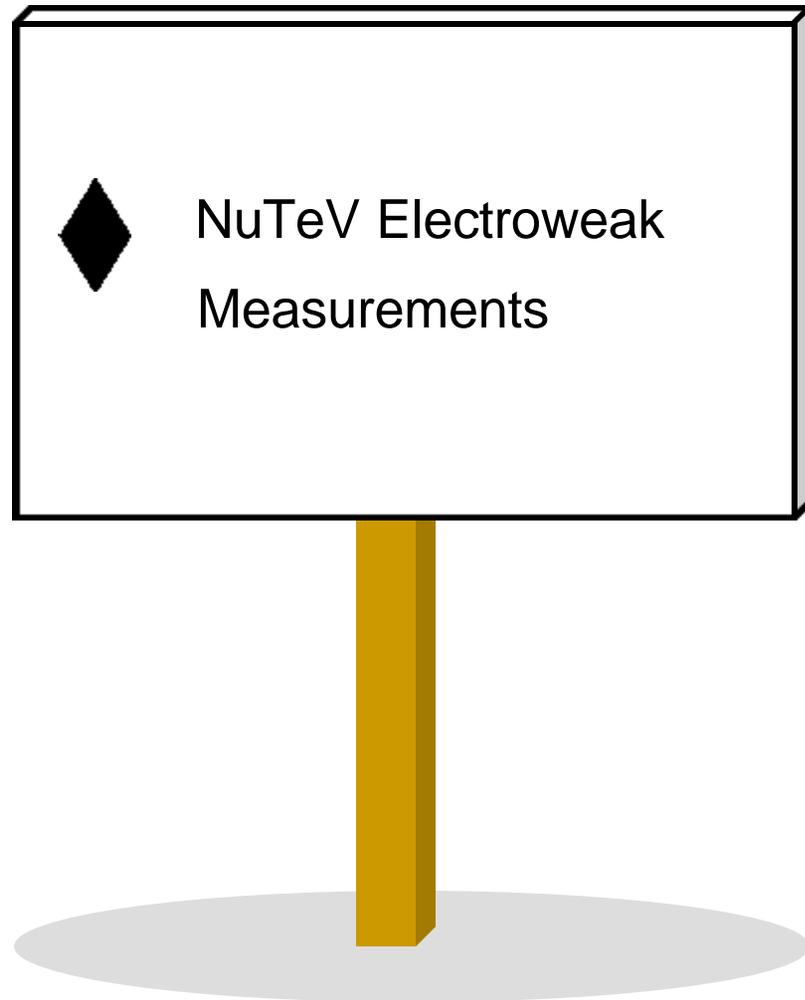
At Hera see W and Z propagator effects
- Also weak \sim EM strength

$$\sigma^{\text{EM}} \propto 1/Q^4$$



Neutrino Physics Topics

- Nucleon structure
 - Structure Functions – F_2 , xF_3
 - Strange sea – $s(x)$
 - Tests of QCD and measure α_s
 - Electroweak Measurements
 - Measure $\sin^2\theta_W$
 - Test GWS SU(2)xU(1) theory
 - Neutrino Properties
 - Neutrino mass
 - Direct measurements
 - Double beta decay
 - Neutrino Oscillations
- { See various review articles:
 (Conrad,Shaevitz,Bolton;
 RMP 70 (1998) 1341)
- { Brief Discussion Today
 about new NuTeV measurement
 (example of high-energy ν exp.)
- { Talk about direct mass
 measurements and then
 neutrino oscillations



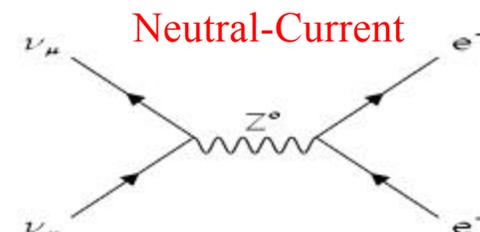
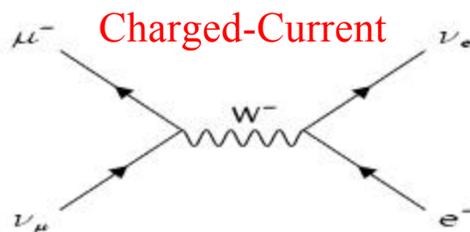
Electroweak Theory

- Standard Model
 - $SU(2) \otimes U(1)$ gauge theory unifying weak/EM
 \Rightarrow weak Neutral Current interaction
 - Measured physical parameters related to mixing parameter for the couplings, $g' = g \tan \theta_W$

<i>Z Couplings</i>	g_L	g_R
ν_e, ν_μ, ν_τ	1/2	0
e, μ, τ	$-1/2 + \sin^2 \theta_W$	$\sin^2 \theta_W$
u, c, t	$1/2 - 2/3 \sin^2 \theta_W$	$-2/3 \sin^2 \theta_W$
d, s, b	$-1/2 + 1/3 \sin^2 \theta_W$	$1/3 \sin^2 \theta_W$

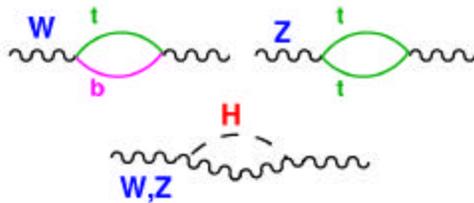
$$e = g \sin \theta_W, G_F = \frac{g^2 \sqrt{2}}{8M_W^2}, \frac{M_W}{M_Z} = \cos \theta_W$$

- Neutrinos are special in SM
 - Only have left-handed weak interactions
 $\Rightarrow W^\pm$ and Z boson exchange

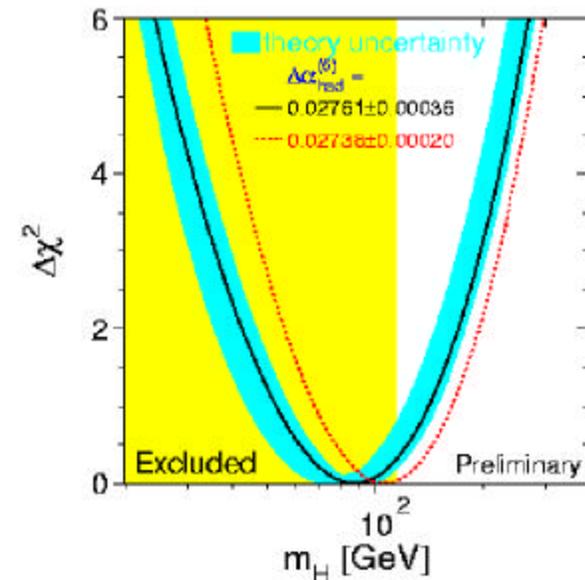


Current Era of Precision EW Measurements

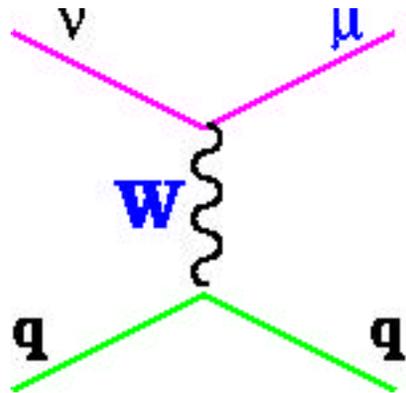
- Precision parameters define the SM:
 - $\alpha_{EM}^{-1} = 137.03599959(40)$ 45ppb (200ppm@ M_Z)
 - $G_\mu = 1.16637(1)\times 10^{-5} \text{ GeV}^{-2}$ 10ppm
 - $M_Z = 91.1871(21)$ 23ppm
- Comparisons test the SM and probe for new physics
 - LEP/SLD ($e+e^-$), CDF/D0 ($p-pbar$), νN , HERA (ep), APV



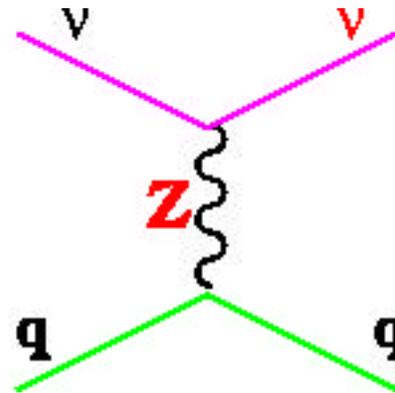
- Radiative corrections are large and sensitive to m_{top} and m_{Higgs}
 - M_{Higgs} *constrained in SM to be less than 196 GeV at 95%CL*



NuTeV Experimental Technique



$$\text{Coupling} \propto J_{\text{weak}}^{(3)}$$



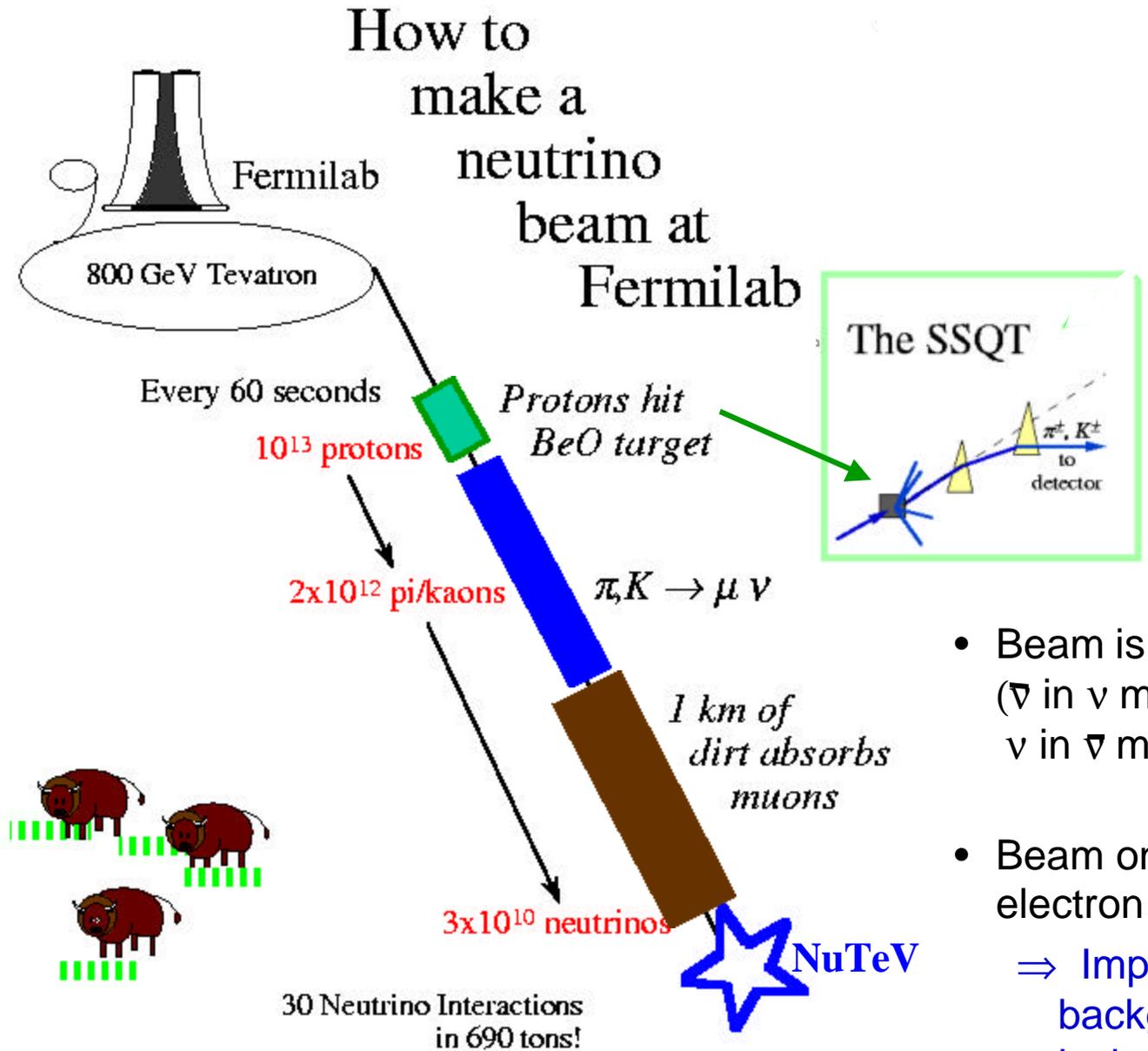
$$\text{Coupling} \propto \left(J_{\text{weak}}^{(3)} - Q_{em} \sin^2 \theta_W \right)$$

- For an isoscalar target composed of u,d quarks:

Llewellyn Smith Relation :

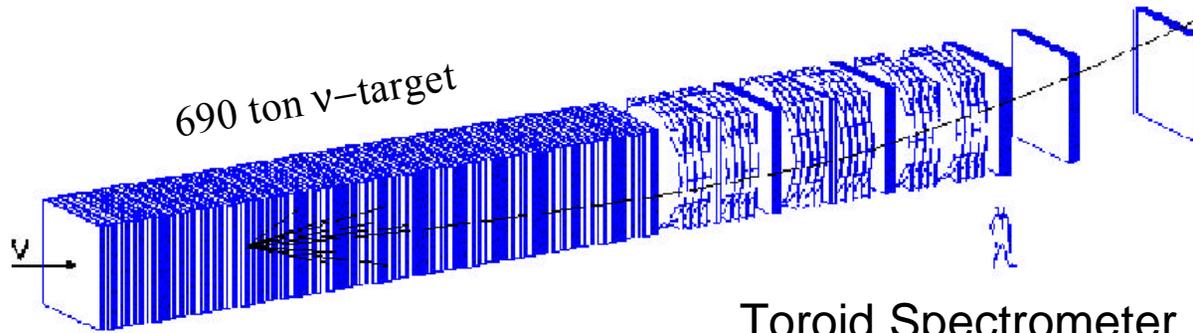
$$R^{n(\bar{n})} = \frac{S_{NC}^{n(\bar{n})}}{S_{CC}^{n(\bar{n})}} = r^2 \left(\frac{1}{2} - \sin^2 \theta_W + \frac{5}{9} \sin^4 \theta_W \left(1 + \frac{S_{CC}^{\bar{n}(n)}}{S_{CC}^{n(\bar{n})}} \right) \right)$$

- NC/CC ratio easiest to measure experimentally
but need separate neutrino and antineutrino running

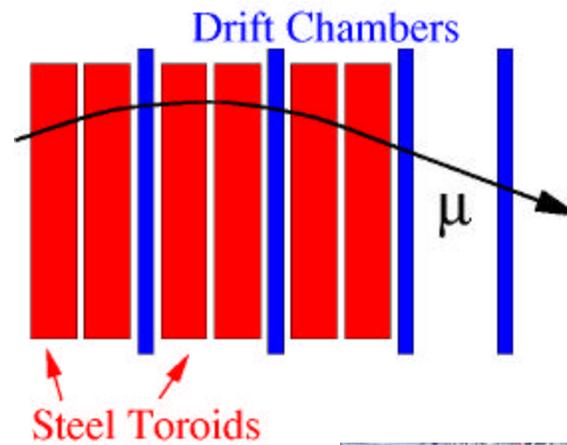
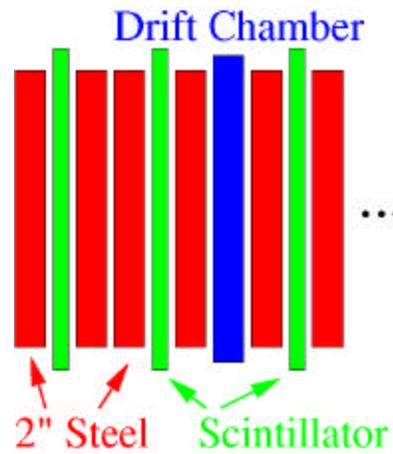


- Beam is very pure ($\bar{\nu}$ in ν mode 3×10^{-4} , ν in $\bar{\nu}$ mode 4×10^{-3})
- Beam only has $\sim 1.6\%$ electron neutrinos
 \Rightarrow Important background for isolating true NC event

NuTeV Detector

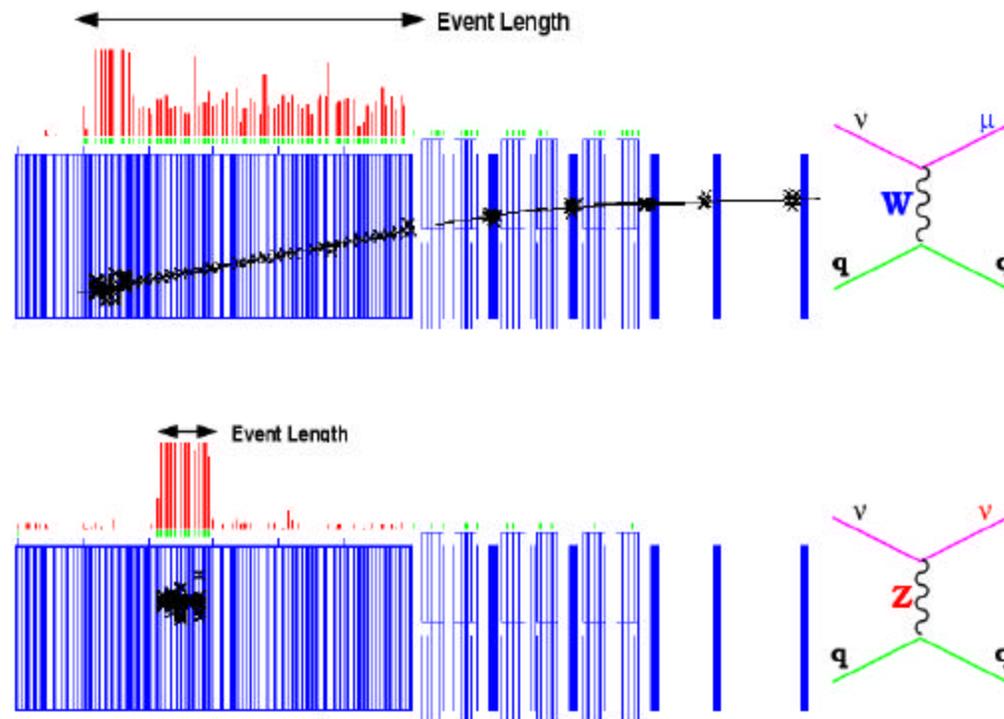


Target / Calorimeter



Neutral Current / Charged Current Event Separation

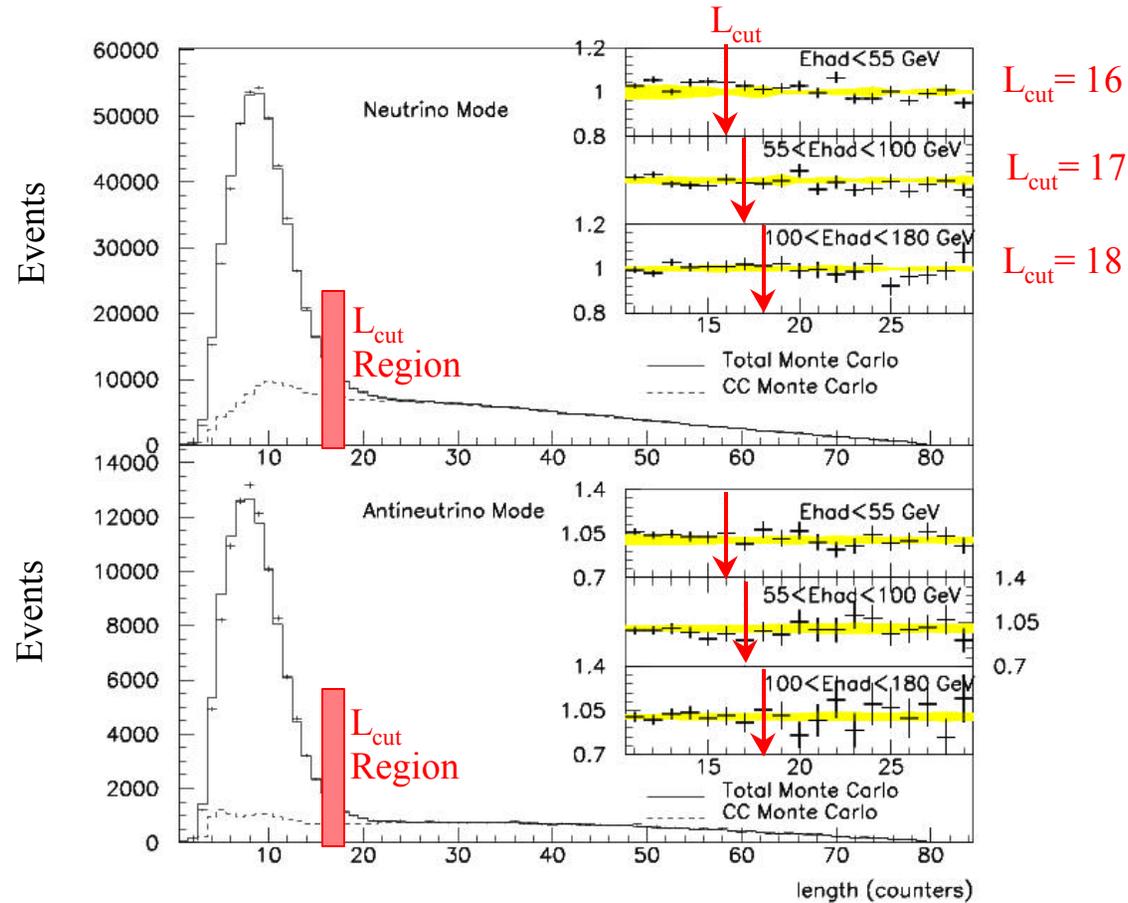
- Separate NC and CC events statistically based on the “event length” defined in terms of # counters traversed



$$R_{\text{exp}} = \frac{\text{SHORT events}}{\text{LONG events}} = \frac{L \leq L_{\text{cut}}}{L > L_{\text{cut}}} = \frac{\text{NC Candidates}}{\text{CC Candidates}}$$

(measure this ratio in both n and \bar{n} modes)

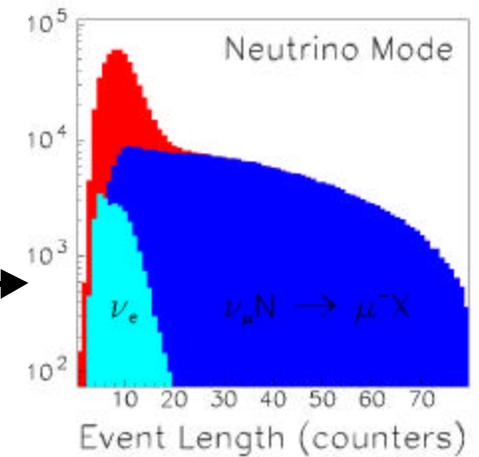
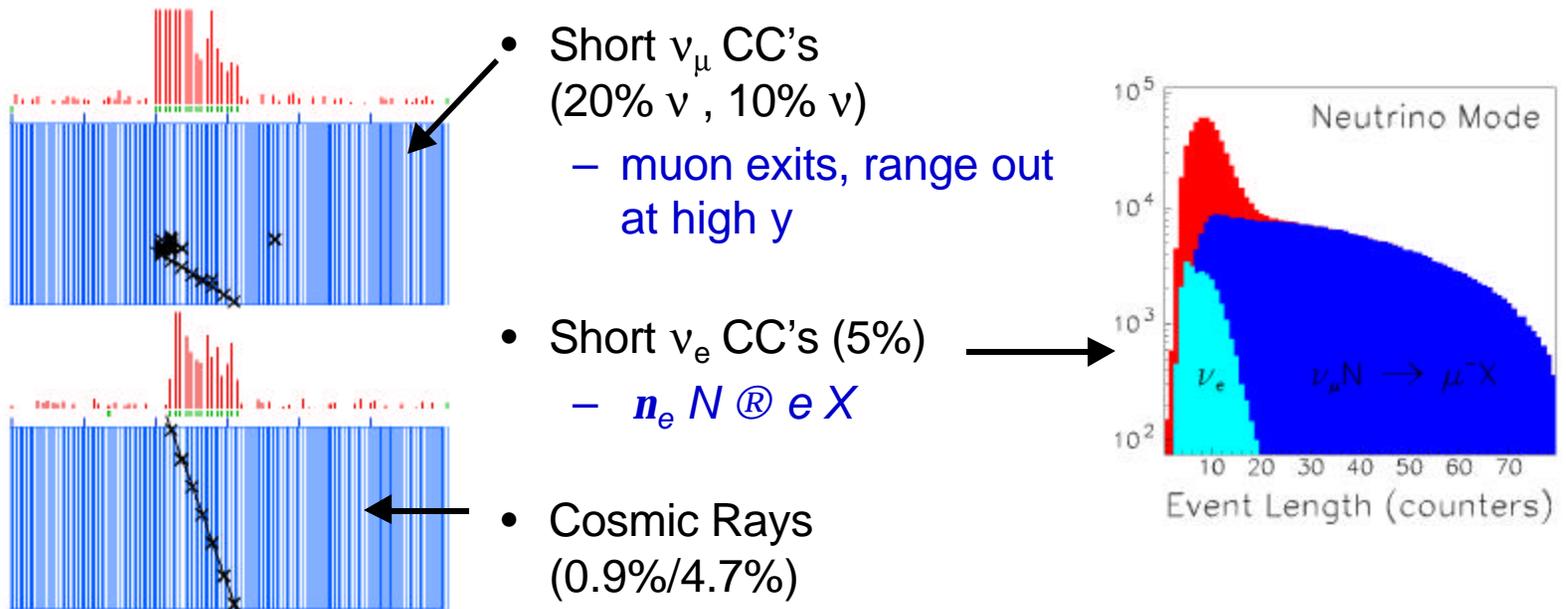
Determine R_{exp} : The Short to Long Ratio:



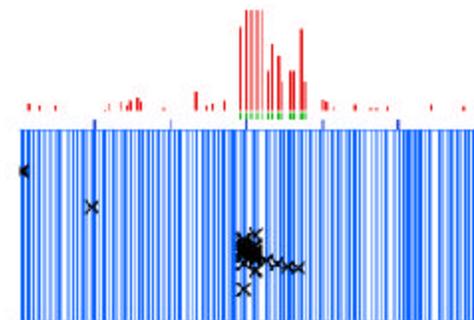
	Short (NC) Events	Long (CC) Events	$R_{exp} = \text{Short/Long}$
Neutrino	457K	1167K	0.3916 ± 0.0007
Antineutrino	101K	250K	0.4050 ± 0.0016

From R_{exp} to R^n

Need detailed Monte Carlo to relate R_{exp} to R^n and $\sin^2 \theta_W$



- Long ν_μ NC's (0.7%)
 - punch-through effects



Result from Fit to R^n and $R^{\bar{n}}$

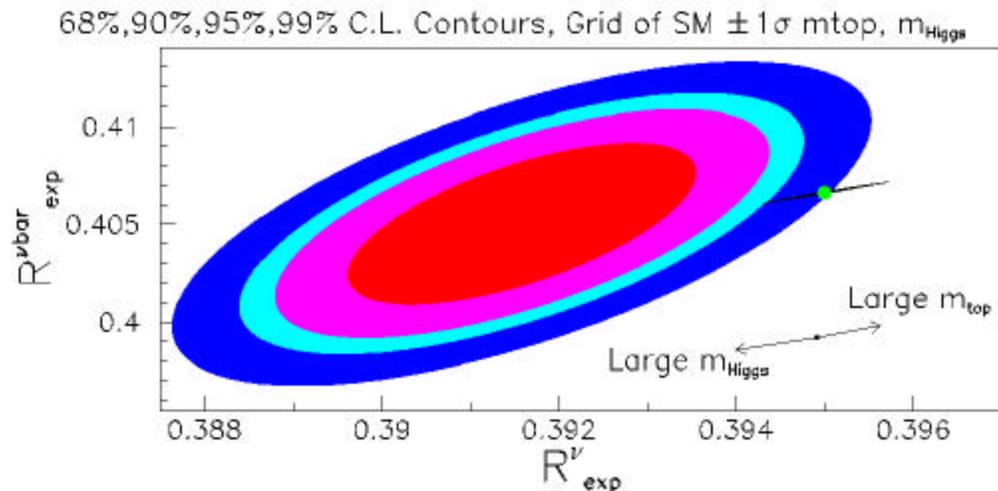
- NuTeV result:

$$\begin{aligned}\sin^2 \theta_W^{(on-shell)} &= 0.2277 \pm \pm 0.0013(stat.) \pm 0.0009(syst.) \\ &= 0.2277 \pm 0.0016\end{aligned}$$

(Previous neutrino measurements gave 0.2277 ± 0.0036)

- Standard model fit (LEPEWWG): 0.2227 ± 0.00037
A 3σ discrepancy

$R_{\text{exp}}^n = 0.3916 \pm 0.0013$ $(SM : 0.3950) \Leftarrow 3\sigma \text{ difference}$ $R_{\text{exp}}^{\bar{n}} = 0.4050 \pm 0.0027$ $(SM : 0.4066) \Leftarrow \text{Good agreement}$



Possible Interpretations

- Changes in Standard Model Fits
 - Change PDF sets
 - Change $M_{\text{higgs}} \Rightarrow \text{Need} > 1000 \text{ TeV} !$
- “Old Physics” Interpretations: QCD
 - Violations of “isospin” symmetry
 - Strange vs anti-strange quark asymmetry
- Are ν 's Different?
 - Special couplings to new particles
 - Majorana neutrino effects
 - Neutrino oscillations – ν_e disappearance
- “New Physics” Interpretations
 - New Z' or lepto-quark exchanges
 - New particle loop corrections

Two parameter fit to R_{exp}^n and $R_{\text{exp}}^{\bar{n}}$:

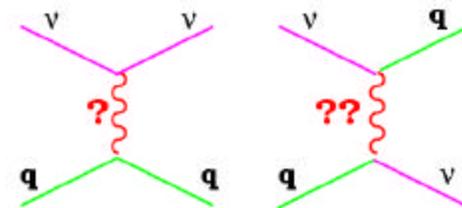
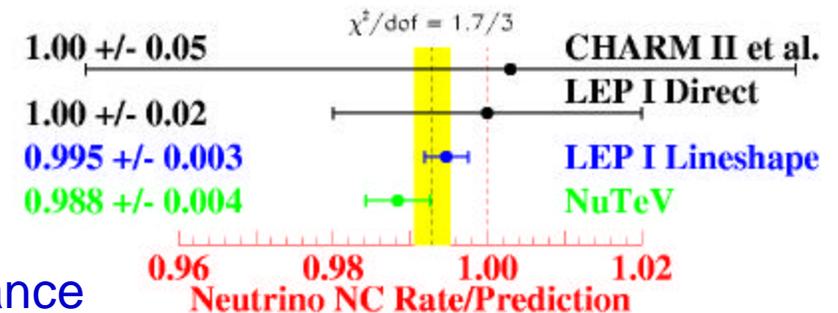
$$g_L^2 = 0.3005 \pm 0.0014$$

(SM : 0.3042) $\Leftarrow 2.6\sigma$ difference

$$g_R^2 = 0.0310 \pm 0.0011$$

(SM : 0.0301) \Leftarrow agreement

Discrepancy is left-handed coupling to u and d quarks

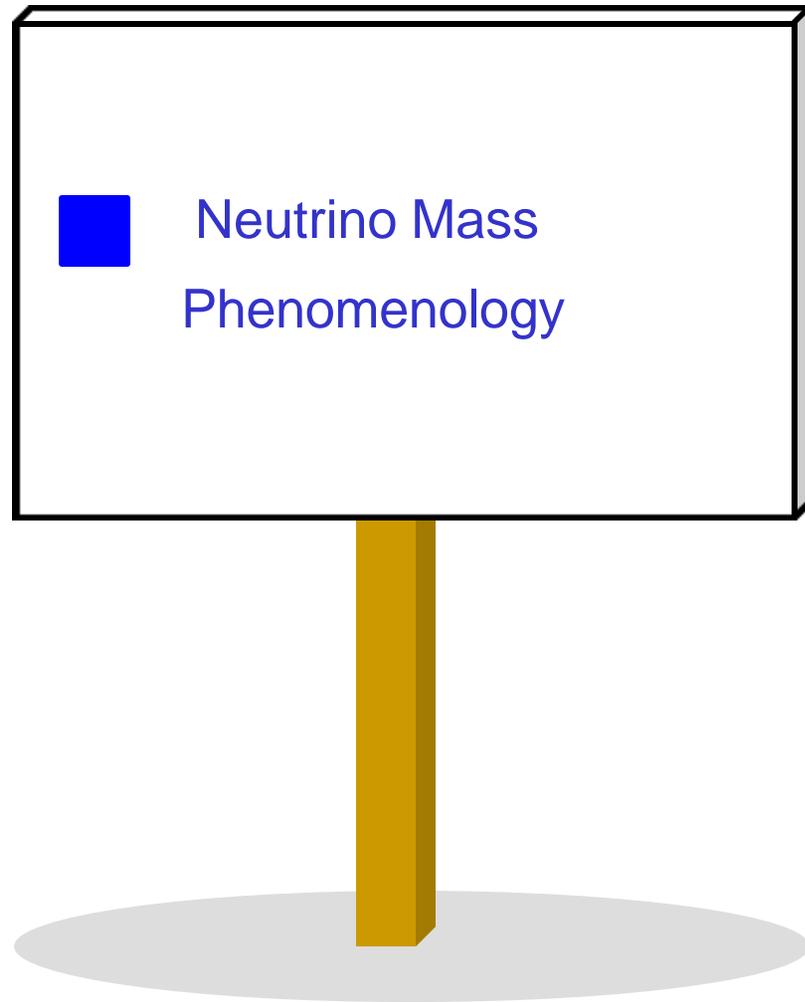


Neutrino Properties

- Neutrino Mass Phenomenology
- Direct Neutrino Mass Experiments
- Double Beta Decay Experiments
- Neutrino Oscillations

Bottom Line:

- *No Direct evidence of neutrino mass*
 - *Neutrinos almost certainly oscillate from one flavor to another*
- P** Neutrinos have mass and mix*



Neutrino Mass: Theoretical Ideas

- No fundamental reason why neutrinos must be massless
 - But why are they much lighter than other particles?

➤ Grand Unified Theories

- Dirac and Majorana Mass
 - ⇒ See-saw Mechanism

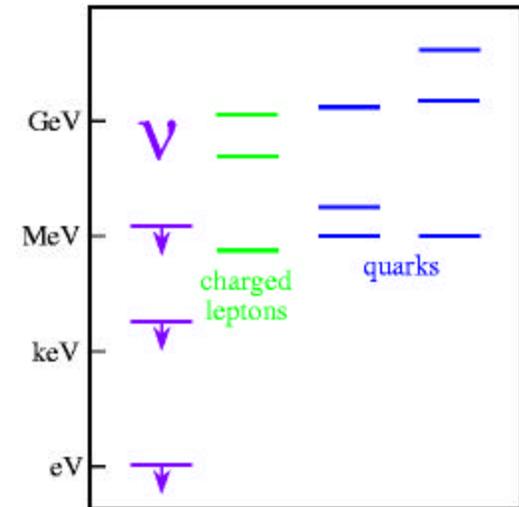
➤ Modified Higgs sector to accommodate neutrino mass

➤ Extra Dimensions

- Neutrinos live outside of 3 + 1 space

Many of these models have at least one Electroweak isosinglet ν

- Right-handed partner of the left-handed ν
- Mass uncertain from light (< 1 eV) to heavy ($> 10^{16}$ eV)
- Would be “sterile” – Doesn’t couple to standard W and Z bosons



Dirac and Majorana Neutrinos

- Dirac Neutrinos

- Neutrino and Antineutrino are distinct particles
- Lepton number conserved
 - Neutrino $\rightarrow \mu^-$
 - Antineutrino $\rightarrow \mu^+$
- Dirac Mass Term

$$-m_D (\bar{\nu}_L \nu_R + \bar{\nu}_R \nu_L)$$

- Majorana Neutrinos

- Neutrinos and Antineutrinos are the same particle
 - \Rightarrow Only difference is “handedness”
 - Neutrinos are left-handed $\nu \rightarrow \mu^-$
 - Antineutrinos are right-handed $\bar{\nu} \rightarrow \mu^+$
- Lepton number not conserved
 - Neutrino \Leftrightarrow Antineutrino with spin flip
- Majorana Mass Term

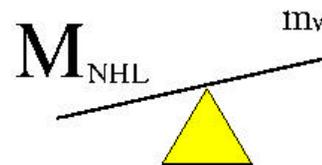
$$-\frac{1}{2} m_M^L (\bar{\nu}_L (\nu_L)^c + \overline{(\nu_L)^c} \nu_L) - \frac{1}{2} m_M^R (\bar{\nu}_R (\nu_R)^c + \overline{(\nu_R)^c} \nu_R)$$

See-Saw Mechanism with Both Majorana and Dirac Terms:

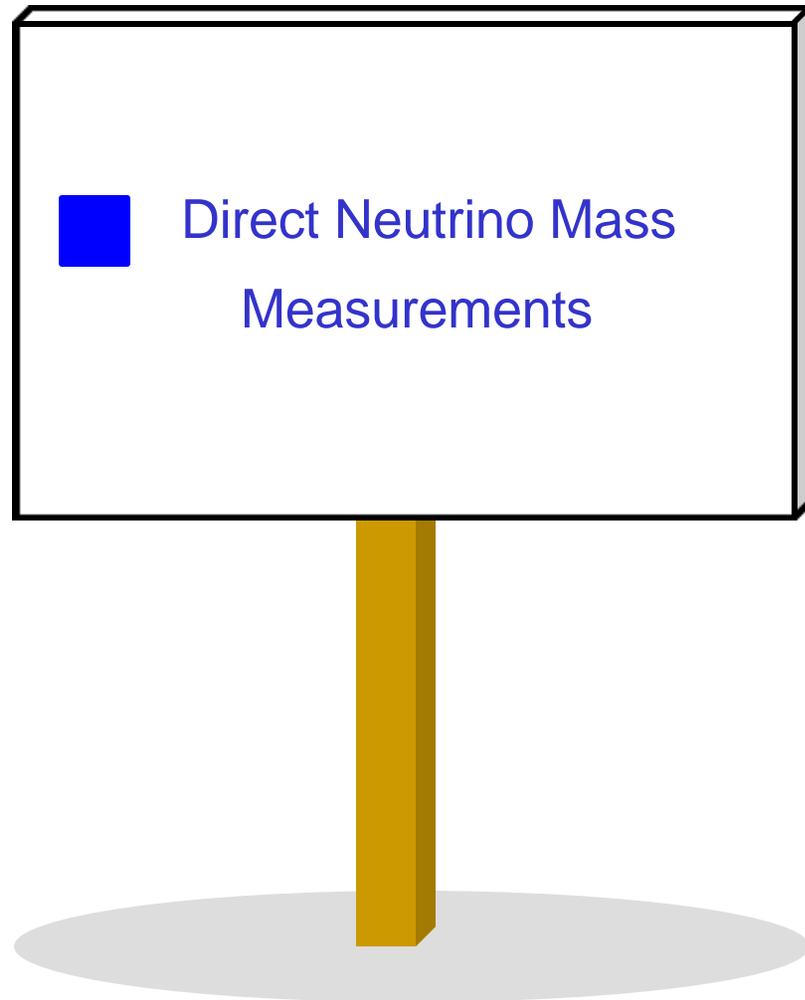
$$\mathcal{L}_{mass} = -\frac{1}{2} (\overline{\nu_L (\nu_R)^c}) \mathcal{M} \begin{pmatrix} (\nu_L)^c \\ \nu_R \end{pmatrix} + h.c.$$

$$\mathcal{M} = \begin{pmatrix} m_M^L & m_D \\ m_D & m_M^R \end{pmatrix}$$

$$m_M^R = M \gg m_D \gg m_M^L = \mu$$



$$m_N \approx M, \quad m_\nu \approx \left| \mu - \frac{m_D^2}{M} \right|$$



Direct Neutrino Mass Experiments

- Techniques

- Electron neutrino:

- Study E_e end point for ${}^3\text{H} \rightarrow {}^3\text{He} + \nu_e + e^-$

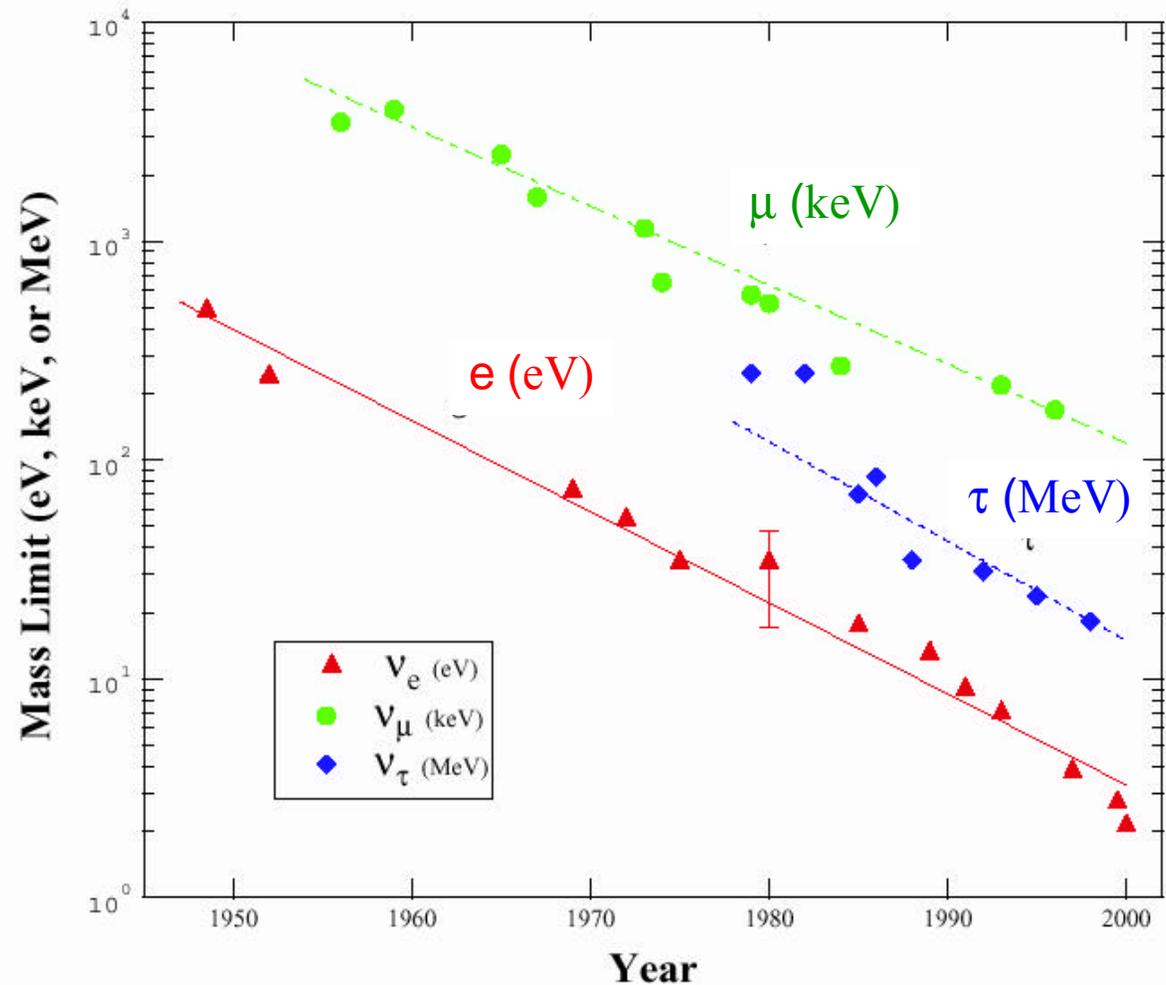
- Muon neutrino:

- Measure P_μ in $\pi \rightarrow \mu \nu_\mu$ decays

- Tau neutrino:

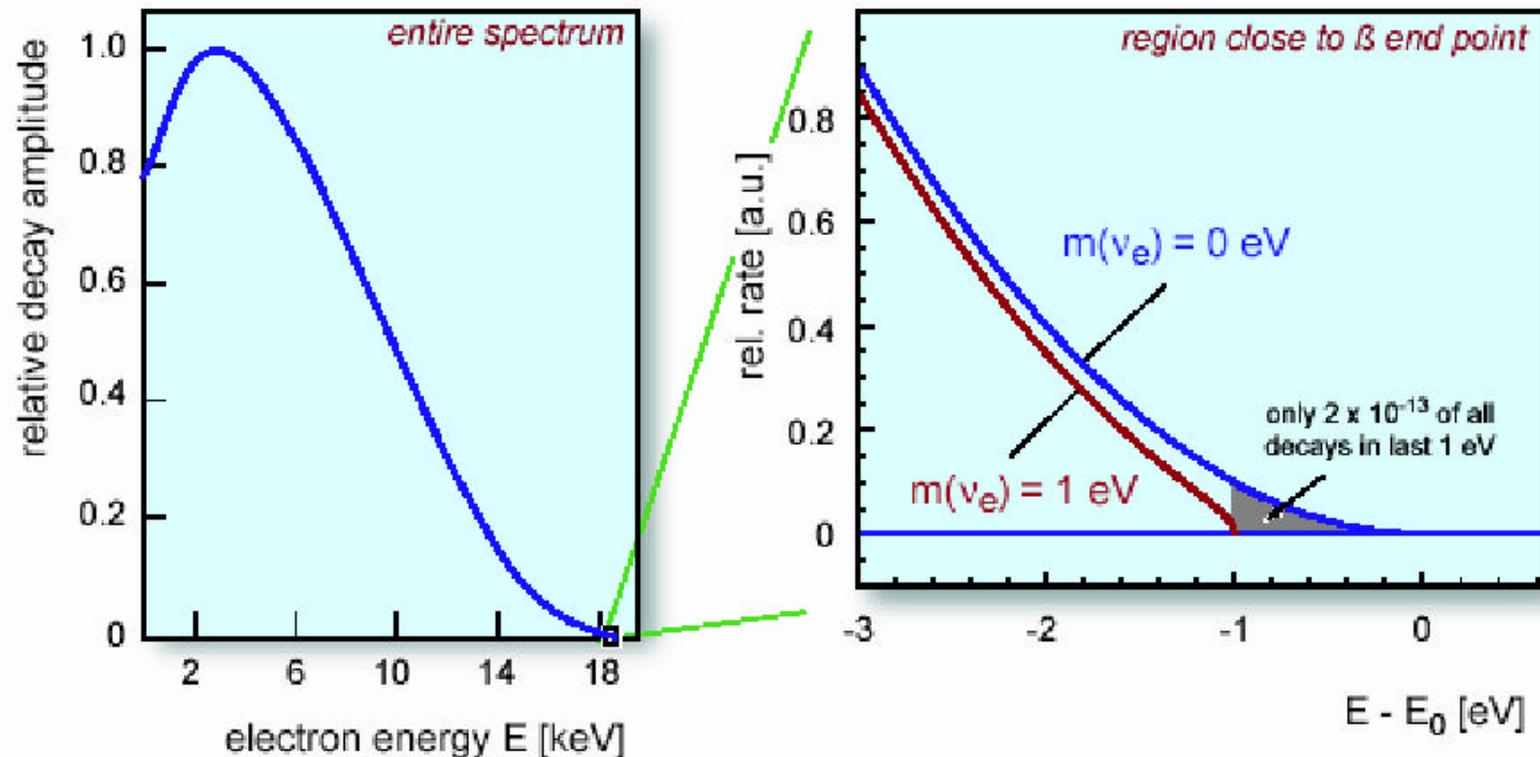
- Study $n\pi$ mass in $\tau \rightarrow (n\pi) \nu_\tau$ decays

(Also, information from Supernova time-of-flight)



n_e Mass Measurements (Tritium β -decay Searches)

- Search for a distortion in the shape of the β -decay spectrum in the end-point region.



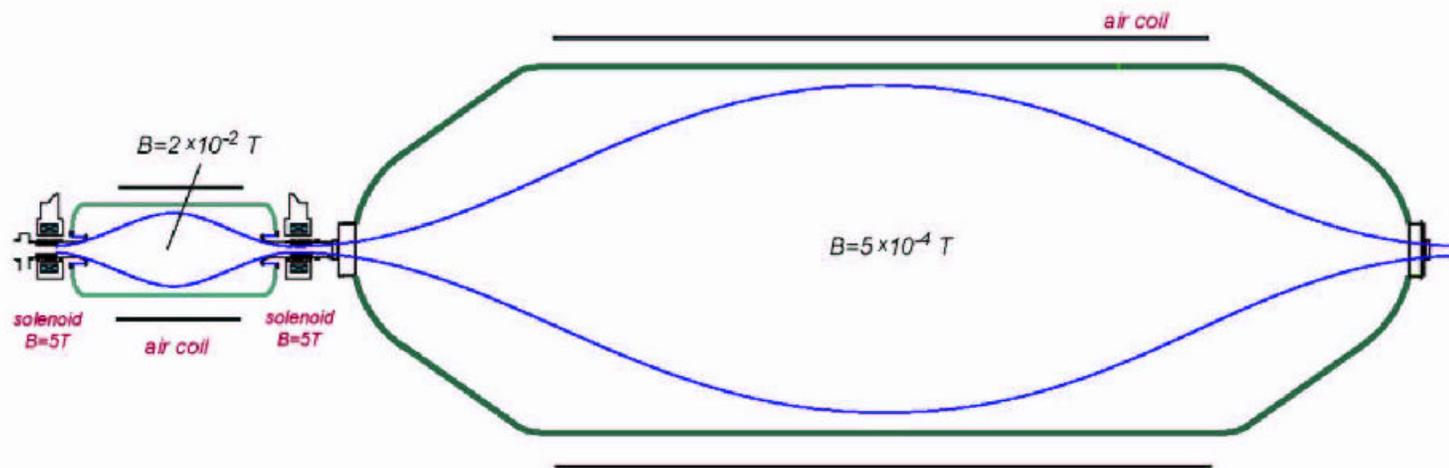
$$dN(E) = K|M|^2 F(Z,R,E) p_e E (E_0 - E) \left\{ (E_0 - E)^2 - m_{\nu_e}^2 c^4 \right\}^{1/2} dE$$

Next Generation b-decay Experiment ($\Delta m \gg 0.35$ eV)

Karlsruhe Tritium Neutrino Experiment (KATRIN)

next-generation experiment with *sub-eV* neutrino mass sensitivity

FH Fulda - FZ & U Karlsruhe - U Mainz - INP Prague - U Seattle - INR Troitsk



pre-spectrometer

fixed retarding potential 18.4 kV

$\varnothing = 1.7\text{ m} / L = 4.0\text{ m}$

$\Delta E = 80\text{ eV}$

main spectrometer

variable retarding potential 18.5-18.6 kV

$\varnothing = 7\text{ m} / L = 20\text{ m}$

$\Delta E = 1\text{ eV}$

Muon Neutrino Mass Studies

- Current best limit from studies of the kinematics of $\pi \rightarrow \mu \nu$ decay

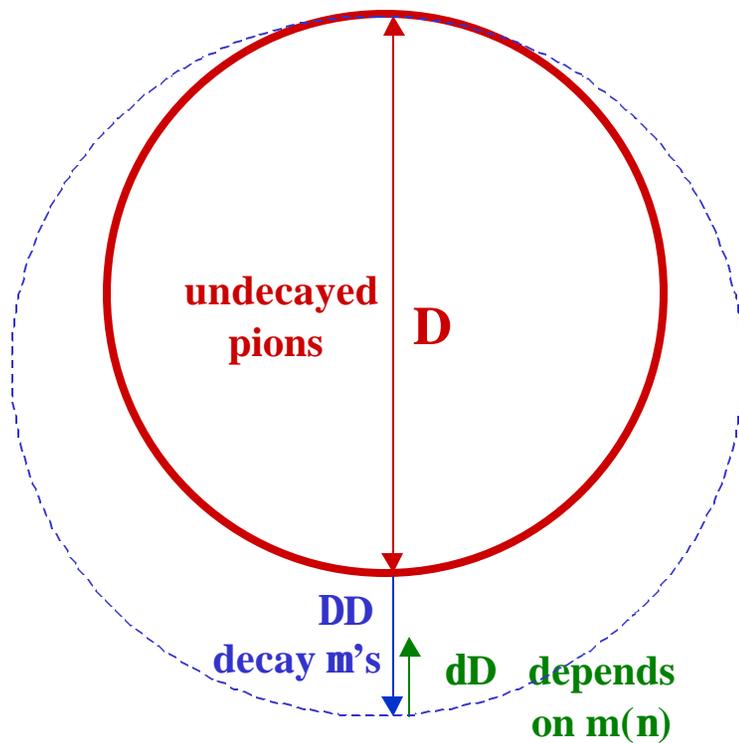
$$p_m^2 + m_m^2 = (m_p^2 + m_m^2 - m_n^2)^2 / 4m_p^2$$

- Can use π -decay:
 - **At Rest:**
Mass of π is dominate uncertainty
 - **In Flight:**
Resolution on p_π - p_μ limited experimentally
- Best mass limit is from π -decay at rest
< 170 keV at 95% CL
(Assamagan *et al.*, PRD 1996)
- New BNL Experiment using $g-2$ setup (sensitivity for > 8 keV)

Proposed BNL “NuMass” Experiment

BNL g-2 Neutrino Mass Experiment

$$m(\nu_\mu) < 8 \text{ keV}/c^2$$



Forward-going decay muons orbit a larger diameter by DD

CM

$$\mathbf{n}_m \longleftarrow \mathbf{p} \longrightarrow \mathbf{m}$$

$$q = 29.7 \text{ MeV}/c$$

$$\frac{DD}{D} = \frac{p_m - p_p}{p_p} = \frac{0.7 \text{ MeV}/c}{3 \text{ GeV}/c} = \frac{3.26 \text{ mm}}{14 \text{ m}}$$

non-zero m_n shrinks DD

$$\frac{dD}{D} = \frac{-m_n^2}{2 q m_p}$$

0.04 mm for current limit

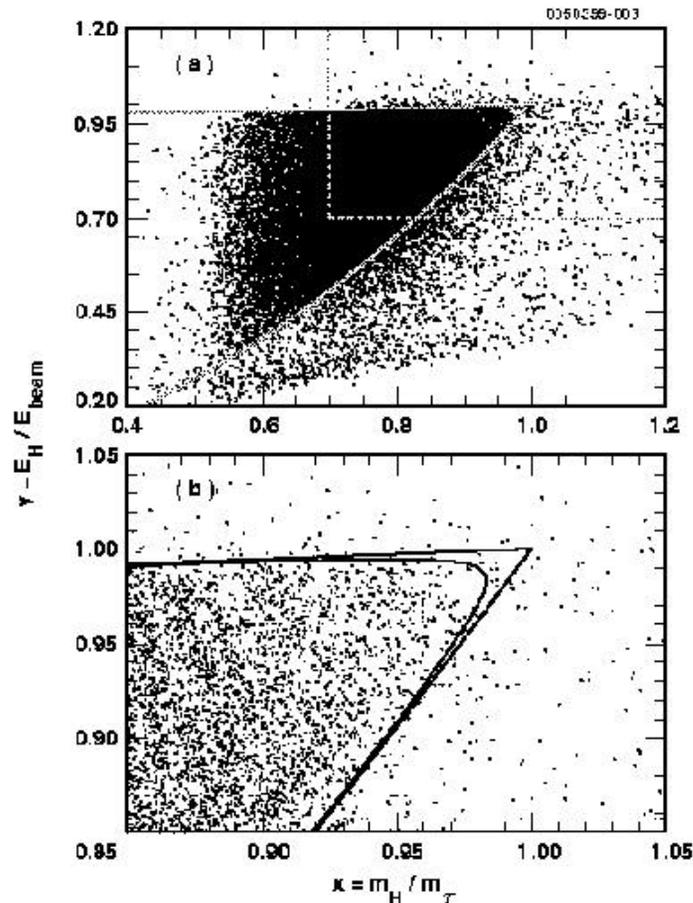
Direct ν_τ Mass Limits

- Look at tau decays near the edge of the allowed kinematic range

$$\tau^- \rightarrow 2\pi^- \pi^+ \nu_\tau \quad \text{and}$$

$$\tau^- \rightarrow 3\pi^- 2\pi^+ (\pi^0) \nu_\tau$$

- Fit to scaled visible energy vs. scaled invariant mass (e.g. hep-ex/9906015, CLEO)
- Best limit is $m(\nu_\tau) < 18.2 \text{ MeV}$ at 95% CL (Aleph, EPJ C2 395 1998)



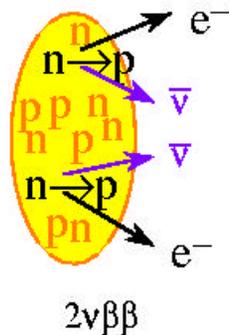
massive ν_τ
shifts the edge
of the distribution

(Outer lines, mass=0;
inner lines, mass=30 MeV)

Double Beta Decay: Are Neutrinos Majorana Particles?

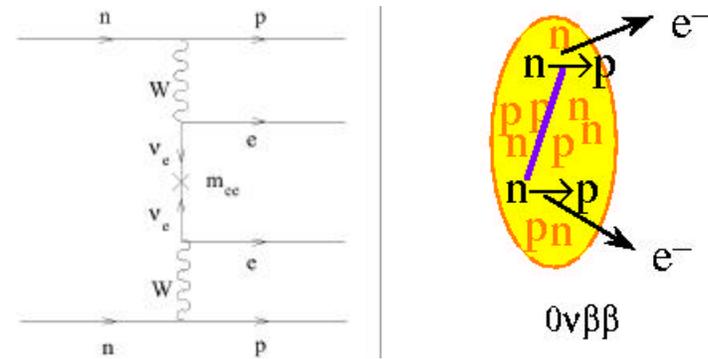
2νββ Decay

- Double-beta decay is transition:
 $(Z,A) \rightarrow (Z+2,A) + (e^- e^- \bar{\nu}_e \nu_e)$
Double weak transition $\propto G_F^4$
- In certain nuclei, single β -decay is energetically not allowed
($^{136}\text{Xe} \rightarrow ^{136}\text{Ba}$, $^{76}\text{Ge} \rightarrow ^{76}\text{Se}$, etc.)

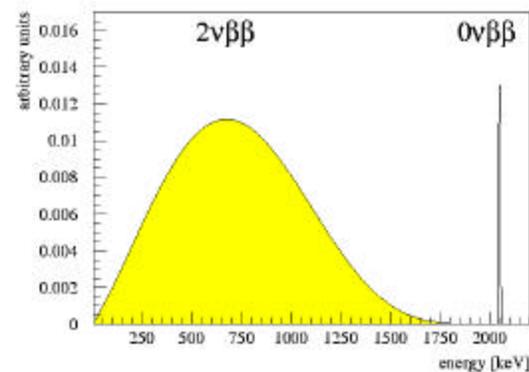


0νββ Decay

- If neutrinos are Majorana then can have 0ν transitions



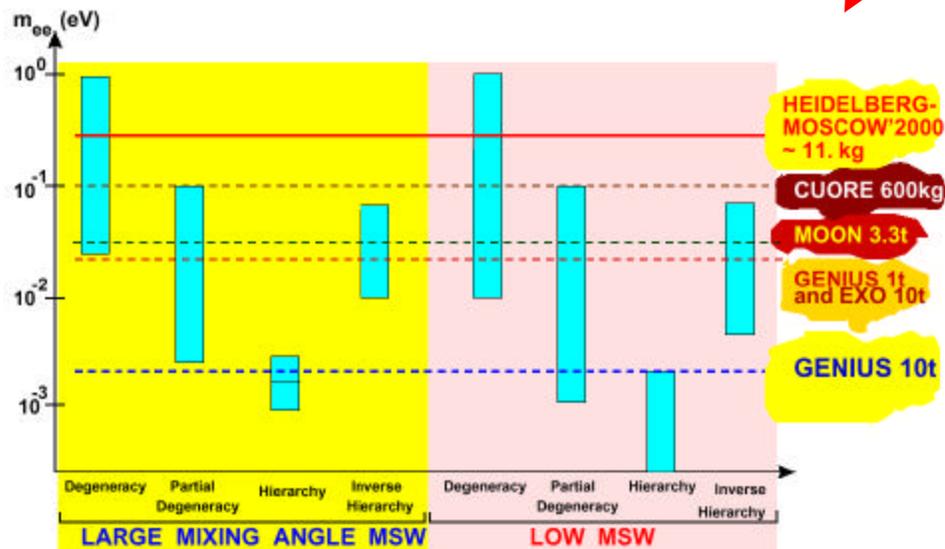
- Look for 0ν signal beyond the 2ν end point



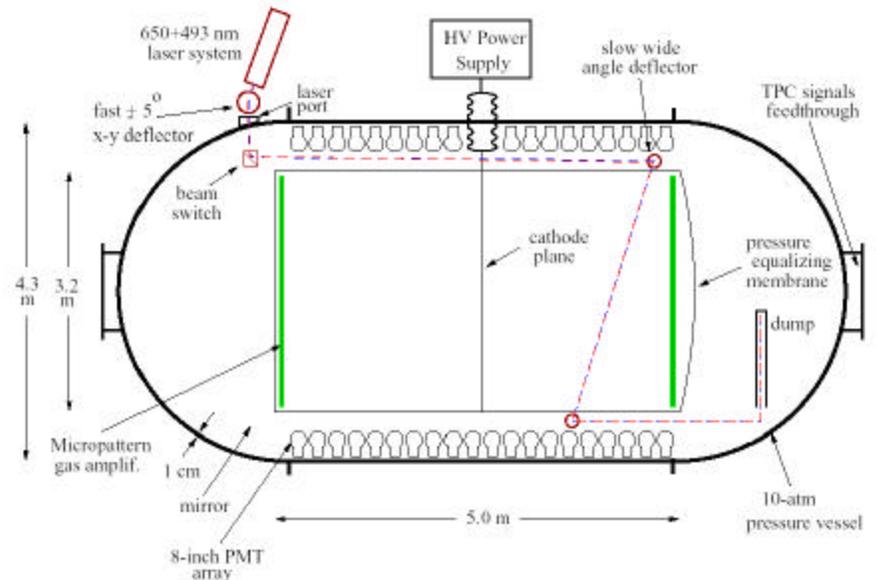
Determine
neutrino mass
from rate which
 $\propto (m_\nu/m_e)^2$

Double Beta Decay Neutrino Mass Searches

- Current best limit comes from Heidelberg-Moscow Experiment using ^{76}Ge
 $m_\nu < 0.2 \text{ eV}$

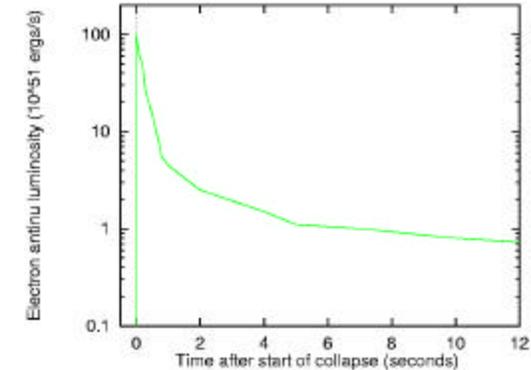


- Proposed next steps:
 - New ^{76}Ge experiments increase from kg to tons! (GENIUS,) $\sim \text{few} \times 10^{-3} \text{ eV}$
 - New TPC technique $^{136}\text{Xe} \rightarrow ^{136}\text{Ba}$
 Track both e^-e^- and Ba atom!
 EXO Experiment $\sim 0.01 \text{ eV}$



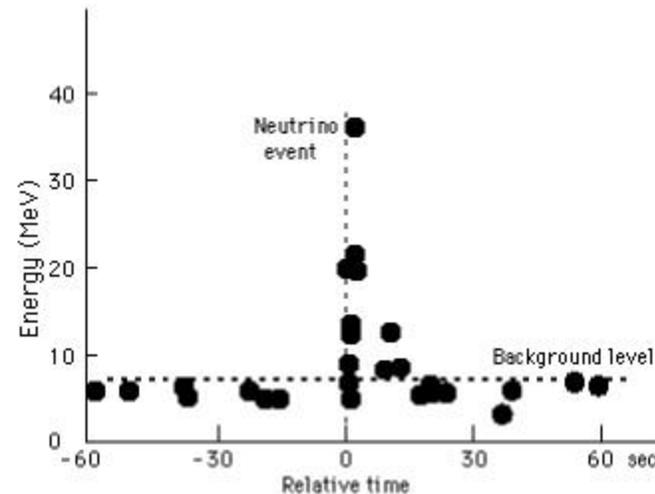
Supernova Neutrinos

- In a super nova explosion
 - Neutrinos escape before the photons
 - Neutrinos carry away ~99% of the energy
 - The rate of escape for ν_e is different from ν_μ and ν_τ (Due extra ν_e CC interactions with electrons)



- Neutrino mass limit can be obtained by the spread in the propagation time

- $t_{\text{obs}} - t_{\text{emit}} = t_0 (1 + m^2/2E^2)$
- Spread in arrival times if $m \neq 0$ due to ΔE
- For SN1987a assuming emission time is over 4 sec
 $m_\nu < \sim 30 \text{ eV}$



(All arrived within about ~13 s after traveling 180,000 light years with energies that differed by up to a factor of three. The neutrinos arrived about 18 hours before the light was seen)

SNEWS

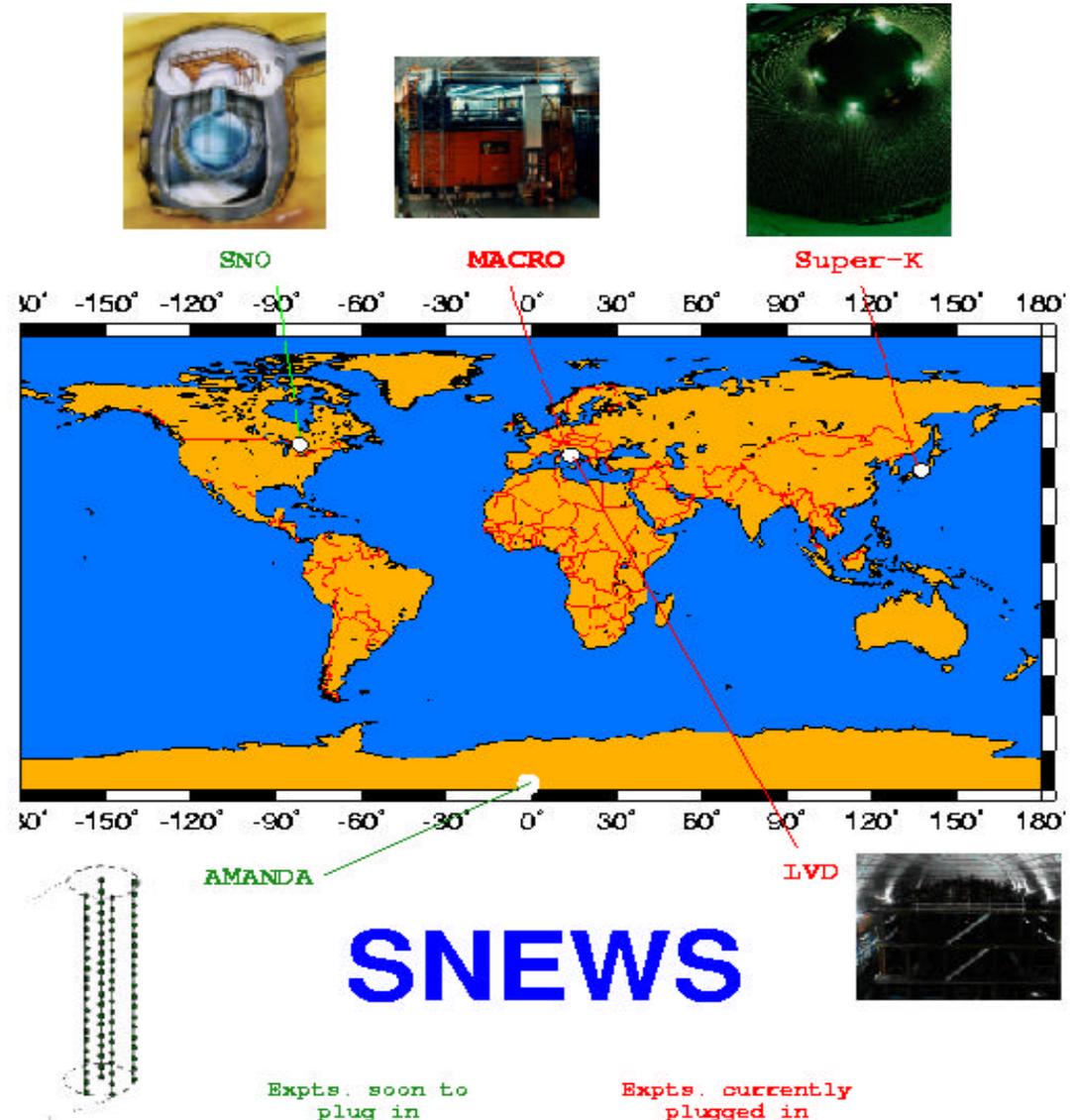
The SuperNova Early Warning System

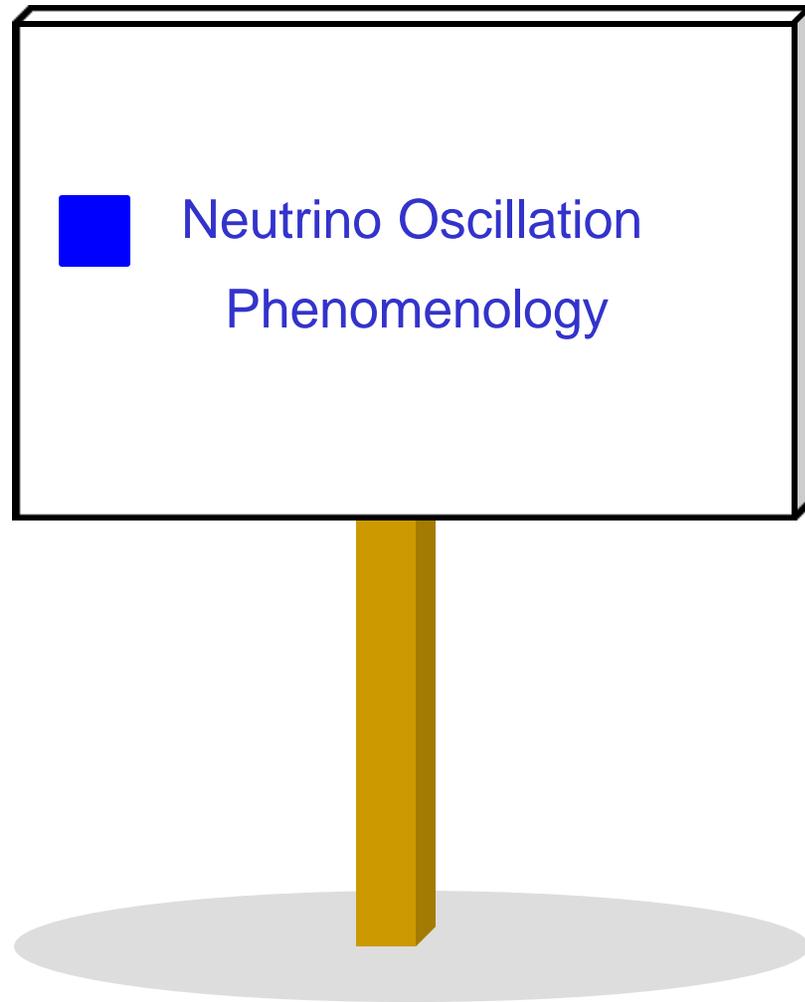
SNEWS –

- Coincidence trigger between world's ν observatories eliminates instrumental false alarms
- Confidence in such an automated signal allows for **FAST** enough alarm to beat the photons
- Running in test mode for $\gtrsim 1$ year, will release automated alarms sometime in 2000

What is to be gained from an early warning?

- UV/soft X-ray flash at shock breakout predicted.
- Environment near progenitor star is probed by the initial stages of the collapse.
- **Possible unknown early effects.** Who knows what we're missing when observing SN at Mpc distances starting days after the explosion?





Neutrino Oscillations

- Direct measurements have difficulty probing small neutrino masses

⇒ *Use neutrino oscillations*

- If we postulate:
 - Neutrinos have (different) mass
 - The *Weak Eigenstates* are a mixture of *Mass Eigenstates*

$$\begin{pmatrix} \nu_e \\ \nu_\mu \end{pmatrix} = \begin{pmatrix} \cos \theta & \sin \theta \\ -\sin \theta & \cos \theta \end{pmatrix} \begin{pmatrix} \nu_1 \\ \nu_2 \end{pmatrix}$$

Then a pure ν_μ beam at $t=0$, will develop a ν_e component with time.

The Probability for Oscillations...

$$P_{osc} = \sin^2 2\theta \sin^2(1.27\Delta m^2 L/E)$$

Derivation of Oscillation Formula

(A favorite graduate exam problem)

Take the mixing matrix to be:

$$\begin{pmatrix} \nu_e \\ \nu_\mu \end{pmatrix} = \begin{pmatrix} \cos \theta & \sin \theta \\ -\sin \theta & \cos \theta \end{pmatrix} \begin{pmatrix} \nu_1 \\ \nu_2 \end{pmatrix}$$

At production ($t = 0$):

$$|\nu_\mu(0)\rangle = -\sin \theta |\nu_1\rangle + \cos \theta |\nu_2\rangle$$

At a later time:

$$\begin{aligned} |\psi(t)\rangle &= -\sin \theta e^{-iE_1 t} |\nu_1\rangle + \cos \theta e^{-iE_2 t} |\nu_2\rangle \\ &= (\cos^2 \theta e^{-iE_1 t} + \sin^2 \theta e^{-iE_2 t}) |\nu_e\rangle + \\ &\quad \sin \theta \cos \theta (e^{-iE_2 t} - e^{-iE_1 t}) |\nu_\mu\rangle \end{aligned}$$

And the probability is:

$$\begin{aligned} P_{osc} &= |\langle \nu_e | \psi(t) \rangle|^2 \\ &= \frac{1}{2} \sin^2 2\theta [1 - \cos(E_2 - E_1)t] \end{aligned}$$

Use $E_1 = \sqrt{p^2 - m_1^2} \approx p + m_1^2/2p$ (and same for E_2)
and $(t/p) = (tc)/(pc) = L/E$; then convert to "real" units

$$\begin{aligned} P_{osc} &\approx \frac{1}{2} \sin^2 2\theta \left(1 - \cos \left(\frac{(m_2^2 - m_1^2)L}{E} \right) \right) \\ &= \sin^2 2\theta \sin^2(1.27 \Delta m^2 L/E) \end{aligned}$$

See if you can derive the 1.27 factor in the formula by recovering from the $\hbar = c = 1$.

Neutrino Oscillation Formalism

- Most analyses assume 2-generation mixing

$$\begin{pmatrix} \mathbf{n}_e \\ \mathbf{n}_m \end{pmatrix} = \begin{pmatrix} \cos q & \sin q \\ -\sin q & \cos q \end{pmatrix} \begin{pmatrix} \mathbf{n}_1 \\ \mathbf{n}_e \end{pmatrix} \quad P(\mathbf{n}_m \rightarrow \mathbf{n}_e) = \sin^2 2q \sin^2(1.27 \Delta m^2 L / E)$$

- But we have 3-generations: ν_e , ν_μ , and ν_τ (and maybe even more the sterile neutrino ν_s 's)

$$\begin{pmatrix} \mathbf{n}_e \\ \mathbf{n}_m \\ \mathbf{n}_t \end{pmatrix} = \begin{pmatrix} c_{12}c_{13} & s_{12}c_{13} & s_{13}e^{-id} \\ -s_{12}c_{23} - c_{12}s_{23}s_{13} & c_{12}c_{23} - s_{12}s_{23}s_{13}e^{id} & s_{23}c_{13} \\ s_{12}s_{23} - c_{12}c_{23}s_{13}e^{id} & -c_{12}s_{23} - s_{12}c_{23}s_{13}e^{id} & c_{23}c_{13} \end{pmatrix} \begin{pmatrix} \mathbf{n}_1 \\ \mathbf{n}_2 \\ \mathbf{n}_3 \end{pmatrix} \leftarrow \begin{array}{l} \text{CKM-like} \\ \text{Mixing Matrix} \\ \text{for Leptons} \end{array}$$

(In this 3-generation model, there are 3 Δm^2 's but only two are independent.) $\Delta m_{12}^2 = m_1^2 - m_2^2$, $\Delta m_{23}^2 = m_2^2 - m_3^2$, $\Delta m_{31}^2 = m_3^2 - m_1^2$

- At each Δm^2 , there can be oscillations between all the neutrino flavors with different mixing angle combinations.

For example: (3 sets of 3 equations like these)

$$\begin{aligned} P(\mathbf{n}_m \rightarrow \mathbf{n}_t) &= \cos^4 q_{13} \sin^2 2q_{23} \sin^2(1.27 \Delta m_{32}^2 L / E_n) \\ P(\mathbf{n}_m \rightarrow \mathbf{n}_e) &= \sin^2 q_{23} \sin^2 2q_{13} \sin^2(1.27 \Delta m_{32}^2 L / E_n) \\ P(\mathbf{n}_e \rightarrow \mathbf{n}_t) &= \cos^2 q_{23} \sin^2 2q_{13} \sin^2(1.27 \Delta m_{32}^2 L / E_n) \end{aligned}$$

$\nu_\mu \rightarrow \nu_e$ at the same Δm^2 as $\nu_\mu \rightarrow \nu_\tau$

CP Violation in Neutrino Oscillations

- Disappearance measurements cannot see CP violation effect

$$P(\mathbf{n}_m \rightarrow \mathbf{n}_m) = P(\bar{\mathbf{n}}_m \rightarrow \bar{\mathbf{n}}_m)$$

- Very, very hard to see CP violation effects in exclusive (appearance) measurements. (From B. Kayser)
 - Only can see CP violation effects if an experiment is sensitive to oscillations involving at least three types of neutrinos.

$$P(\mathbf{n}_m \rightarrow \mathbf{n}_e) - P(\bar{\mathbf{n}}_m \rightarrow \bar{\mathbf{n}}_e) = 4 \operatorname{Im}(U_{m1} U_{e1}^* U_{m3}^* U_{e3}) (s_{12} + s_{23} + s_{31})$$

$$\text{where } s_{ij} = \sin(\mathbf{d}m_{ij}^2 L/2E) \text{ and } \mathbf{d}m_{ij}^2 = m_i^2 - m_j^2$$

- All the terms (s_{12} , s_{13} , s_{23}) must not be $\ll 1$ or effectively becomes only two component oscillation
 - For example, if $s_{31} \approx 0$ then $s_{12} \approx -s_{23} \Rightarrow s_{12} + s_{31} + s_{23} \approx 0$

P To see CP violation must be sensitive to all three neutrino oscillations

i.e. the hardest is usually the lowest (solar neutrino)

$$\mathbf{D}m^2 \gg 10^{-4} - 10^{-10} \text{ eV}^2$$

Oscillation Formula Parameters

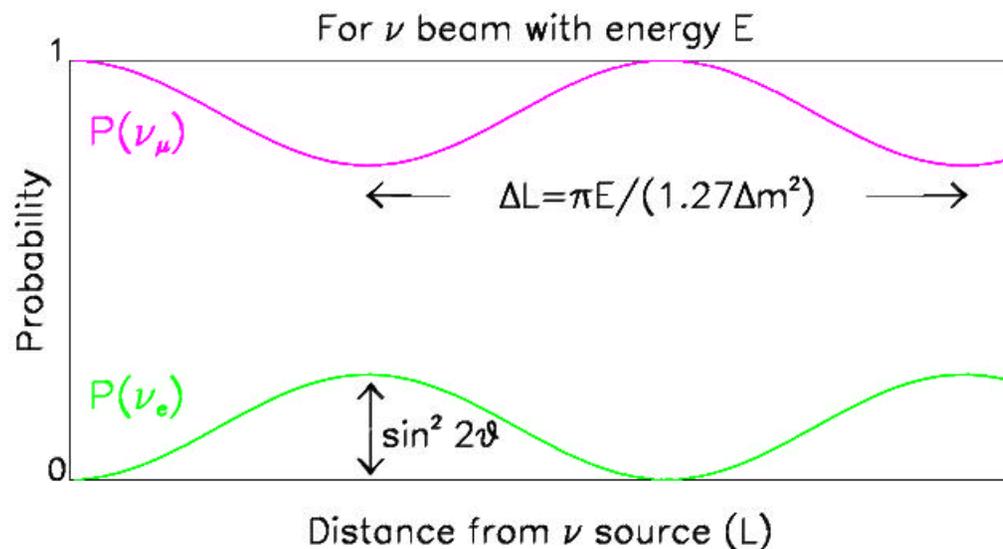
$$P_{Osc} = \sin^2 2\theta \sin^2(1.27\Delta m^2 L / E)$$

...Depends Upon Two Experimental Parameters:

- L – The distance from the ν source to detector (km)
- E – The energy of the neutrinos (GeV)

...And Two Fundamental Parameters:

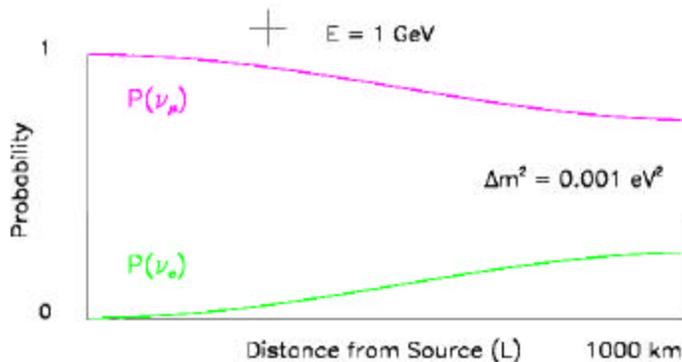
- $\Delta m^2 = m_1^2 - m_2^2$ (eV^2)
- $\sin^2 2\theta$



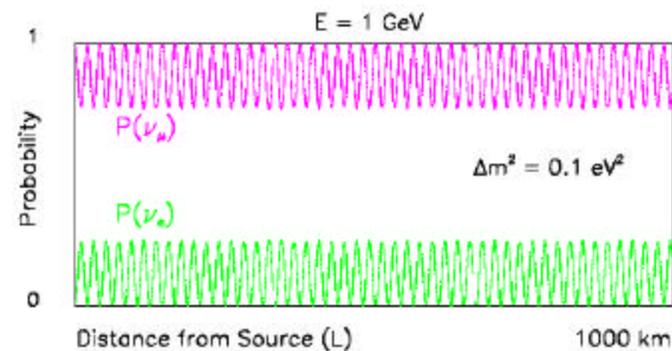
Oscillation Phenomenology

- Two types of oscillation searches:
 - *Appearance Experiment:*
 - Look for appearance of ν_e or ν_τ in a pure ν_μ beam vs. L and E
 - Need to know the backgrounds
 - *Disappearance Experiment:*
 - Look for a change in ν_μ flux as a function of L and E
 - Need to know the flux and cross sections
- $P_{\text{osc}} = \sin^2 2\theta \sin^2(1.27 \Delta m^2 L/E)$ sets the details of search
 - Mixing angle $\sin^2 2\theta$ sets the needed statistics

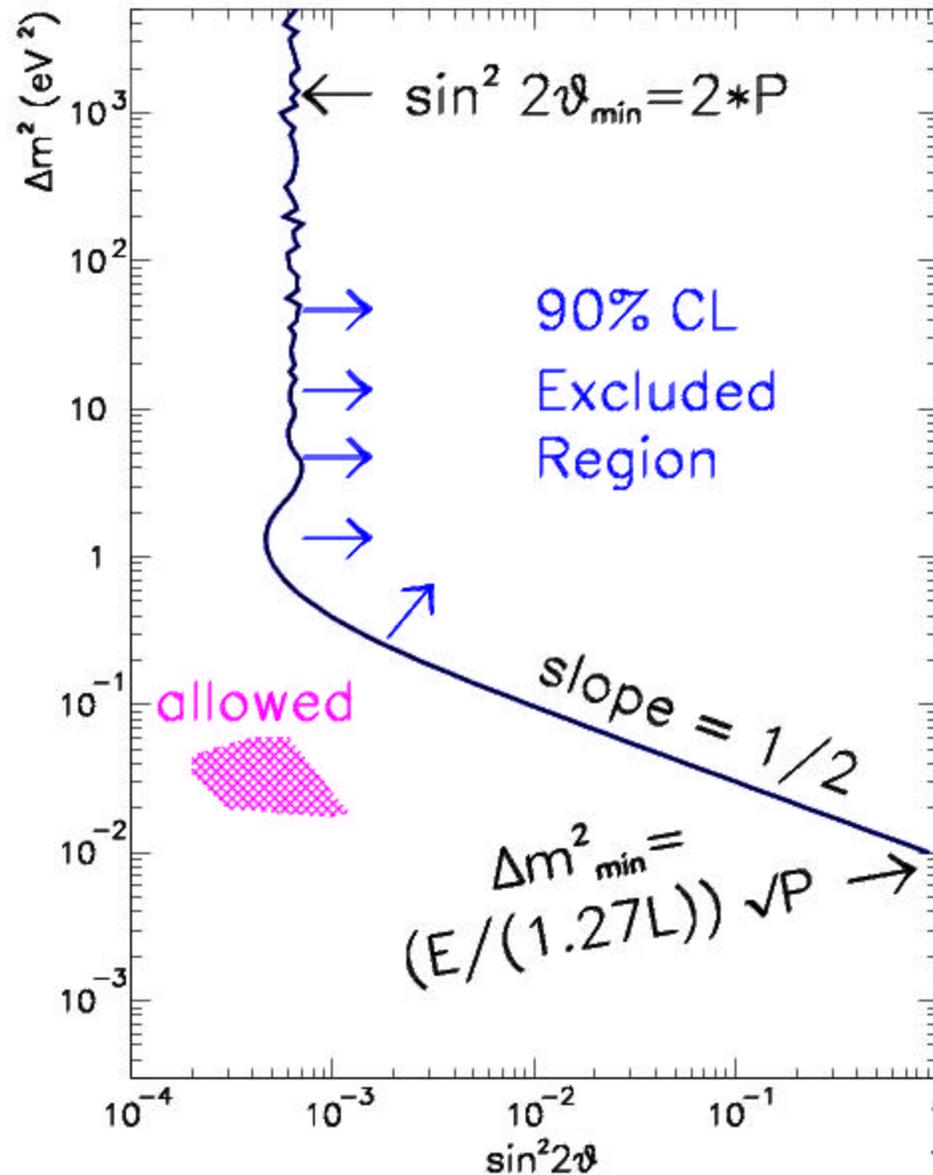
Small Δm^2 (Need large L/E)



Large Δm^2 : $\langle \sin^2(1.27 \Delta m^2 L/E) \rangle = 1/2$



Oscillation Plots



- If you see an oscillation signal with

$$P_{\text{osc}} = P \pm dP$$

then carve out an **allowed region** in $(\Delta m^2, \sin^2 2\theta)$ plane.

- If you see no signal and limit oscillation with

$$P_{\text{osc}} < P \text{ @ 90\% CL}$$

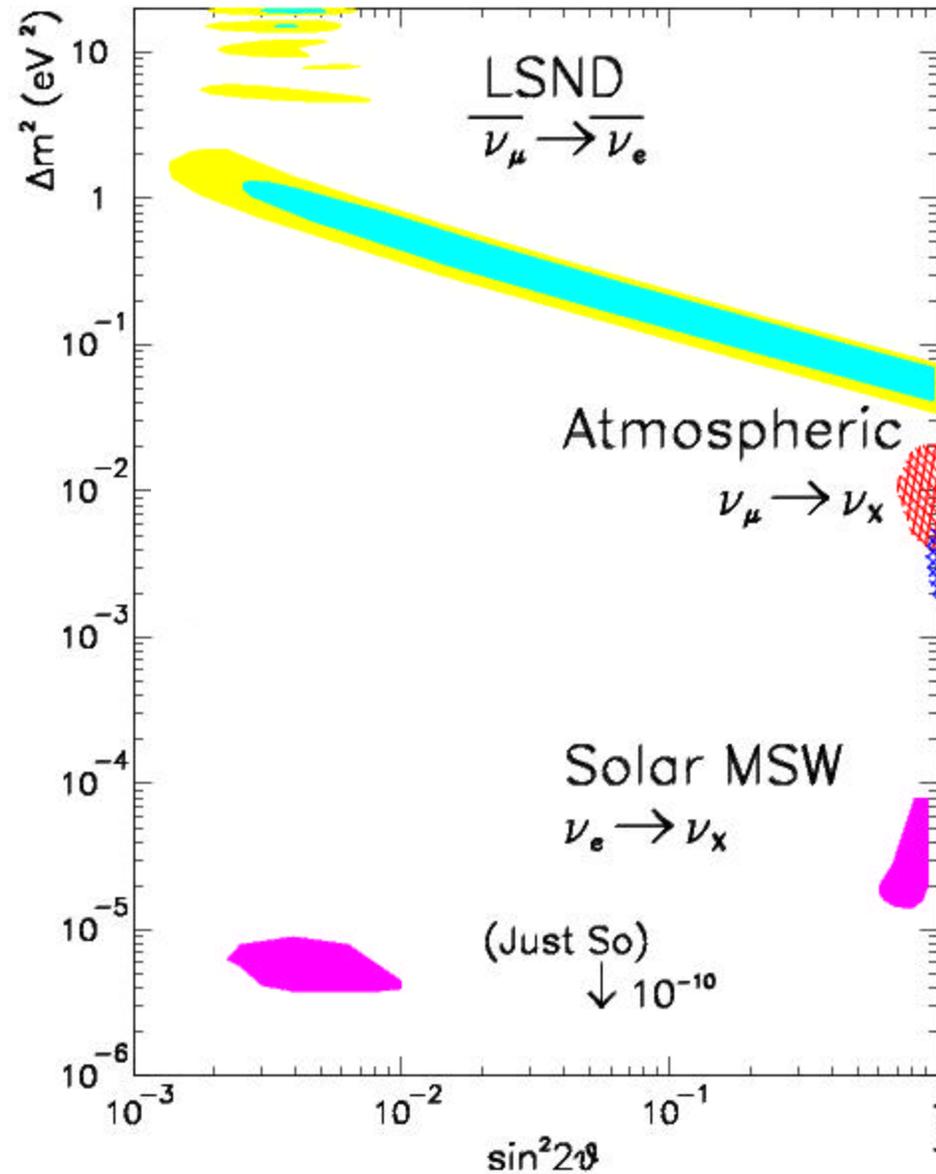
then carve out an **excluded region** in the $(\Delta m^2, \sin^2 2\theta)$ plane.

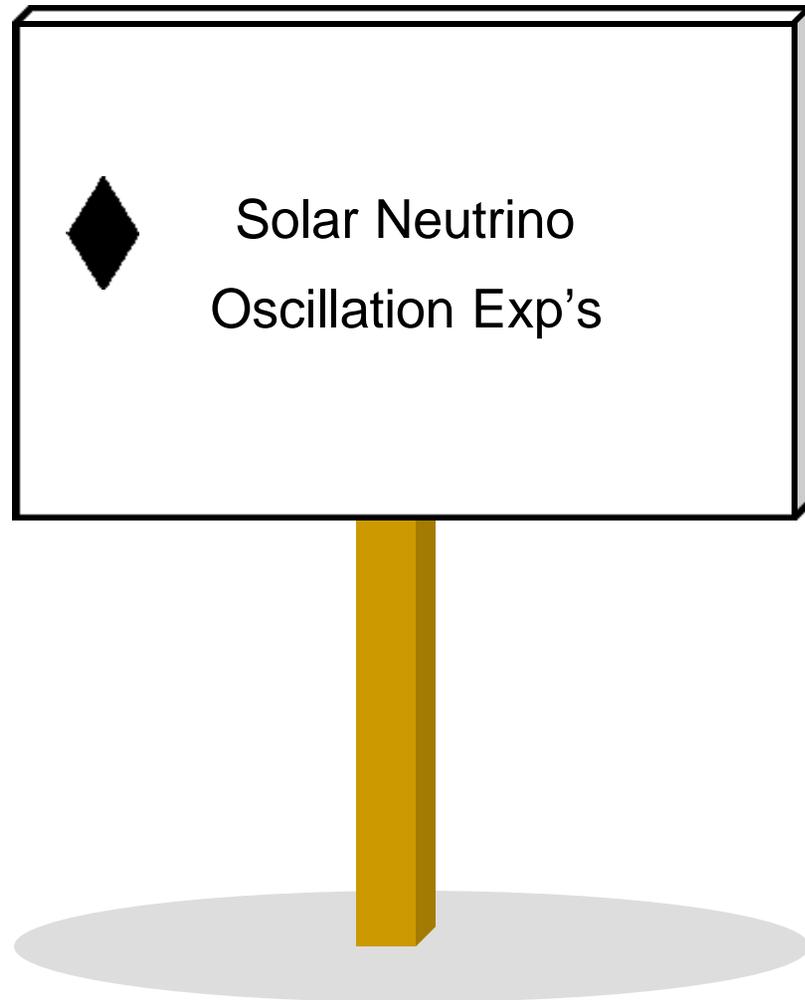
Current Neutrino Oscillation Signals

- Three Positive Signals
 - Solar Neutrinos
 - Atmospheric Neutrinos
 - Low-E Accelerator Neutrinos

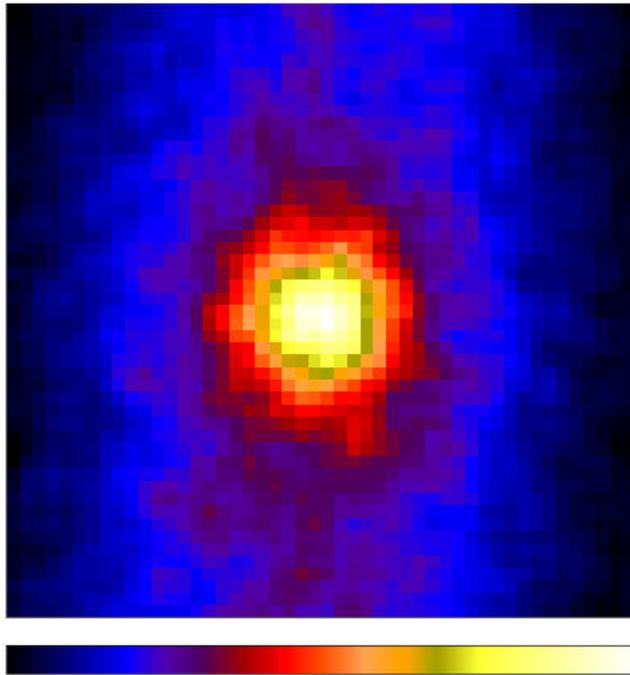
- Many negative searches

*Go thru results of each area
and try to fit things together*





Solar Neutrino Deficit



Super- K (Japan) image
of the sun using neutrinos

Flux of solar neutrinos detected at the earth is much less than expected

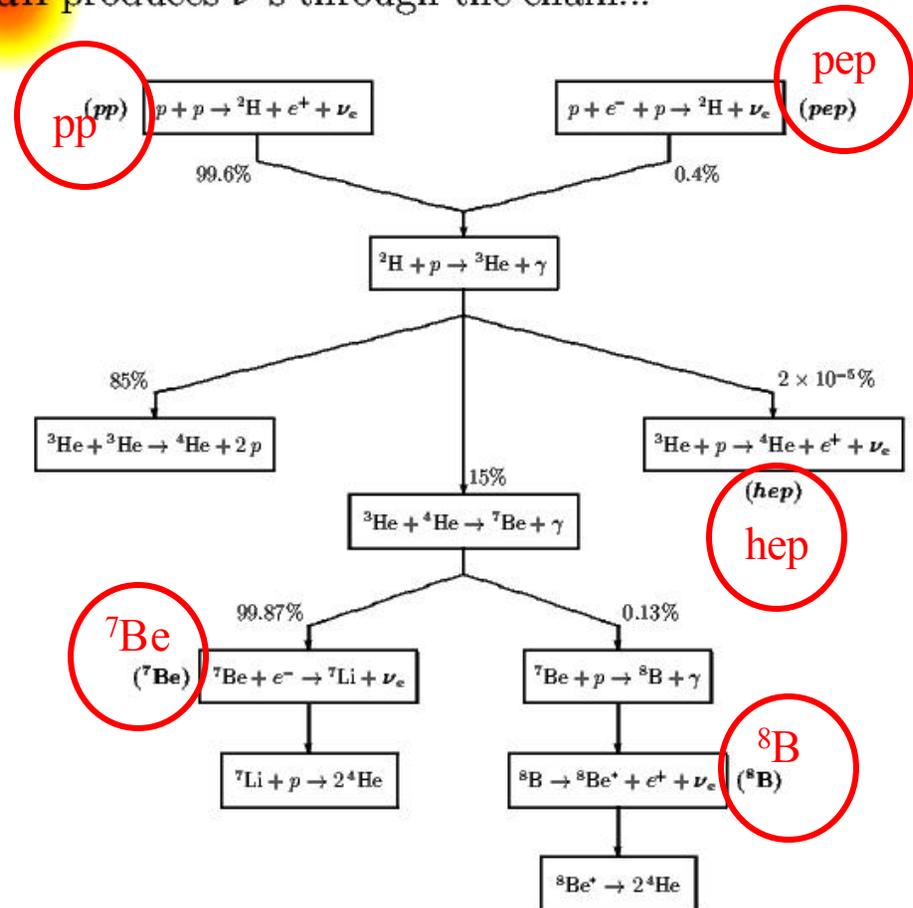
⇒ Is it due to neutrino oscillations?

- The “Standard Solar Model”
- Wide range of measurement techniques
- How does it fit into a oscillation hypothesis?
 - Several possible oscillation scenarios fit data
- Remaining questions and future plans

Standard Solar Model

- Stellar evolution models:
 - Hydrodynamic equilibrium between pressure and gravity
 - Energy transport by radiation and convection
 - Energy production by nuclear reactions
 - Can produce ν 's here
- Many experimental and theoretical inputs:
 - Age, luminosity, opacity, abundances, radius, surface temp, core temp, core density, diffusion parameters.
- Output:
 - Temp(r), density(r)
 - Neutrino Flux**

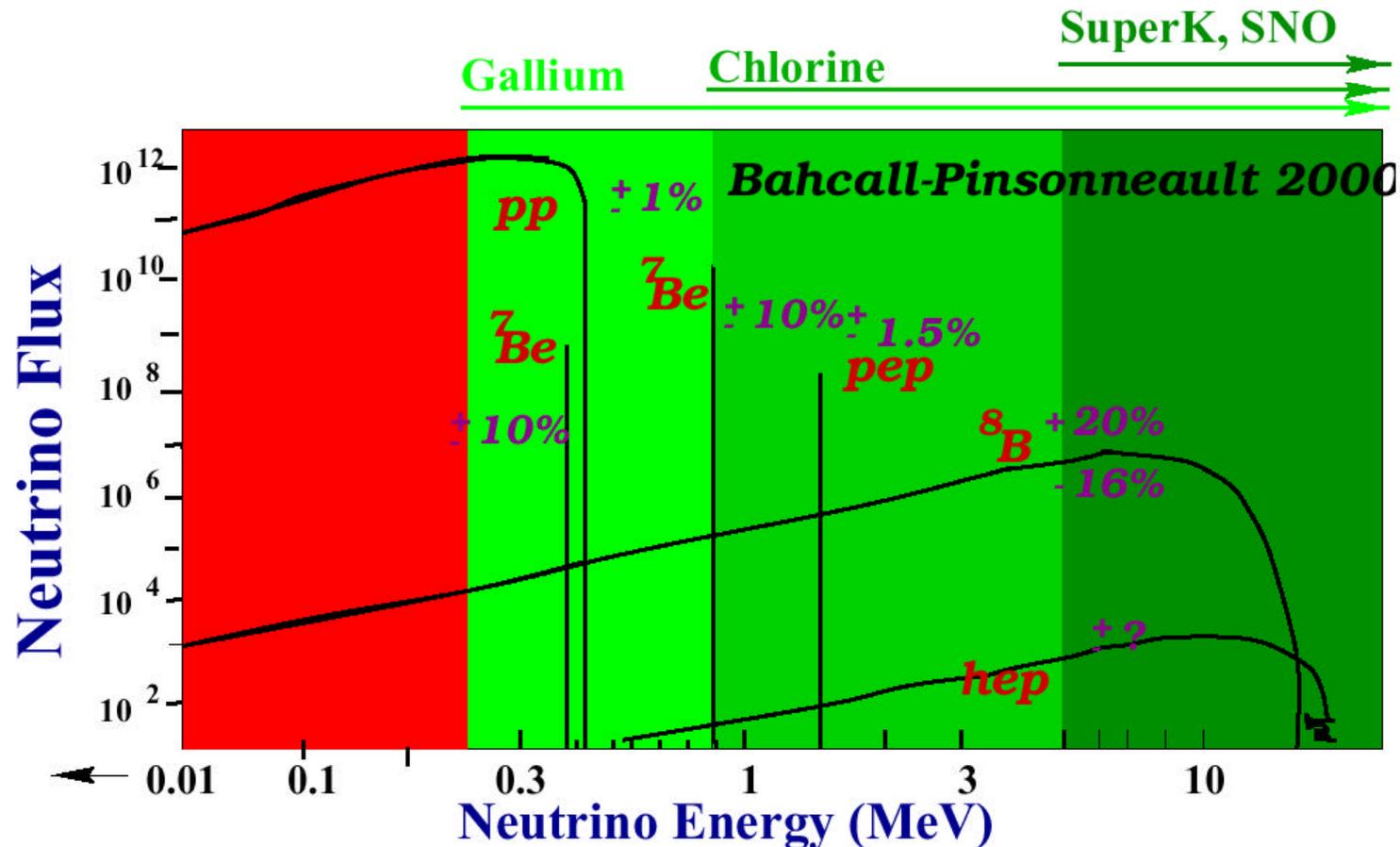
The sun produces ν 's through the chain...



But how big are the uncertainties

Solar Neutrino Spectrum

- Many fusion processes in the sun lead to neutrinos
- Solar model predicts flux
 - From solar luminosity, main pp neutrino flux known to 1%
 - ${}^7\text{Be}$ and ${}^8\text{B}$ neutrinos 10% to 20% uncertainties

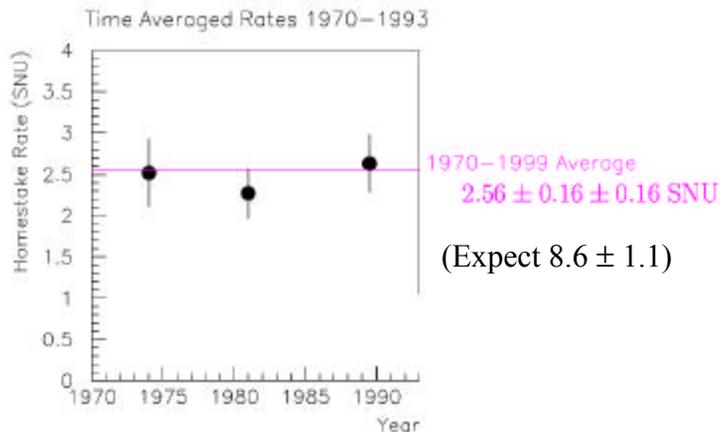


Solar Neutrino Experiments

- Solar neutrino cross sections
 - are very, very small
 - At these energies $\sigma_\nu \sim 10^{-45} \text{ cm}^2$
 - With flux of $10^{10}/\text{cm}^2/\text{s}$ and 10^{30} atoms \rightarrow 1 event / day
 - Introduce new unit *“The SNU”*
 - 1 SNU = 10^{-36} captures / target atom / s
- Two types of experiments:
 - Chemical Extraction experiments
 - Homestake (“Chlorine”) $\nu_e + {}^{37}\text{Cl} \rightarrow {}^{37}\text{Ar} + e^-$
 - Sage and Gallex (“Gallium”) $\nu_e + {}^{71}\text{Ga} \rightarrow {}^{71}\text{Ge} + e^-$
 - Scattering experiments
 - SuperKamioka (Kamioka)
(Light water) $\nu_x + e^- \rightarrow \nu_x + e^-$
 - SNO
(Heavy water)
 - $\nu_e + d \rightarrow e^- + p + p$
 - $\nu_x + d \rightarrow \nu_x + n + p$

Chemical Extraction Experiments

- Homestake: $\nu_e + {}^{37}\text{Cl} \rightarrow {}^{37}\text{Ar} + e^-$
 - Located in Lead, SD
 - 615 tons of C_2Cl_4 (Cleaning fluid)
 - Extraction method:
 - Pump in He that displaces Ar
 - Collect Ar in charcoal traps
 - Count Ar using radioactive decay
 - Systematic errors ~ 7%
- Gallium Exps: $\nu_e + {}^{71}\text{Ga} \rightarrow {}^{71}\text{Ge} + e^-$
 - GALLEX (Gran Sasso, Italy) uses aqueous gallium chloride (101 tons)
 - SAGE (Baksan, Russia) uses metallic gallium (57 tons)
 - Extraction method:
 - Synthesized into GeH_4
 - Inserted into Xe prop. Counters
 - Detect x-rays and Auger electrons



Sage : 67 ± 8 SNU

Gallex: 78 ± 6 SNU

(Expect 130 ± 1.1)

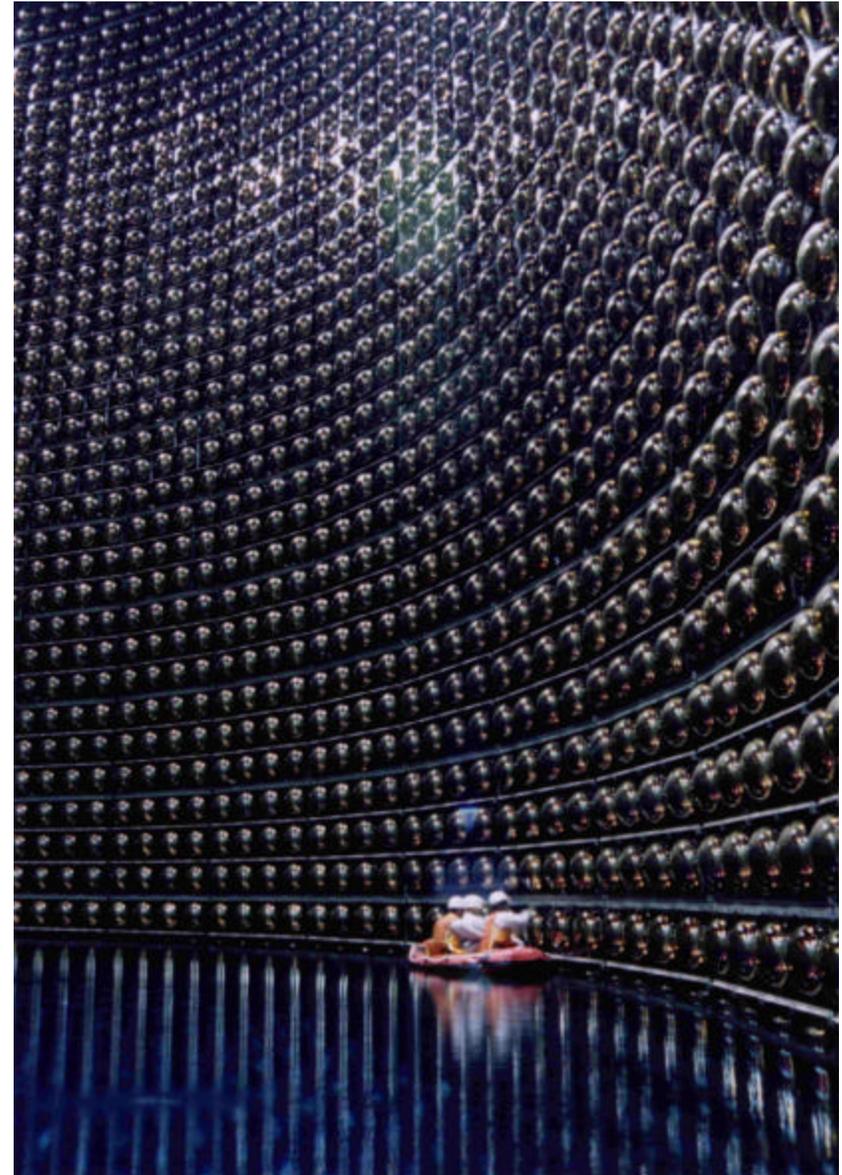
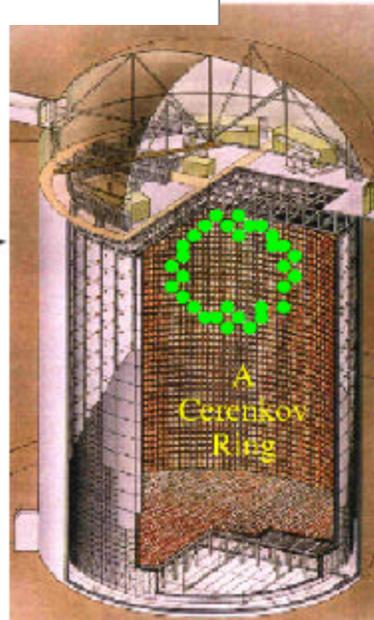
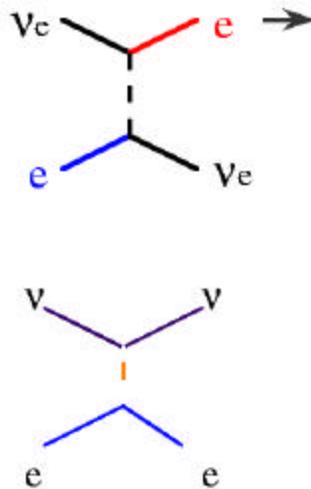
Super-K Experiment

H₂O Cerenkov Detectors

- SuperK

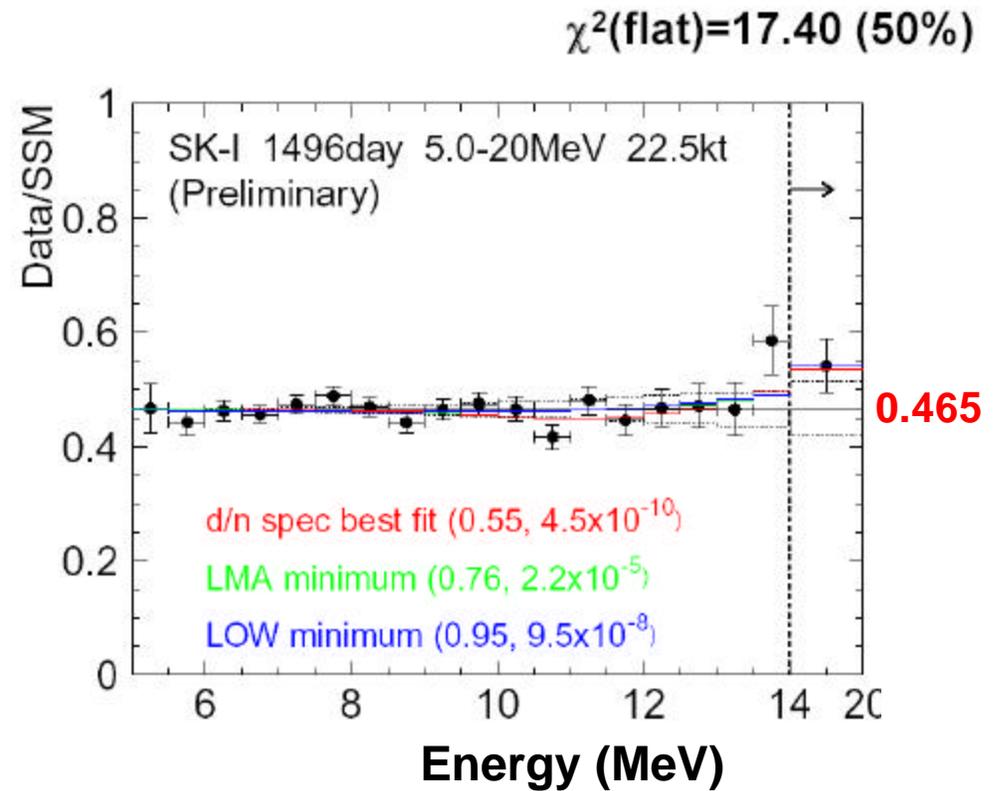
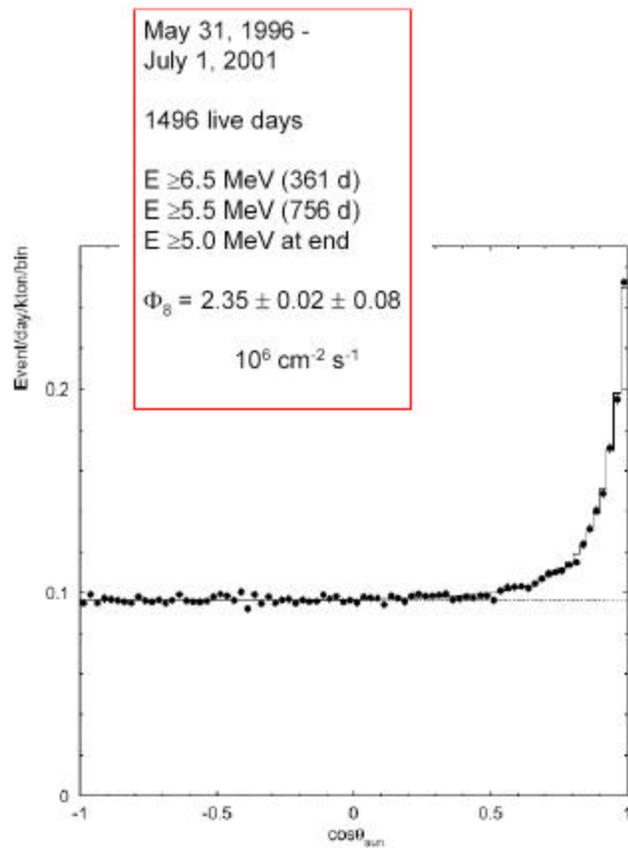
- 22.5 kton fiducial volume
- 36 m high, 34 m diam.
- 11,146 phototubes (50 cm)
- Energy threshold: 6.5 MeV
- Linac (5 – 16 MeV)
for in-situ calibration

Both NC & CC scatters



Super-K Results

- Super-K has good angular, energy, and time resolution
 - Sensitivity to seasonal variations
 - Sensitive to day/night variations
 - Ability to “see” the sun



Solar Neutrino Experiments

Rate measurement

- Homestake (US)
- SAGE (Russia)
- Gallex+GNO (Italy)
- Super-K (Japan) H₂O
- SNO (Canada) D₂O

Reaction



Obs / Theory

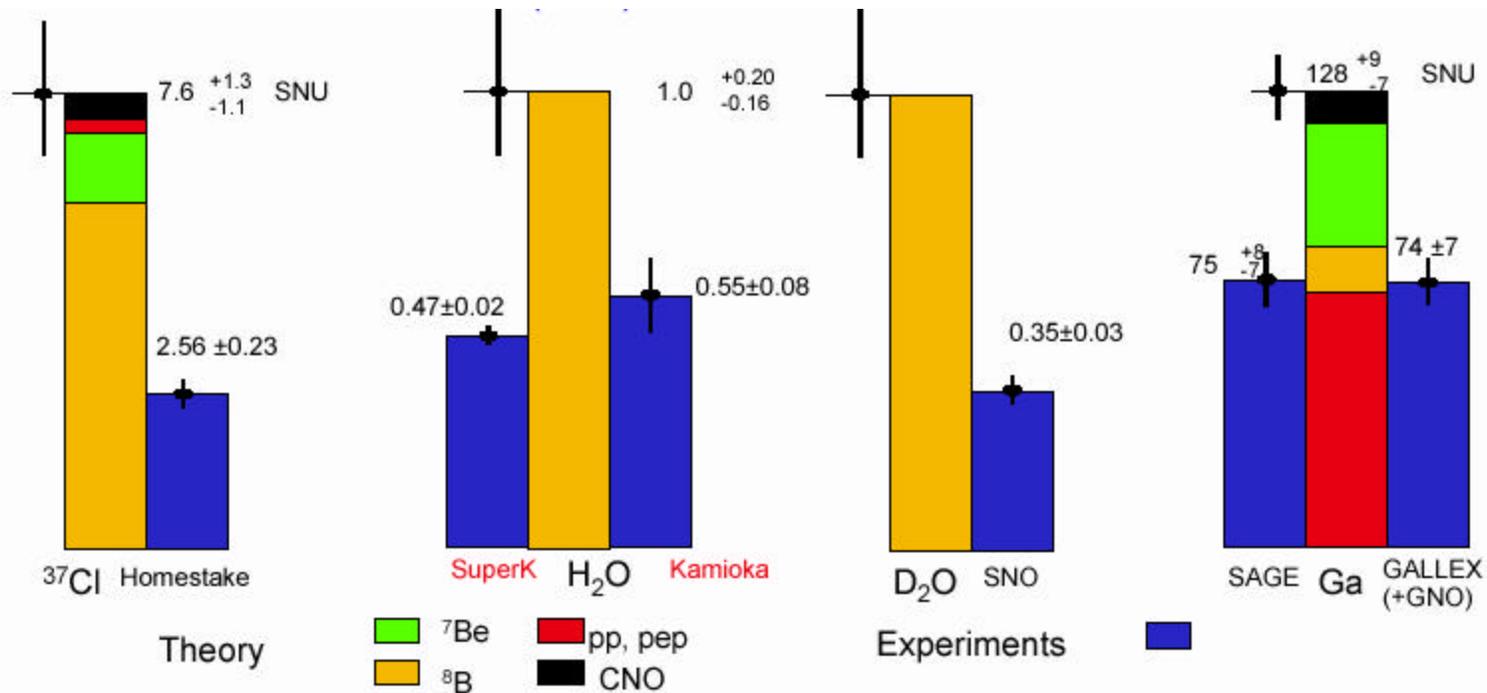
$$0.34 \pm 0.03$$

$$0.59 \pm 0.06$$

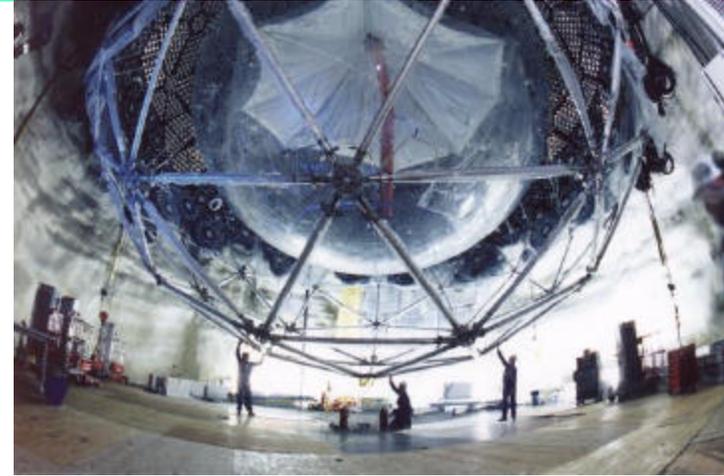
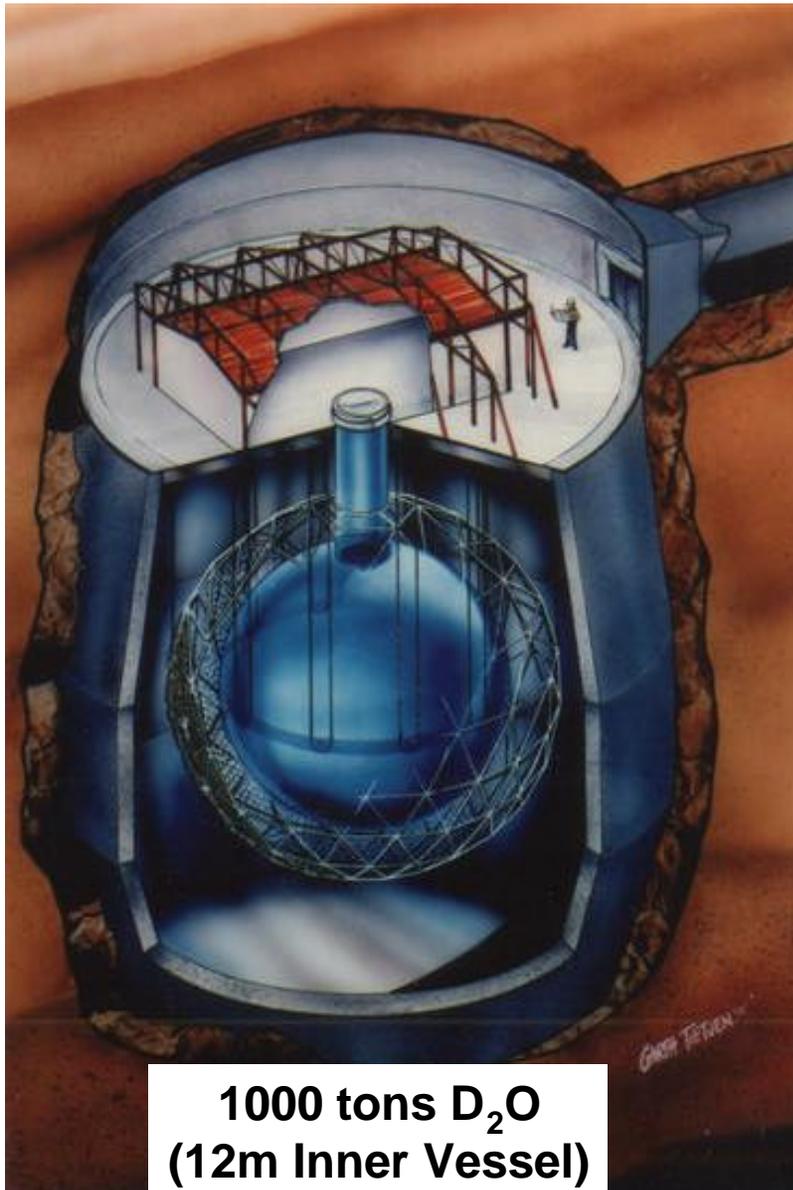
$$0.58 \pm 0.05$$

$$0.46 \pm 0.02$$

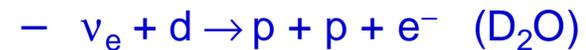
$$0.35 \pm 0.03$$



Sudbury Neutrino Observatory (SNO)



- Advantages of Heavy vs Light Water



- Cross section $\propto (E_{cm})^2 = s$

- $s = 2 m_{target} E_\nu$
 - $\Rightarrow s_N/s_{e^-} = M_p/M_e \approx 2000$

- But x5 more electrons in H₂O than n's

SNO (1kton) 8.1 CC events/day

SuperK (22ktons) 25 events/day

SNO Results

ν Reactions in Heavy Water



- "Charged Current"
- ν_e only.



- "Neutral Current"
- Equal cross section for all active ν types



- "Elastic Scattering"
- Mainly sensitive to ν_e , some sensitivity to ν_μ and ν_τ

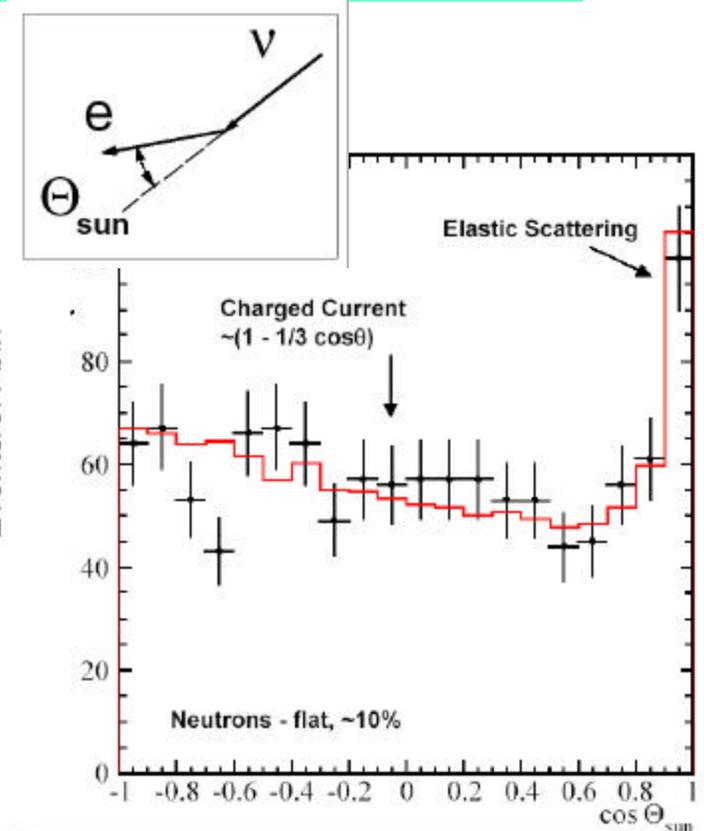
Measure total flux of solar neutrinos vs. the pure ν_e flux

Charged-Current to Neutral Current ratio is a direct signature for oscillations

$$\frac{CC}{NC} = \frac{\nu_e}{\nu_e + \nu_\mu + \nu_\tau}$$

CC/ES Could also show significant effects

$$\frac{CC}{ES} = \frac{\nu_e}{\nu_e + 0.15(\nu_\mu + \nu_\tau)}$$



ES = Elastic Scattering

- $n_e = NC + CC$
- n_m or $n_t = NC$ only

SNO Physics

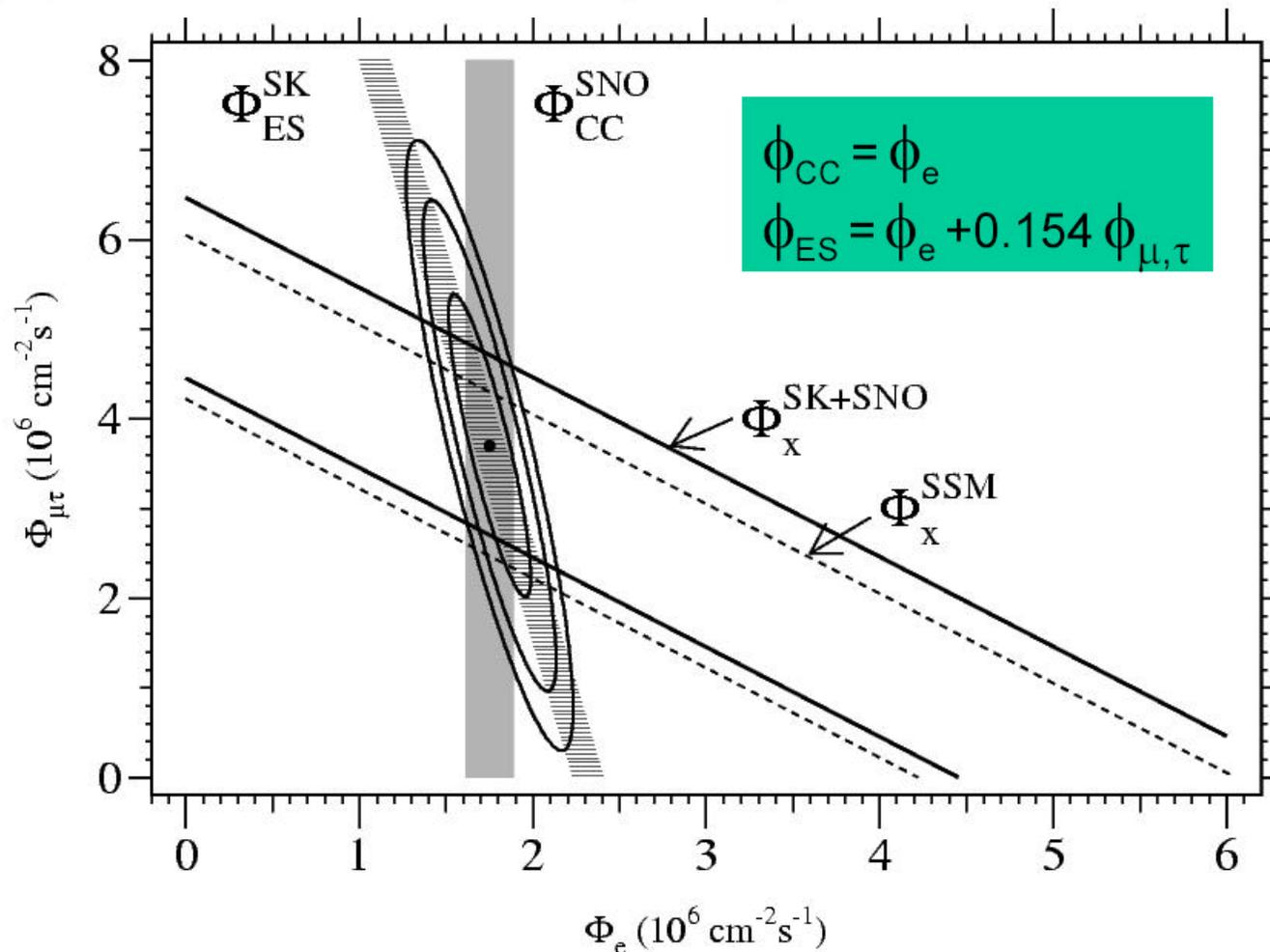
- First measurement of the total flux of ^8B neutrinos:

$$\phi_{\text{total}}(^8\text{B}) = 5.44 \pm 0.99 \times 10^6 \text{ cm}^{-2} \text{ s}^{-1}$$

Agrees well with solar models:

$$\phi_{\text{SSM}}(^8\text{B}) = 5.05 \pm 0.80 \times 10^6 \text{ cm}^{-2} \text{ s}^{-1} \text{ (BPB01)}$$

**⊢ Solar Oscillations
not totally to sterile
neutrinos**

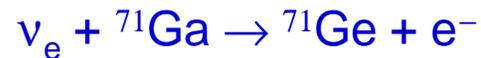


Solar Neutrino Experiments

Rate measurement

- Homestake (US)
- SAGE (Russia)
- Gallex+GNO (Italy)
- Super-K (Japan) H₂O
- SNO (Canada) D₂O

Reaction



Obs / Theory

$$0.34 \pm 0.03$$

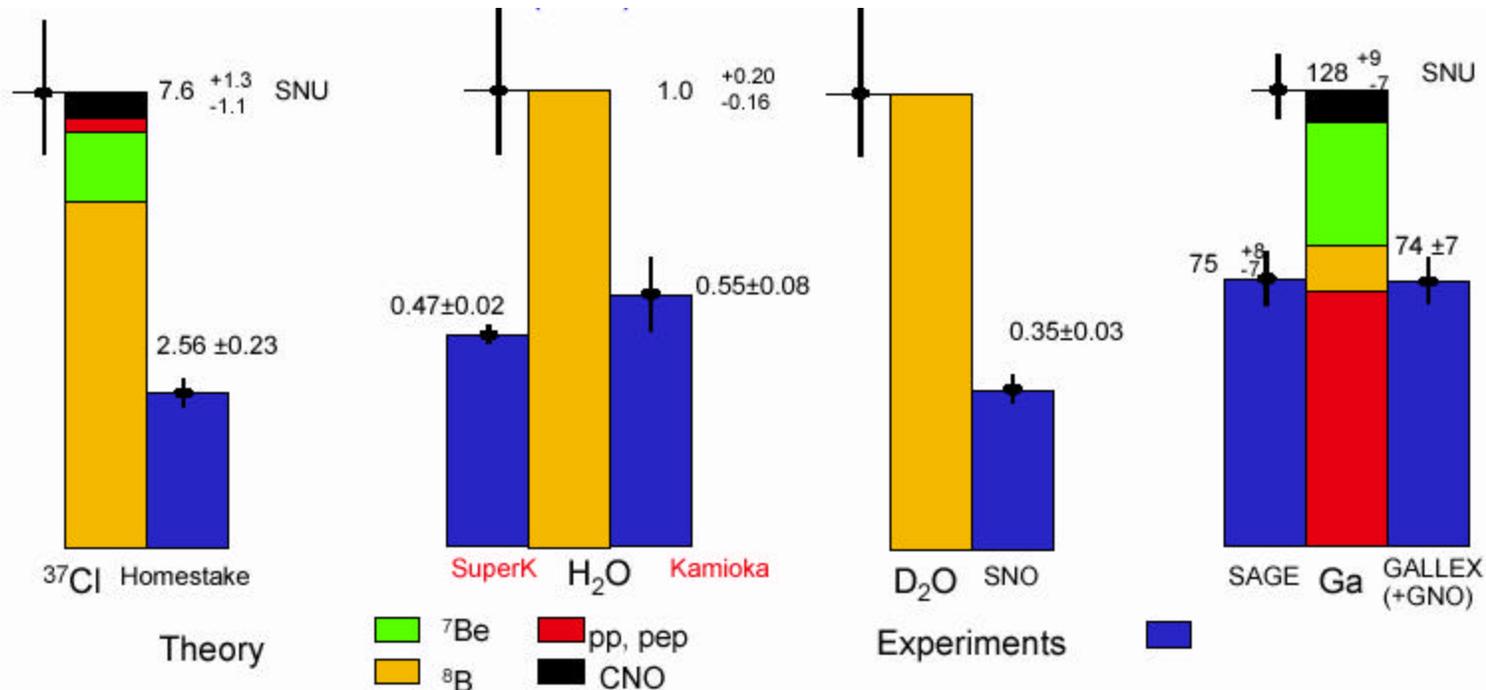
$$0.59 \pm 0.06$$

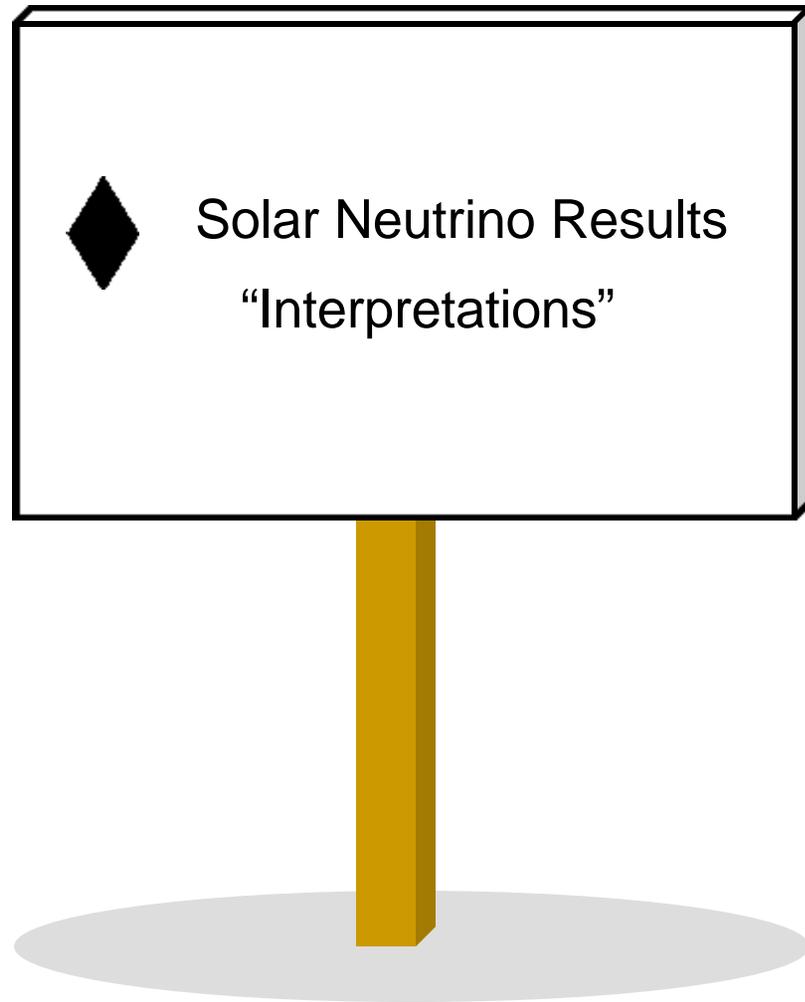
$$0.58 \pm 0.05$$

$$0.46 \pm 0.02$$

$$0.35 \pm 0.03$$

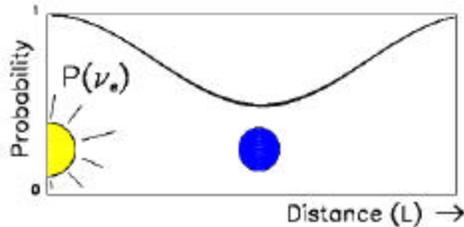
Limits
osc to ν_s
<50% @
90%CL





Oscillation Interpretations

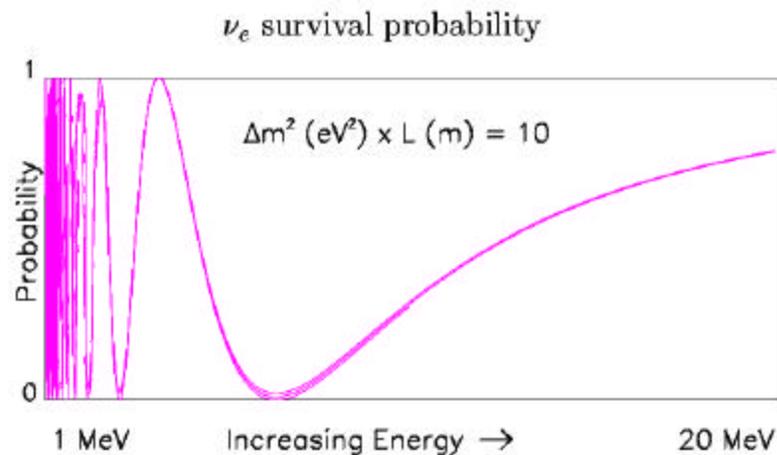
- “Just-So” or Vacuum Oscillations



- Try to fit the results into the the oscillation formula

$$P_{osc} = \sin^2 2q \sin^2 (1.27 Dm^2 L/E)$$

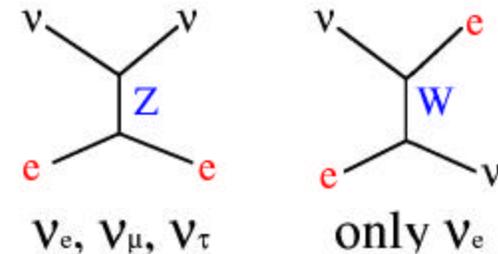
for $L \approx 10^{11}(\text{m})$



- MSW or Matter Effects in Sun (Mikheyev-Smirnov-Wolfenstein)

- Mass eigenstates propagate
- But these are mixtures of flavor eigenstates

- They have different interactions with e's in sun



- If $N =$ electron density then

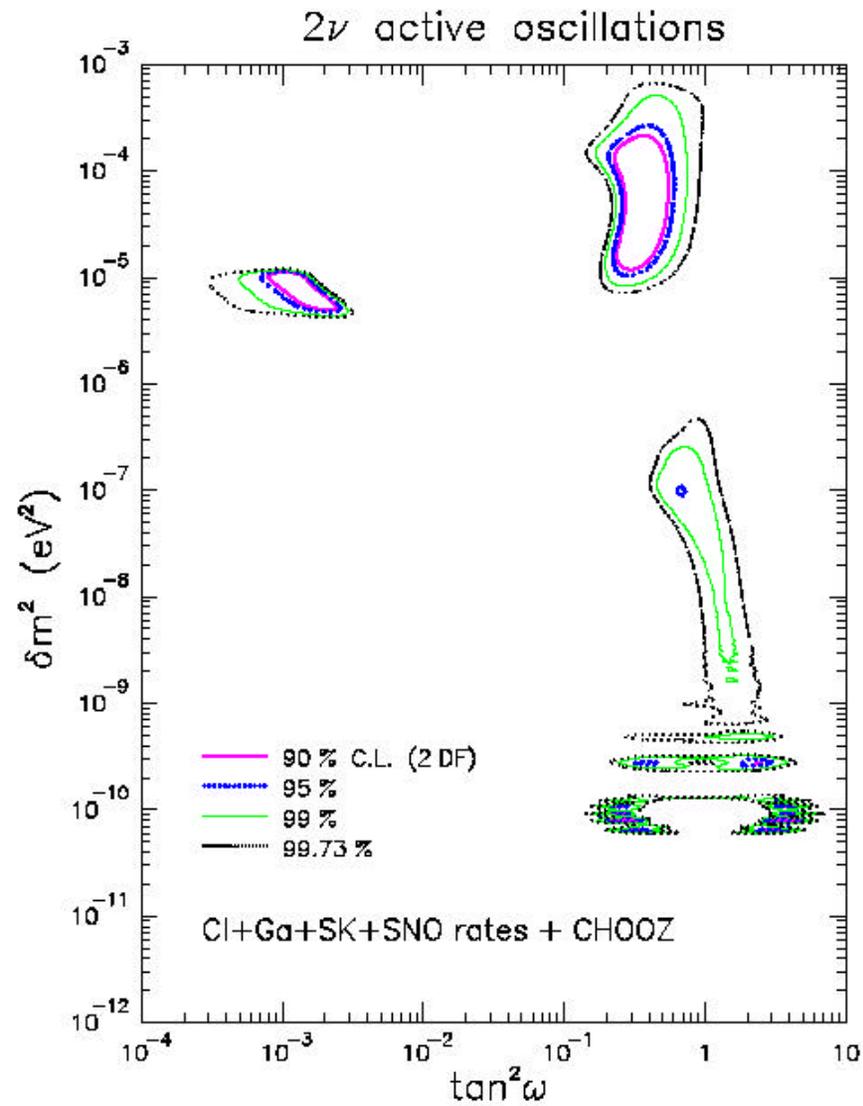
$$\text{Prob}(\nu_e \rightarrow \nu_\mu) = (\sin^2 2\theta/W^2) \sin^2 (1.27W\Delta m^2 L/E)$$

where $W^2 = \sin^2 2\theta + (\sqrt{2}G_F N(2E/\Delta m^2) - \cos 2\theta)^2$

Resonance Condition:

$$\sin^2 2q_{eff} = 1 \text{ if } W^2 = \sin^2 2q$$

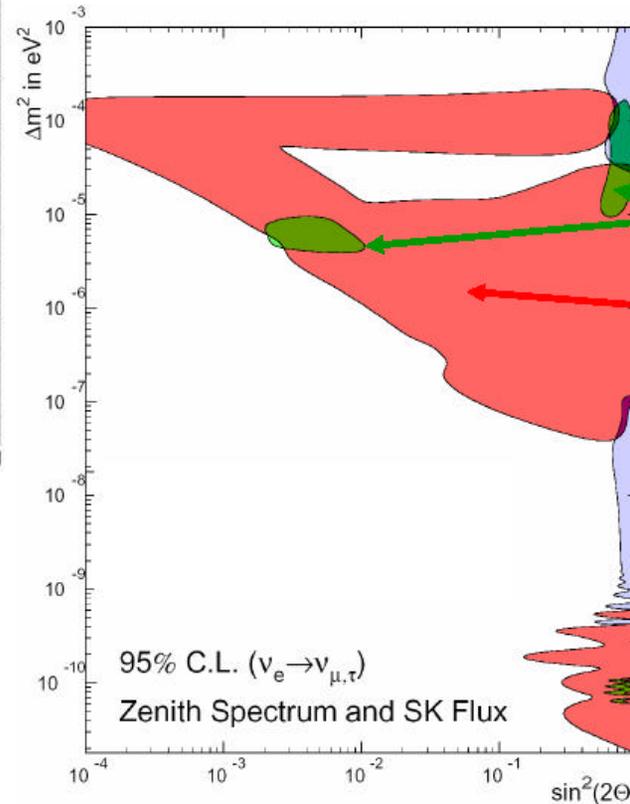
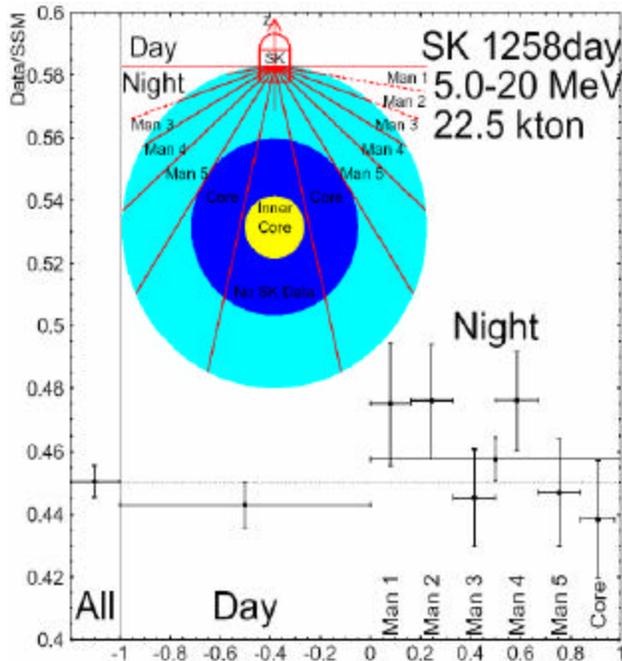
Allowed Regions



Fogli et al. hep-ph/0106247; Bahcall et al. hep-ph/0106258

- Matter effects can also occur in the electrons in the earth
 - Would cause a *day/night* effect in the Super-K data

Oscillation Interpretations (Preliminary Super-K)



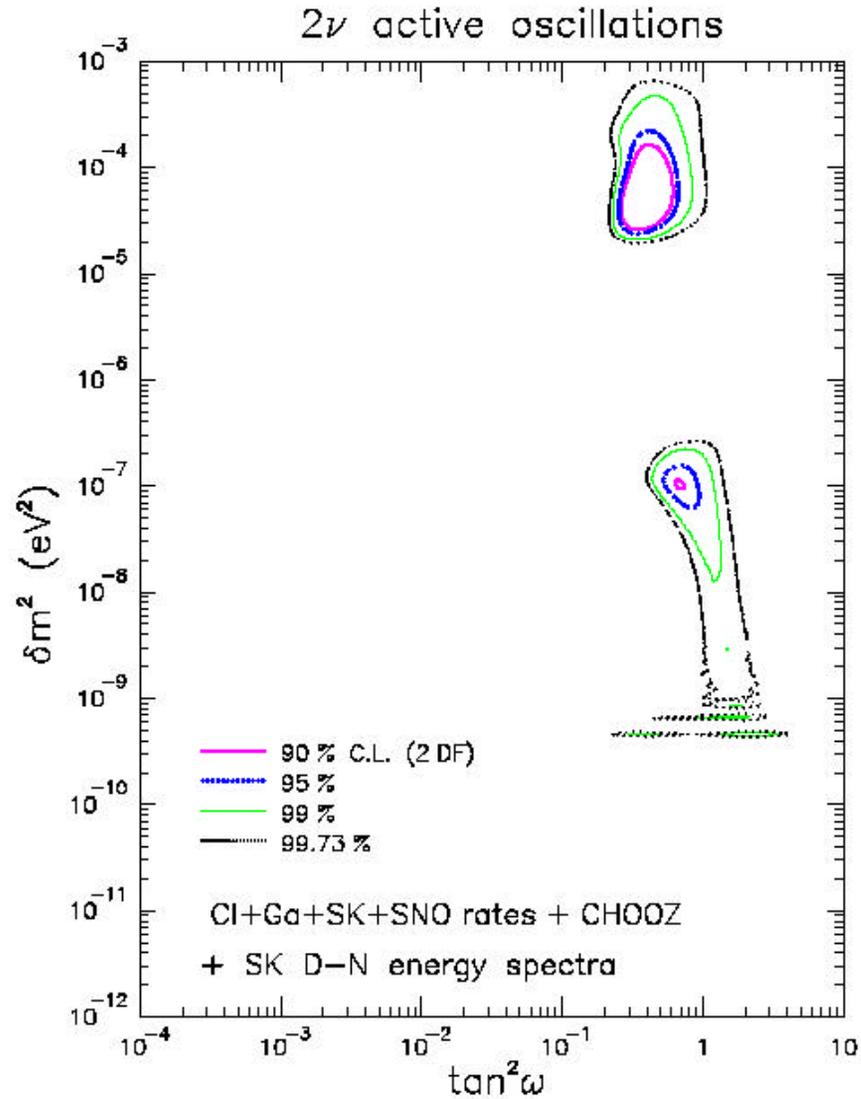
SK+Gallium+Chlorine - flux only allowed 95% C.L.

95% excluded by SK flux-independent zenith angle energy spectrum

95% C.L. allowed. - SK flux constrained w/ zenith angle energy spectrum

95% C.L. ($\nu_e \rightarrow \nu_{\mu,\tau}$)
Zenith Spectrum and SK Flux

Putting It All Together



Fogli et al. hep-ph/0106247; Bahcall et al. hep-ph/0106258

What's Coming Up in Solar $\bar{\nu}_e$'s

- Kamland

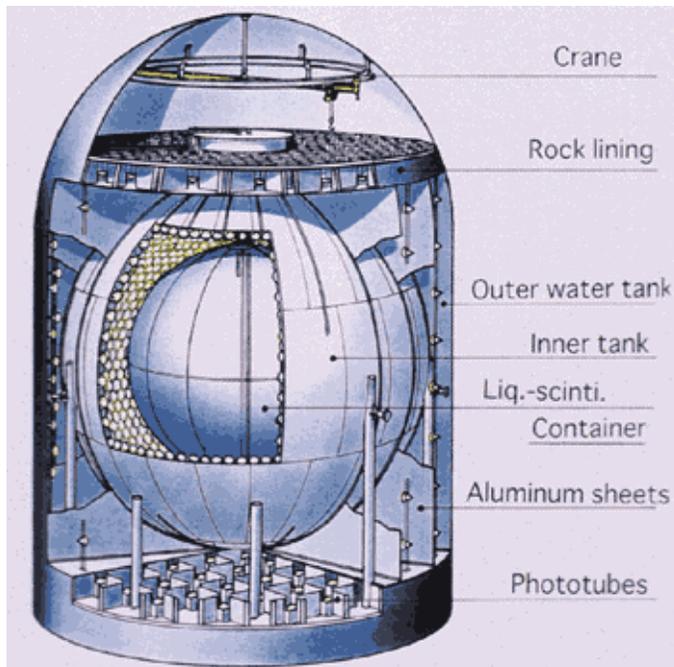
Reactor neutrino exp. In solar region

- 1000 m³ liquid scintillator
- 2000 17-inch phototubes

$\bar{\nu}_e$ from reactors (L ~ 170 km)

Detect e^+ from $\bar{\nu}_e + p \rightarrow e^+ + n$

($E_{threshold} = 1.8 \text{ MeV}$)



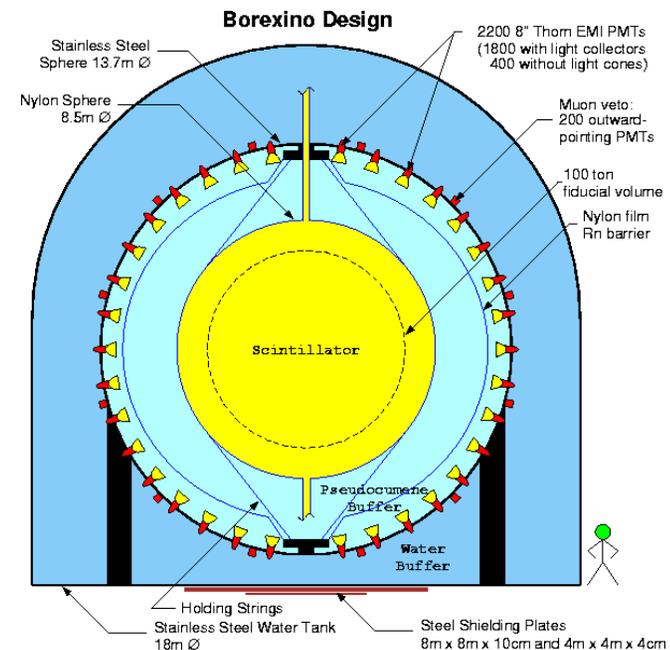
- Borexino

Go after ${}^7\text{Be}$ $\bar{\nu}_e$'s

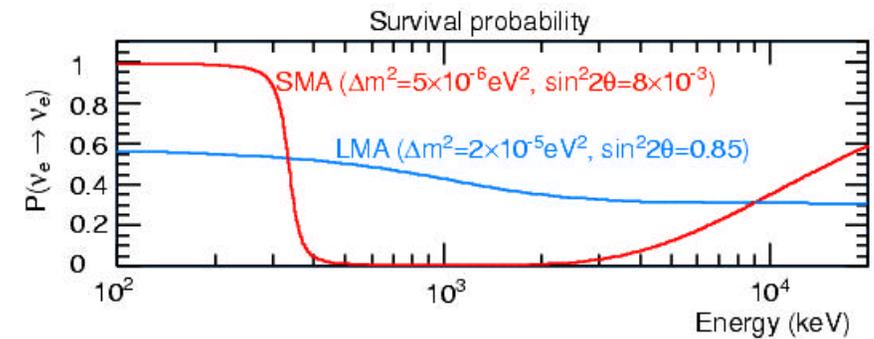
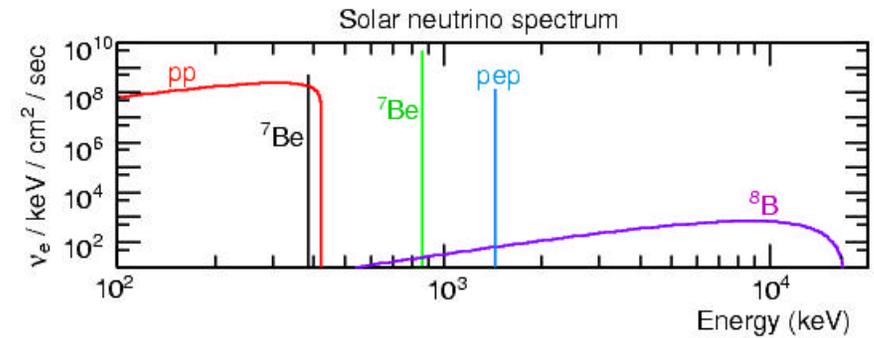
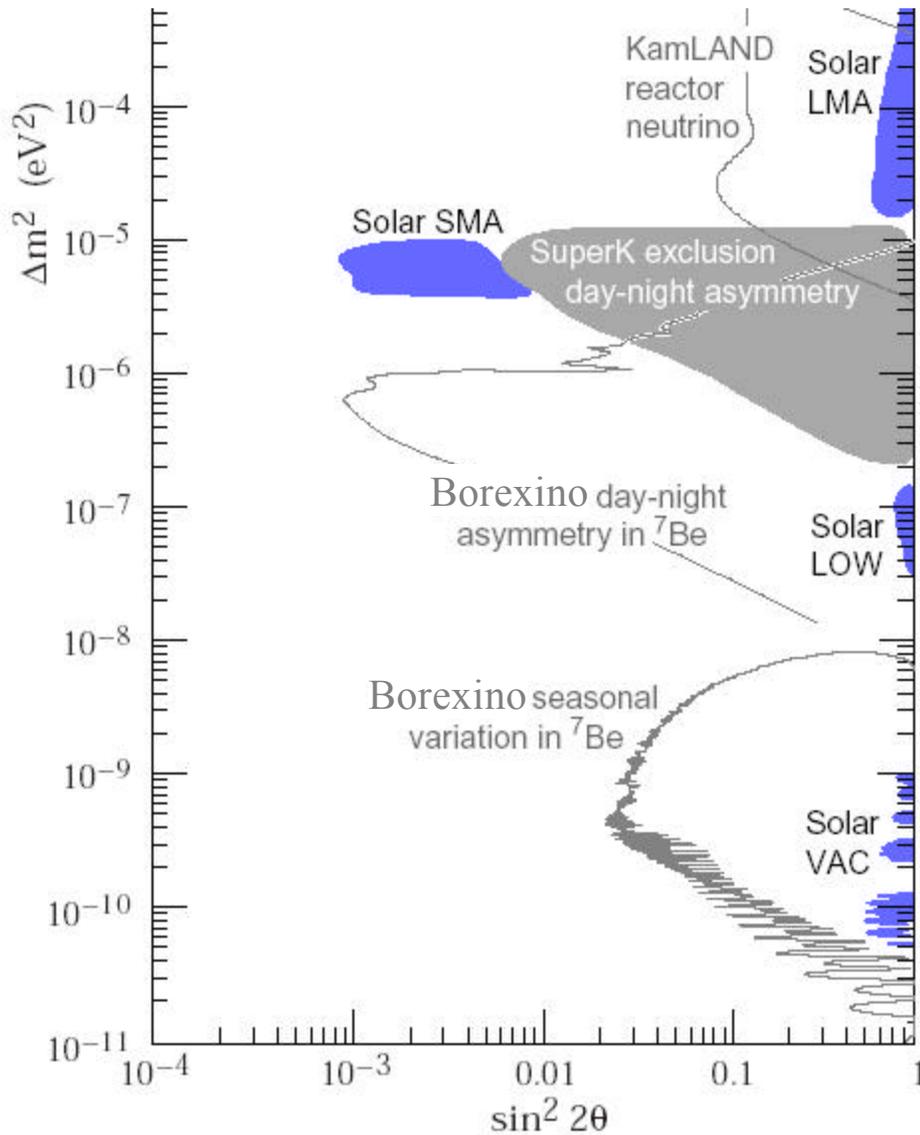
- 300 ton liquid scintillator
- 2200 8-inch phototubes
- $E_e > 250 \text{ keV}$

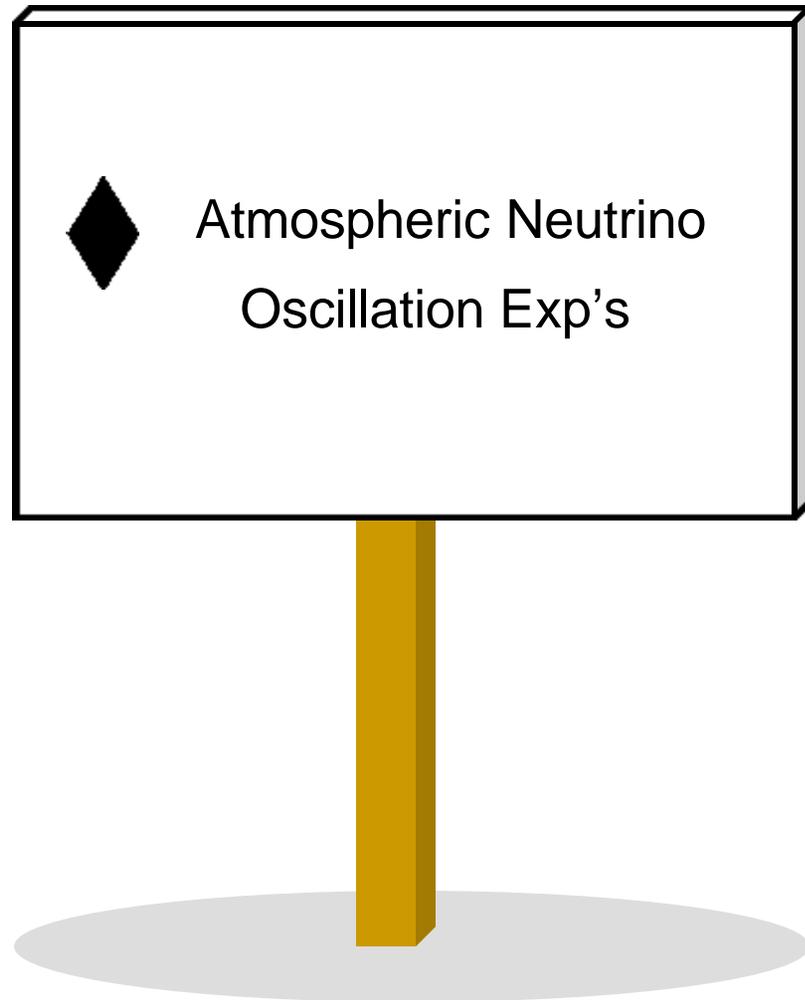
- Detect $\nu_e + e^- \rightarrow \nu_e + e^-$

- 55 events/day for SSM

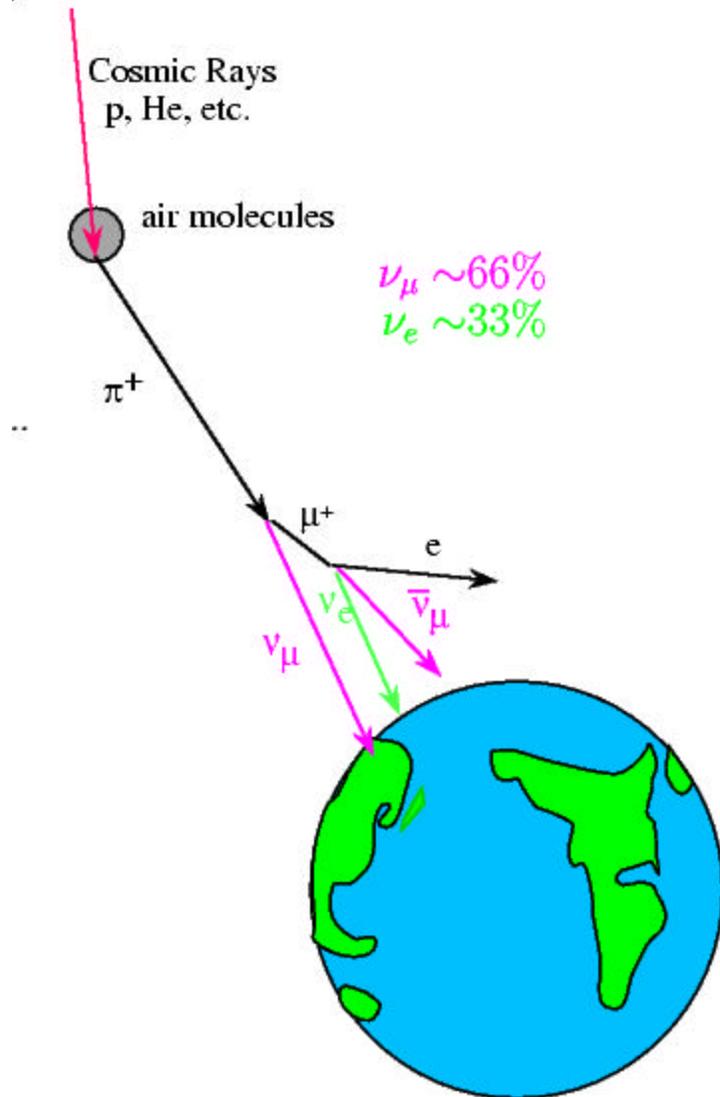


Kamland and Borexino Sensitivity





Atmospheric Neutrino Oscillations



- Atmospheric Neutrino Flux
 - From π and μ decay from cosmic-ray hadronic showers in the atmosphere
 - Flux modeled using:
 - Measured cosmic-ray fluxes
 - Accelerator cross section measurements
 - Include geomagnetic effects
 - Some disagreements with atmospheric muon measurements (~20% level)

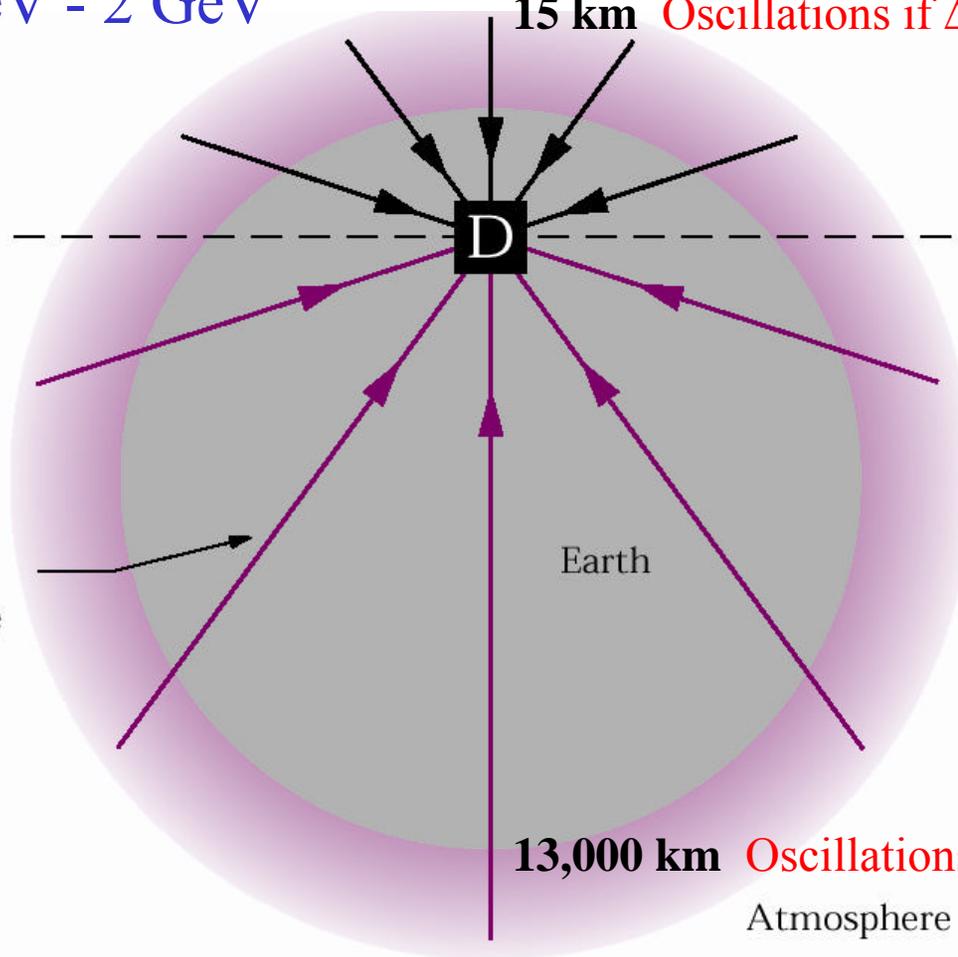
Atmospheric Neutrino Studies

$E_\nu \sim 300 \text{ MeV} - 2 \text{ GeV}$

$$\cos\theta_{\text{Zenith}} = 1.0$$

15 km Oscillations if $\Delta m^2 > 10^{-2} \text{ eV}^2$

Neutrino Made
in the Atmosphere



13,000 km Oscillations if $\Delta m^2 > \text{few} \times 10^{-5} \text{ eV}^2$

Atmosphere

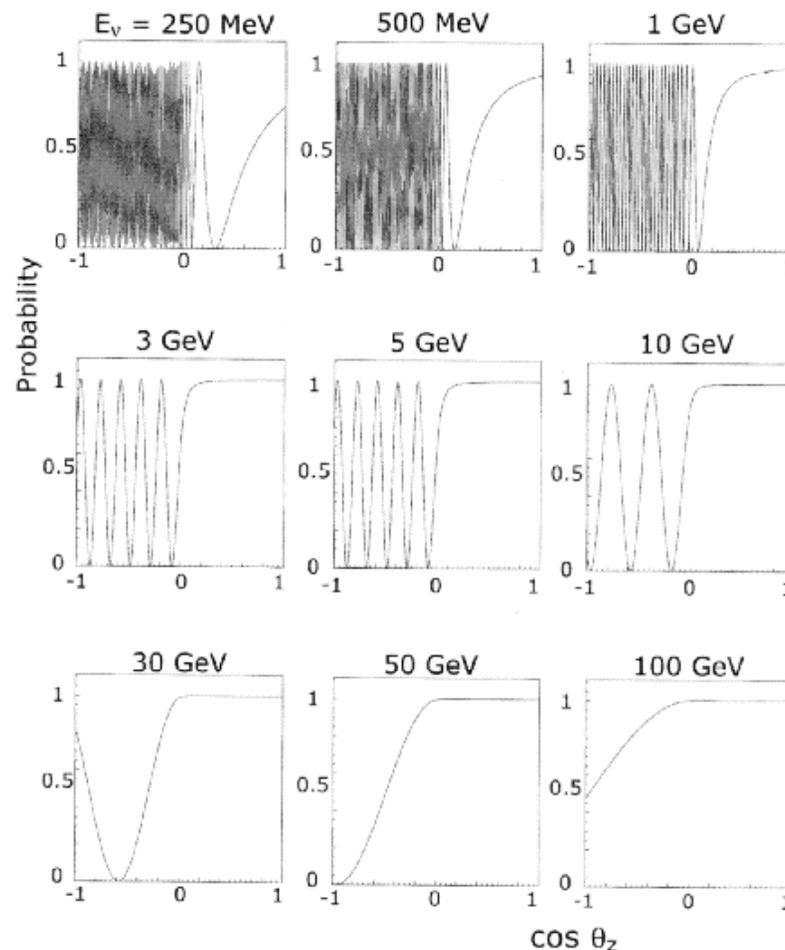
$$\cos\theta_{\text{Zenith}} = -1.0$$

- Flux dependence on azimuth is directly related to distance traveled
 - Perfect laboratory to search for oscillations

Oscillation Survival Probability for $\nu_m \rightarrow \nu_t$

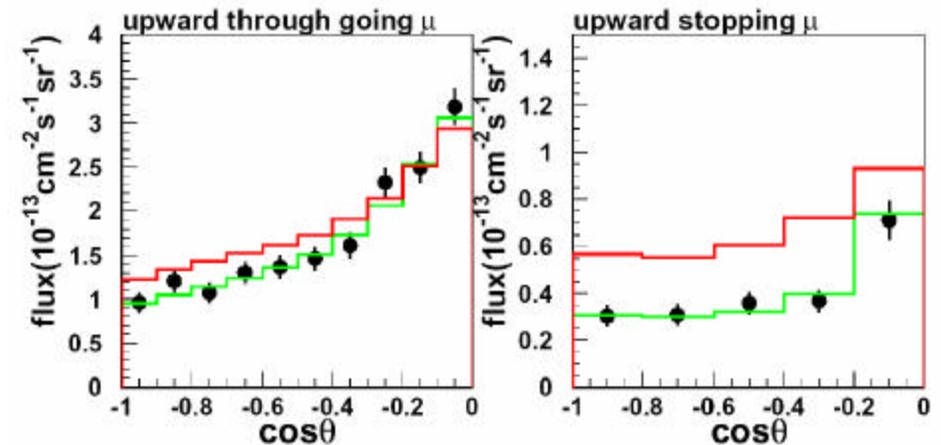
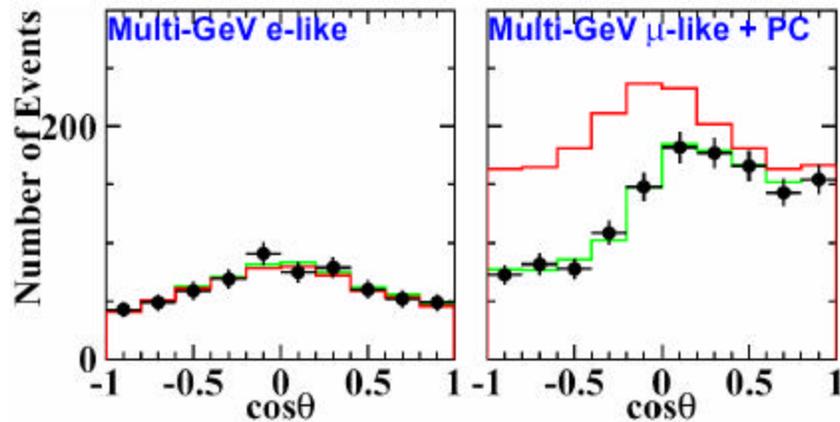
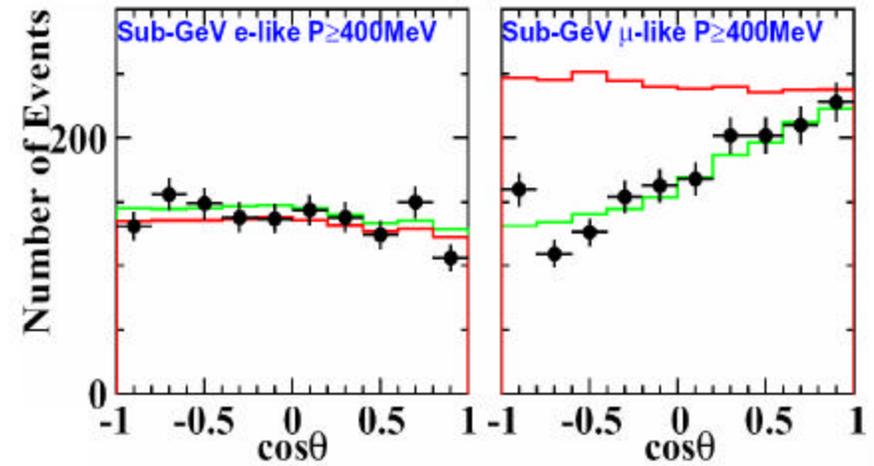
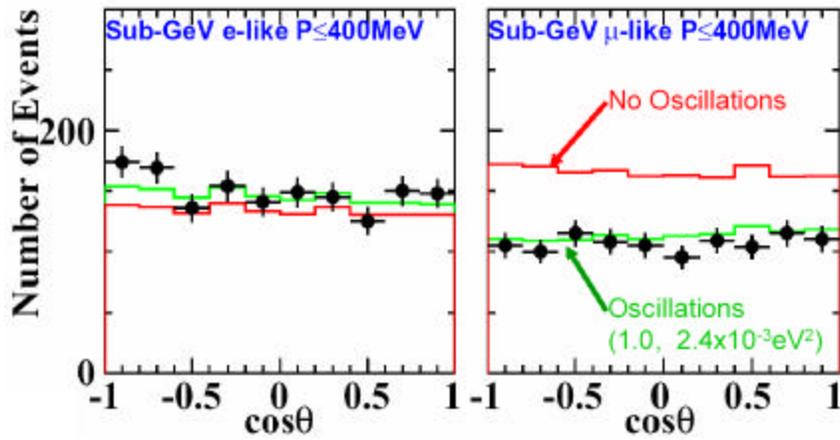
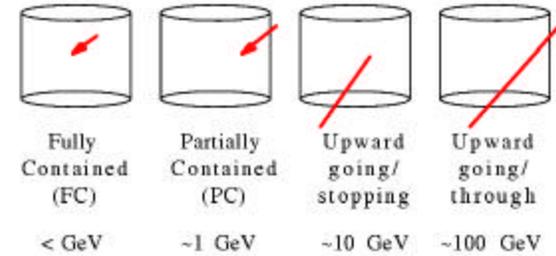
- $\cos\theta_{\text{Zenith}}$ distributions for various neutrino energies, E_ν
(Rapid change in behavior for $\cos\theta_z < 0$)

- $\Delta m^2 = 5 \times 10^{-3} \text{ eV}^2$
 $\sin^2 2\theta = 1.0$

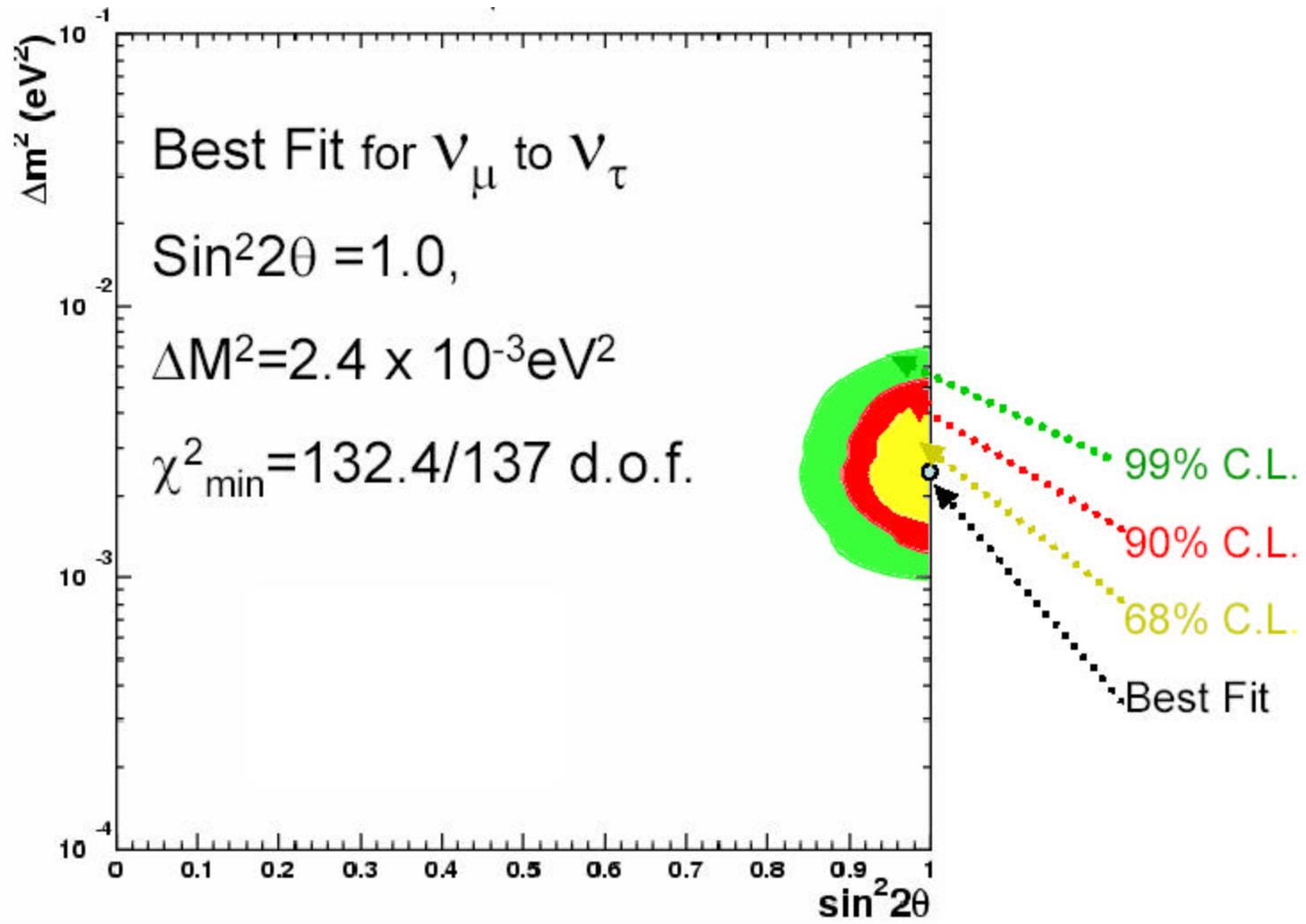


Note: Detector resolution will integrate over rapid oscillations and average to $\frac{1}{2}$.

Super-K Atmospheric Results (1290 days)

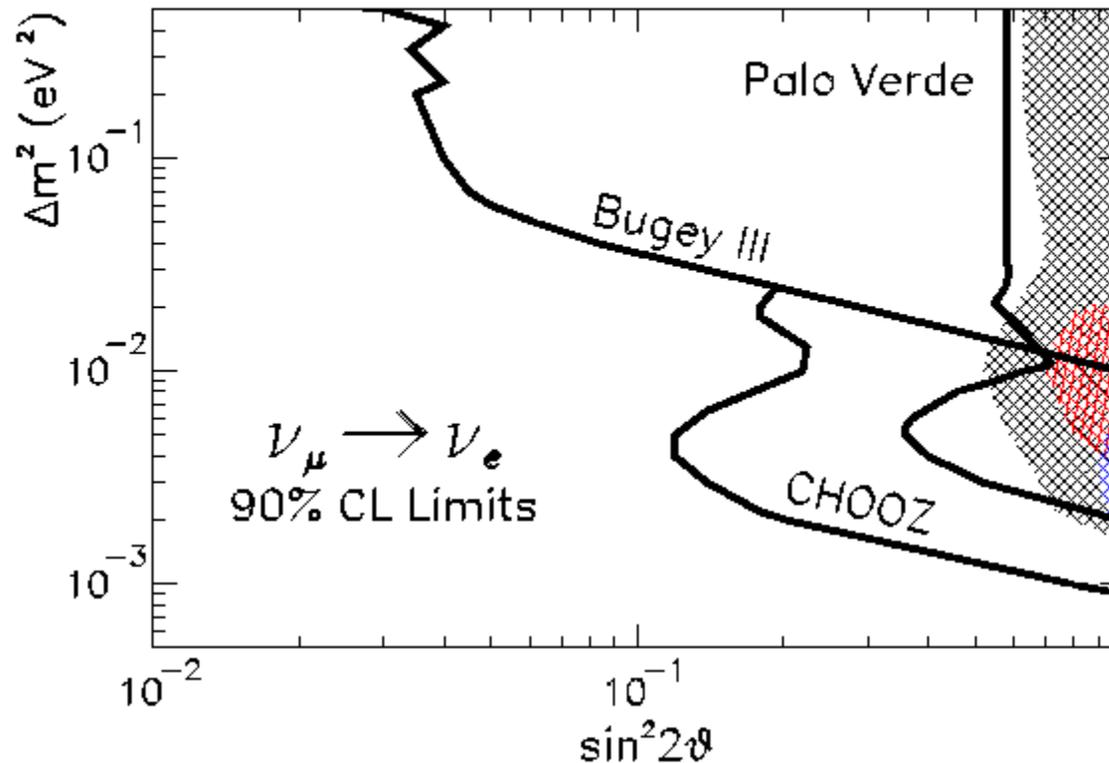


Super-K Fits to $n_m \textcircled{R} n_t$



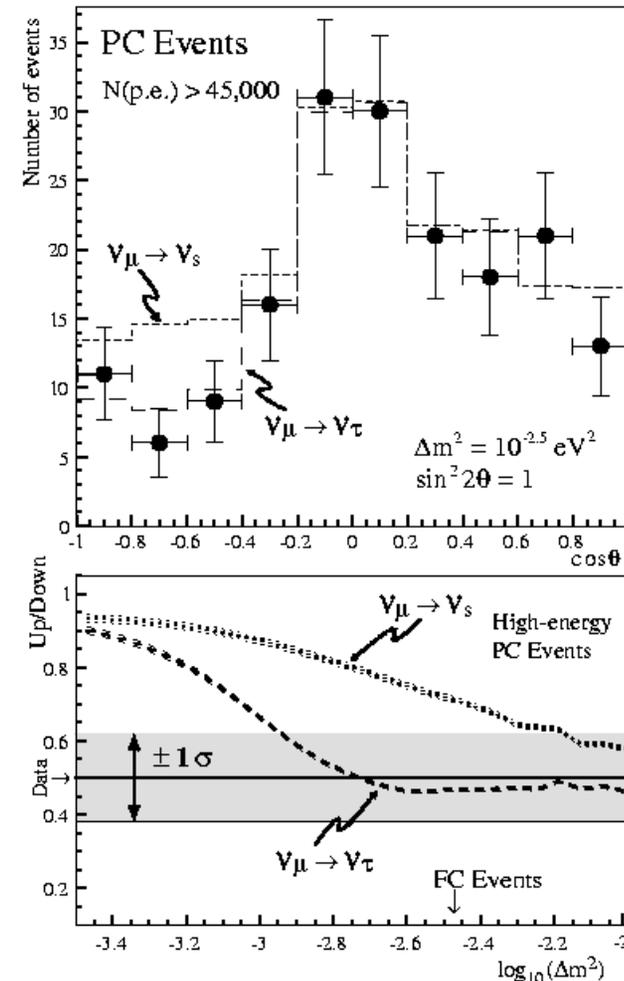
Reactor Experiments Limit Atmospheric $\nu_m \text{ @ } \nu_e$ Possibilities

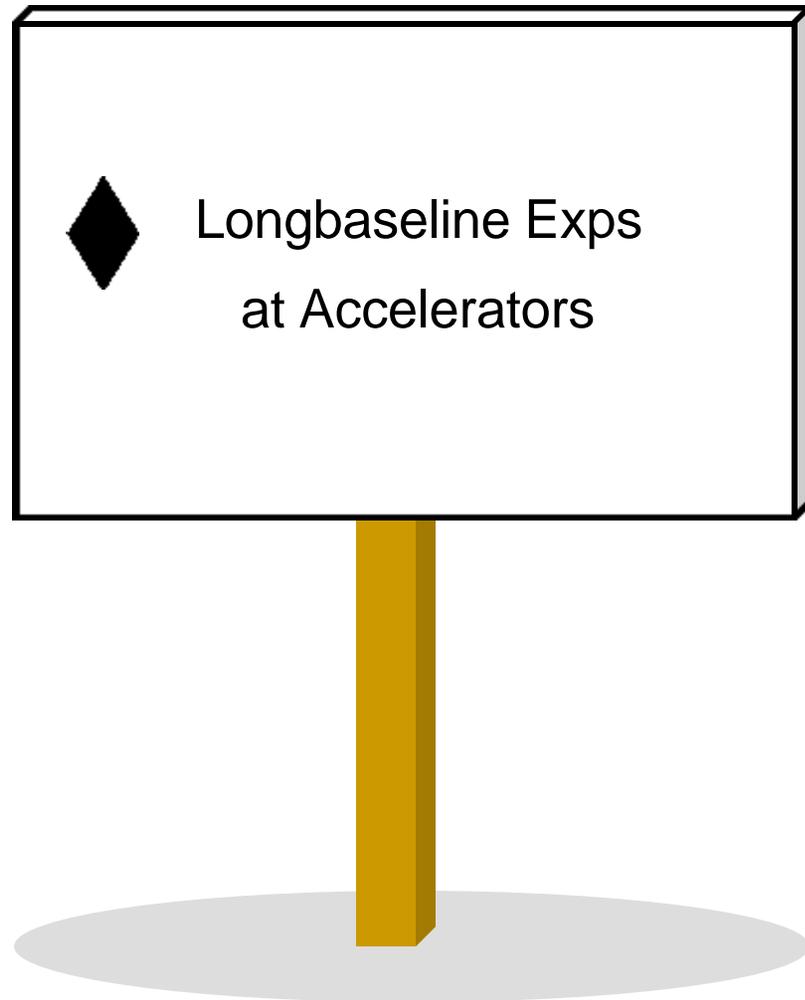
- CHOOZ, Bugey, and Palo Verde Reactor Experiments
 - $\langle E_\nu \rangle \sim 3 \text{ MeV}$ and $L \sim 1 \text{ km}$
- Dominant $\nu_\mu \rightarrow \nu_e$:
 - Ruled out by CHOOZ reactor ν experiment
 - Sub-dominant osc. possible at the $\sin^2 2\theta < 0.10$ level



Can atmospheric result be due to $n_m \textcircled{R} n_s$ oscillations ?

- Interactions with matter in earth different for $\nu_\mu \rightarrow \nu_\tau$ VS. $\nu_\mu \rightarrow \nu_{\text{sterile}}$
 - ν_{sterile} has no NC interactions with quarks
 - Mainly near $\cos\theta = -1.0$
- Also, differences for:
 - NC enriched multi-ring events
 - Upward-going thru- μ events
- Exclude
 - Complete $\nu_\mu \rightarrow \nu_{\text{sterile}}$ ruled out at 99% CL
 - $\nu_\mu \rightarrow \nu_{\text{sterile}}$ fraction $< 25\%$ at 90% CL





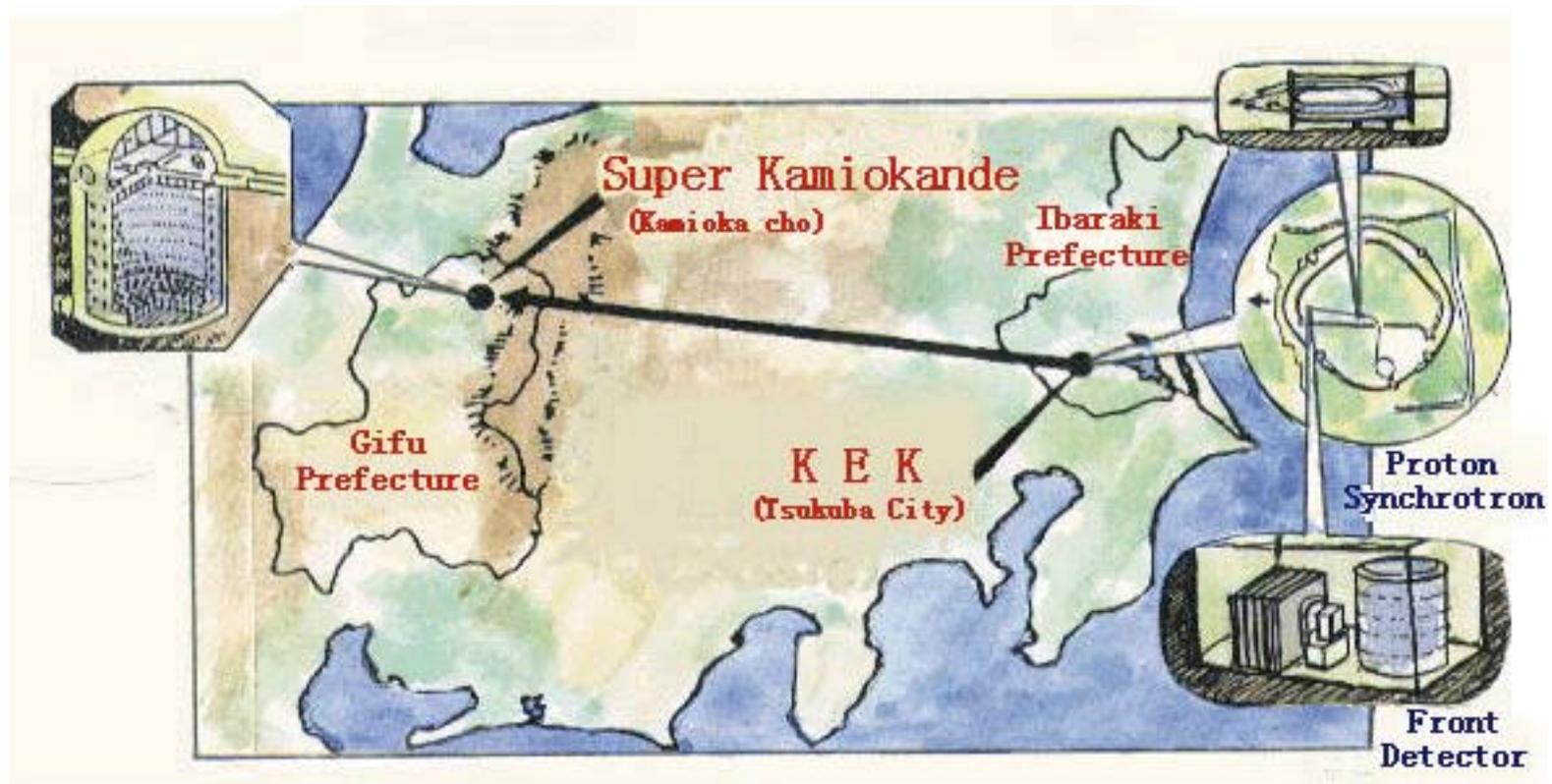
Long-Baseline Experiments

- Long-baseline experiments can be used to check atmospheric results with a well controlled accelerator produced ν beam
- With high statistics and good control of systematics can:
 - Measure oscillation parameters Δm^2 , $\sin^2 2\theta$ more accurately
 - See oscillatory behavior with energy
 - Measure $\nu_\mu \rightarrow \nu_e$ at the atmospheric Δm^2
 - Directly observe ν_τ events from $\nu_\mu \rightarrow \nu_\tau$ oscillations
 - Do further checks of possible $\nu_\mu \rightarrow \nu_{\text{sterile}}$
- Having a near monitoring detector along with far detector is best
- Current and near future experiments: **K2K, MINOS, CNGS**

KEK to SuperK (K2K) Experiment

See C. Walters Talk

- Low energy, $\langle E_\nu \rangle = 1.4$ GeV, beam sent from KEK to SuperK (250 km)
- Several front detectors at 100m and beam monitors



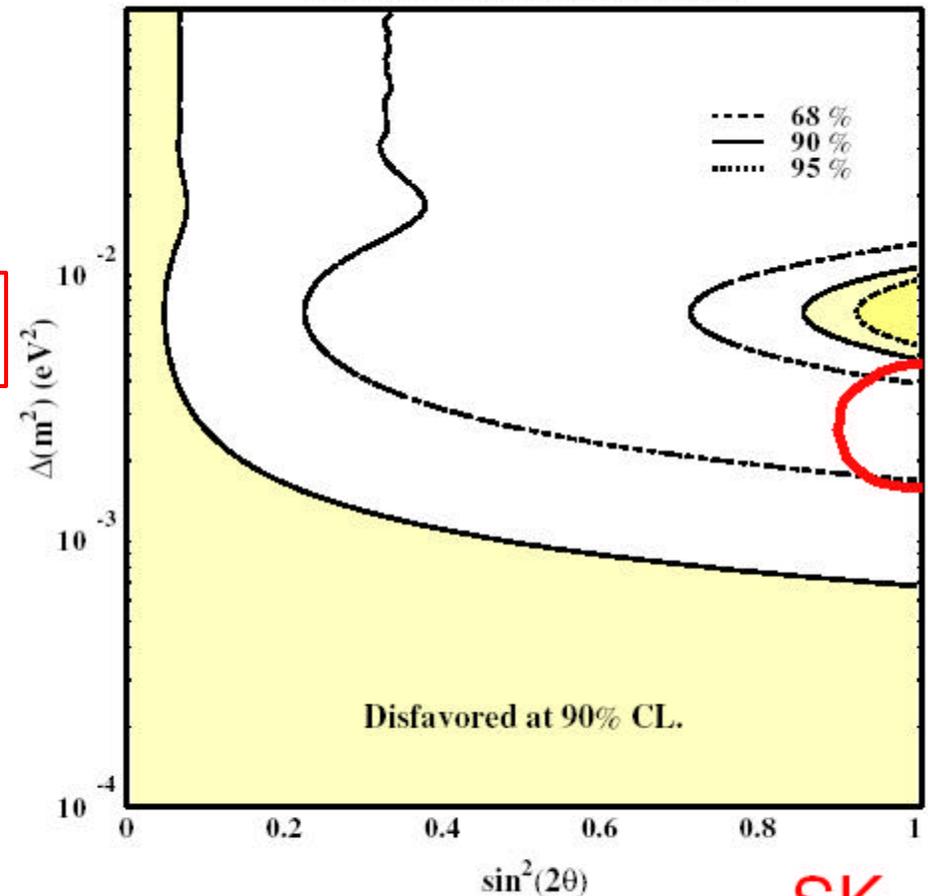
K2K Results (Events)

5.6×10^{19} POT delivered,
through July 2001

Event Summary:

	detected	no osc	3×10^{-3}
FC	56	80.6 ± 8.0	52.0
1-ring μ	30	43.6 ± 6.9	24.2
1-ring e	2	4.4 ± 1.7	3.7
multiring	24	31.9 ± 5.3	24.1

Observed/Expected Counts Oscillation Analysis
Gaussian tail hypothesis test

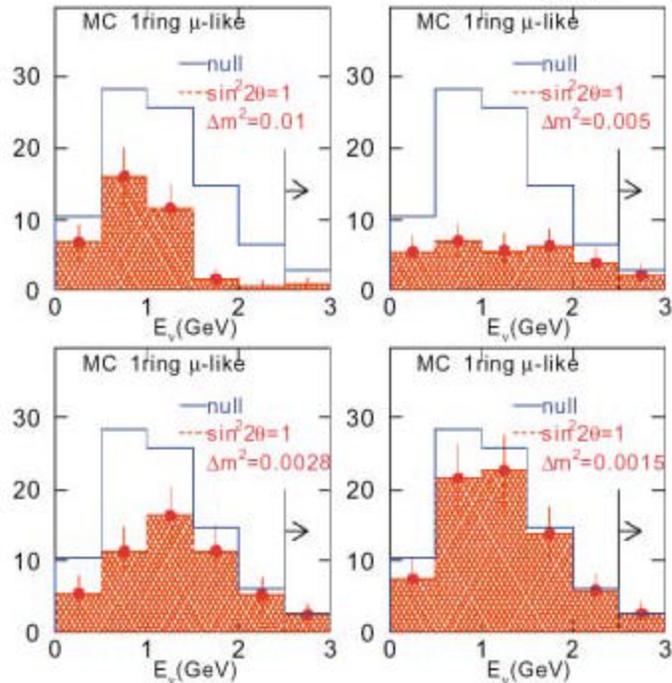


SK
best-fit

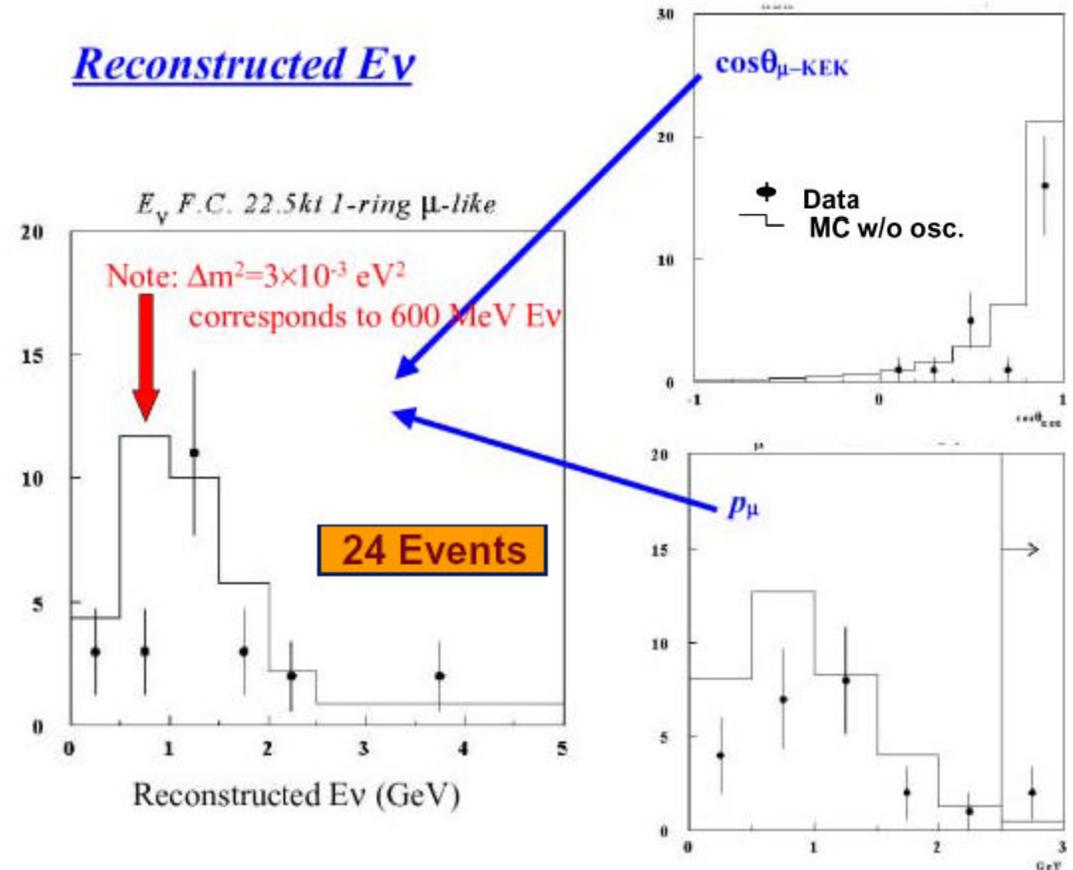
==> Null Oscillation probability: less than 3%

K2K Results (Energy Spectrum)

Monte Carlo Prediction for various oscillation scenarios



Reconstructed E_ν



**Conclude: Event deficit consistent with oscillations
but no oscillatory behavior and information on Δm^2**

NuMI / MINOS Experiment

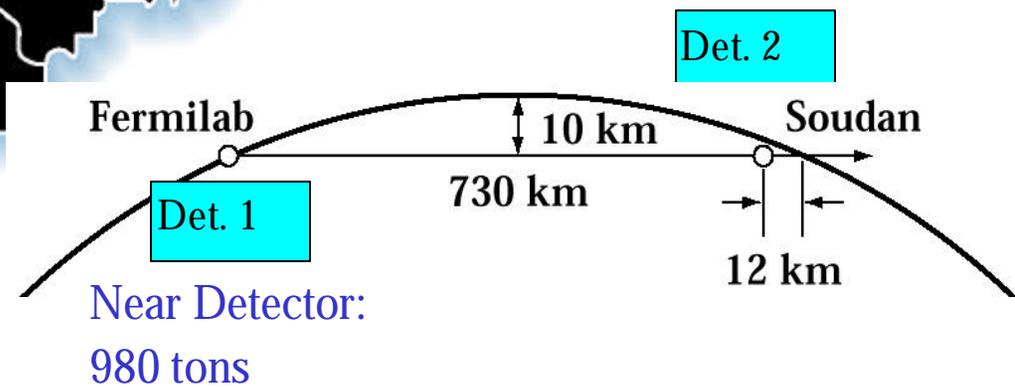
“Neutrinos at the Main Injector”



Two Detector Neutrino Oscillation Experiment



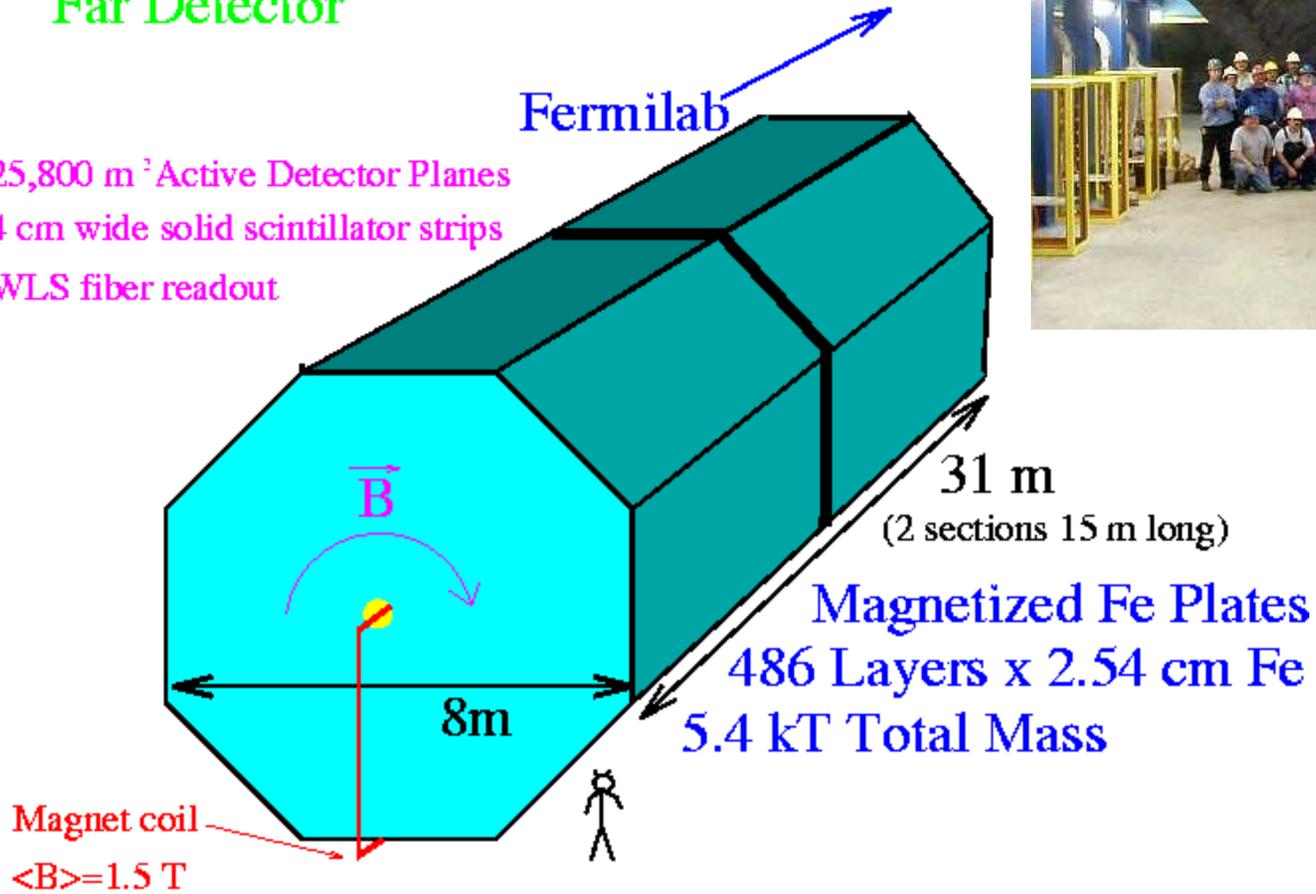
Far Detector:
5400 tons



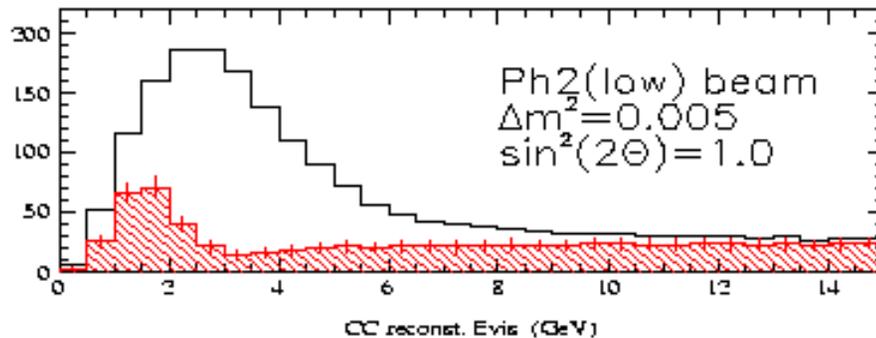
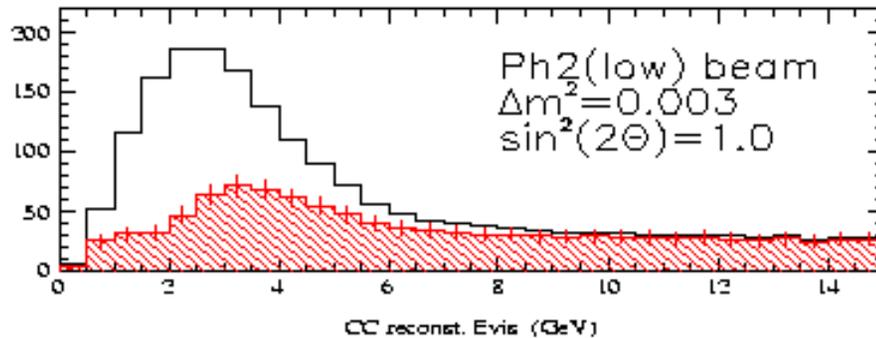
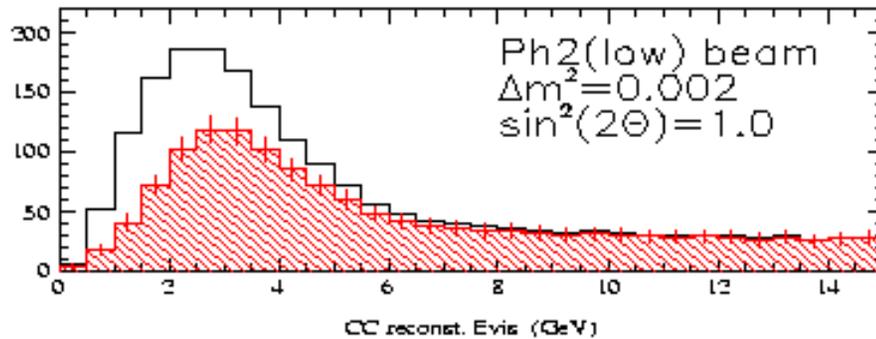
MINOS Far Detector

Far Detector

25,800 m² Active Detector Planes
4 cm wide solid scintillator strips
WLS fiber readout



MINOS Energy Spectra



10 kt-yr Exposure
 (~700 CC events/yr)

Solid lines - energy spectrum
 without oscillations

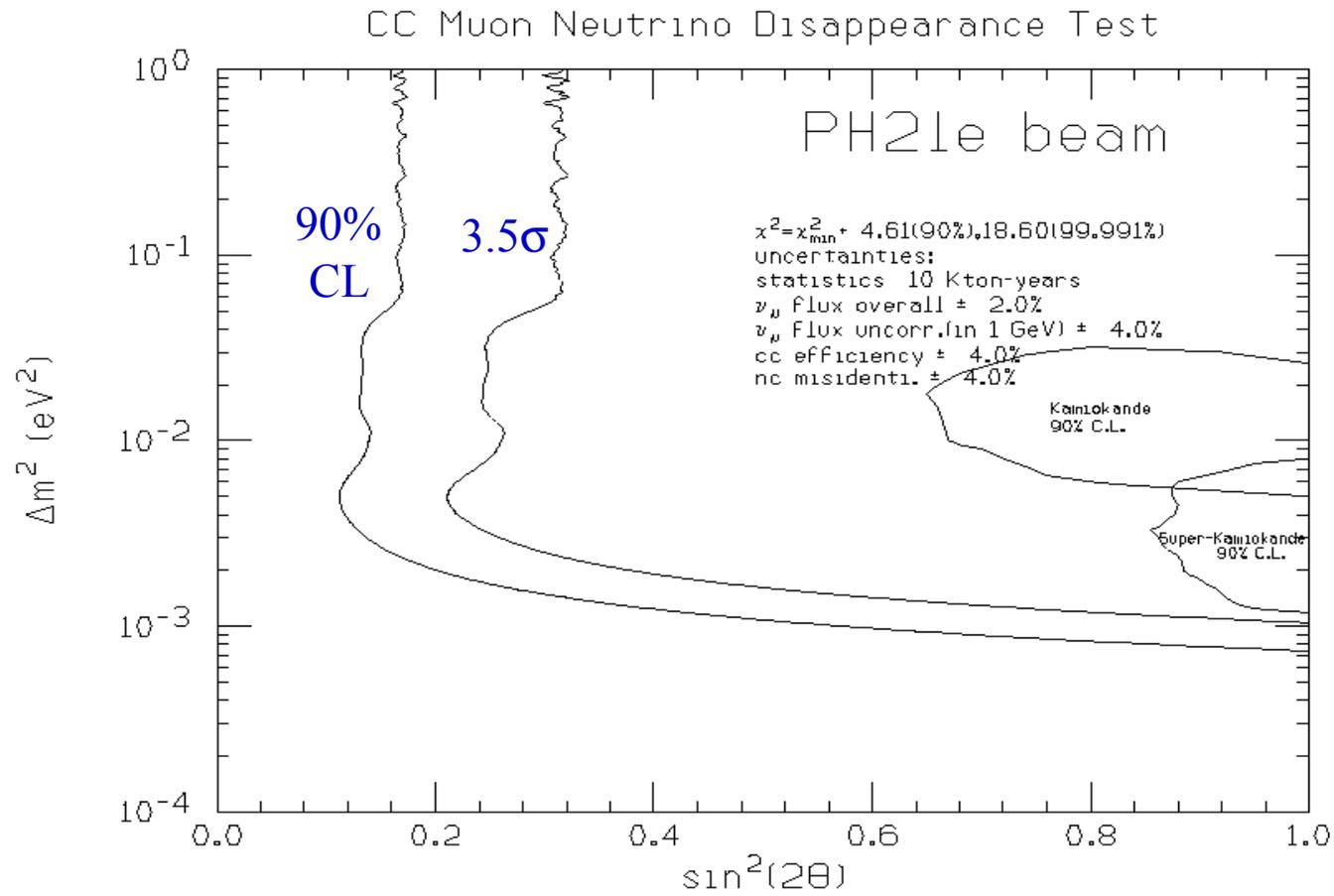
Dashed histogram - spectrum
 in presence of oscillations

Can measure:

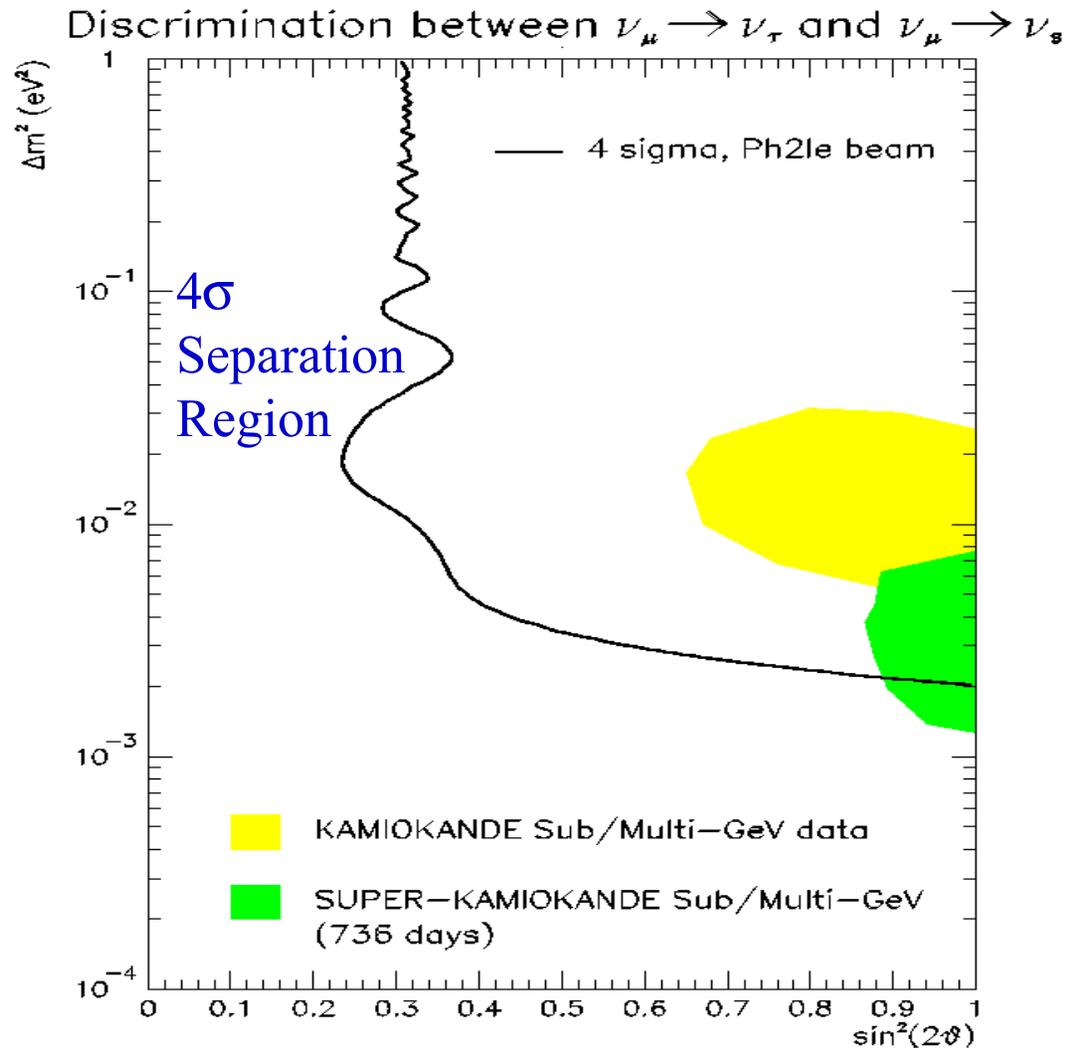
Δm^2 to ~10 - 20%

$\sin^2 2\theta$ to ~0.10

MINOS Δm^2 Sensitivity



MINOS Oscillation Mode Sensitivity (Discriminate $n_m \textcircled{R} n_t$ vs. $n_m \textcircled{R} n_{\text{sterile}}$)



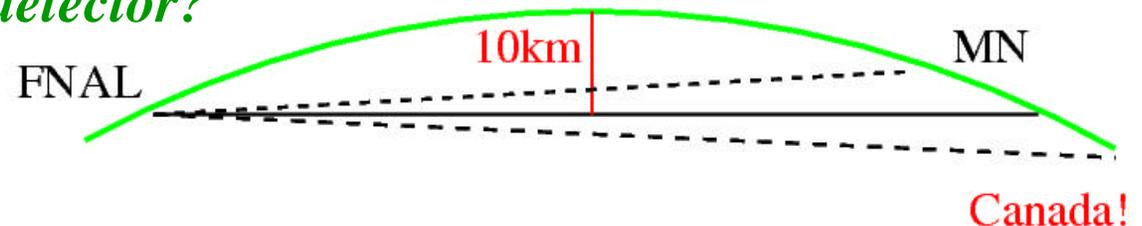
- Use **CC/NC Ratio** to distinguish between oscillations to ν_τ or ν_{sterile}
- For $\nu_\mu \rightarrow \nu_\tau$, CC production of τ 's will look like NC $\sim 80\%$ of the time
CC/NC \rightarrow down
- For $\nu_\mu \rightarrow \nu_{\text{sterile}}$, both CC and NC will be suppressed.
CC/NC stays \sim constant

Possible New Potential for NuMI Program Off-Axis “Minos” Detector

- Goal: Measure $\nu_\mu \rightarrow \nu_e$ at the atmospheric $\Delta m^2 \Rightarrow \sin^2 2\theta_{13}$
(Current CHOOZ Limit: $\sin^2 2\theta_{13} \approx 0.10$ @ 90% CL)
 - Backgrounds and identification are main problems
 - Intrinsic ν_e 's in the beam, NC/CC π^0 production
 - Electron decays of τ 's from $\nu_\mu \rightarrow \nu_\tau$
 - Key is to use energy constraint beam
 - Need a sharp energy distribution
 - Need little high energy tail
 - Answer is the normal NuMI beam to Minos *but*
 - Put your detector offaxis (at ~ 15 mr)

Where does this put the detector?

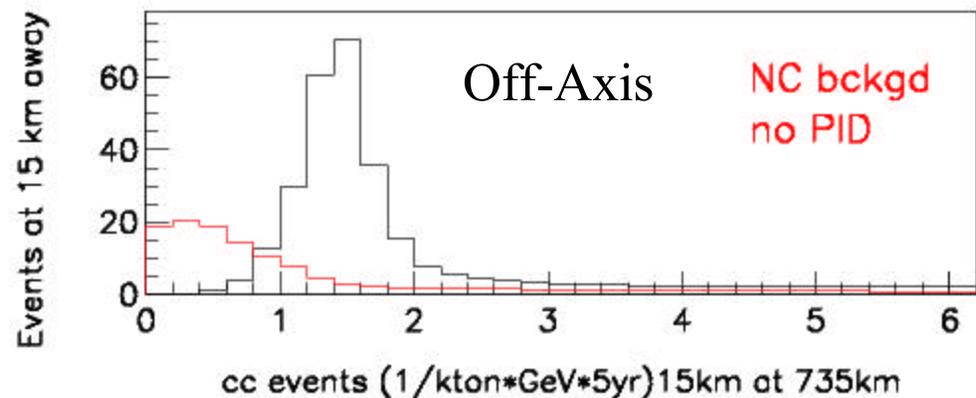
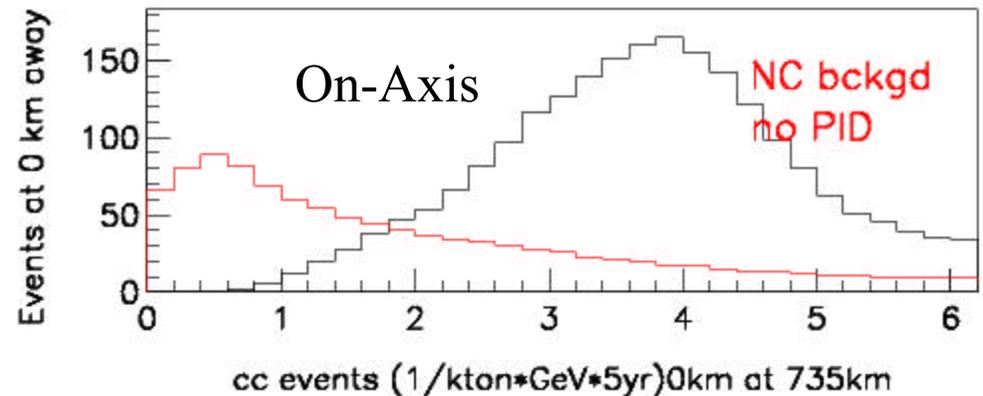
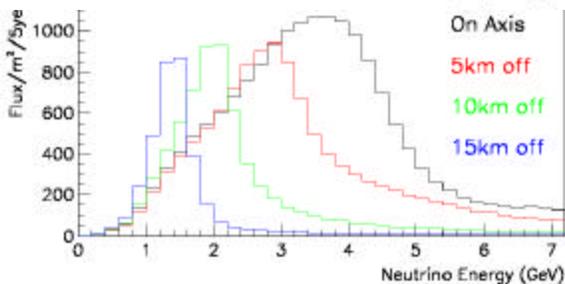
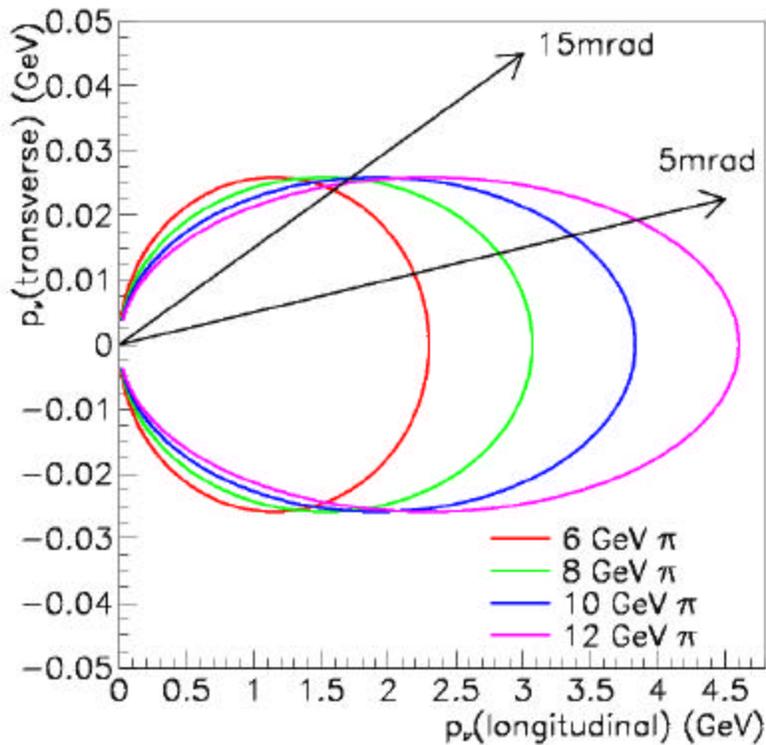
... Maybe Canada!





How/Why Does an Offaxis Beam Work?

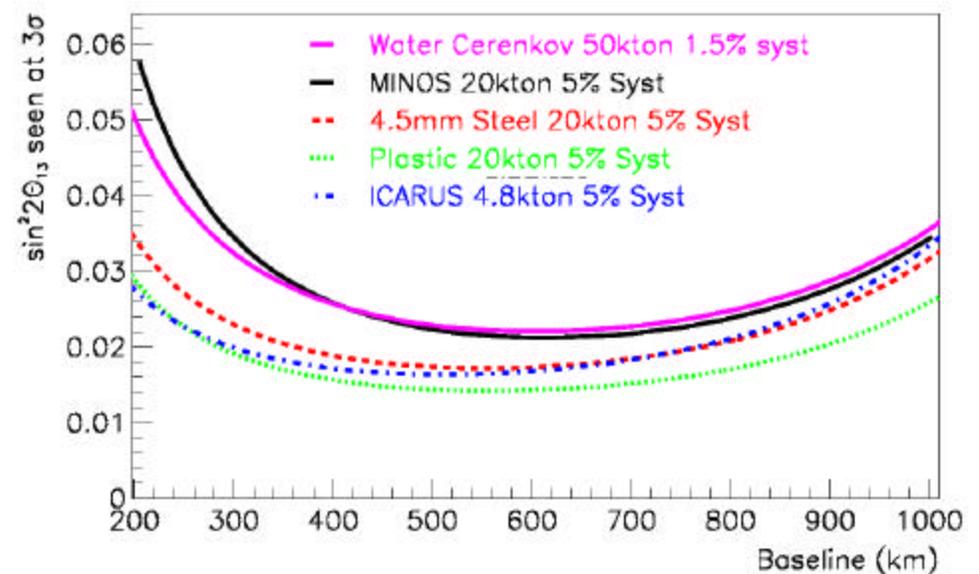
- Neutrinos produced from π -decay
 - Kinematics give mono-energetic beam at 15 mrad
- Energy cuts much more effective in reducing NC background with offaxis beam
 - NC tail from high E_ν on-axis events



Estimates of Sensitivity

- Need to optimize:
 - Baseline
 - Detector
 - Mass and Technology (Signal and Bckgnd efficiency)
- Electron appearance requirements for detector
 - Good segmentation
 - Identify outgoing electrons
 - Good energy resolution
 - Separate ν_e and NC events
 - Particle identification
 - At the 1% or better level

- Study of capabilities of various detector technologies



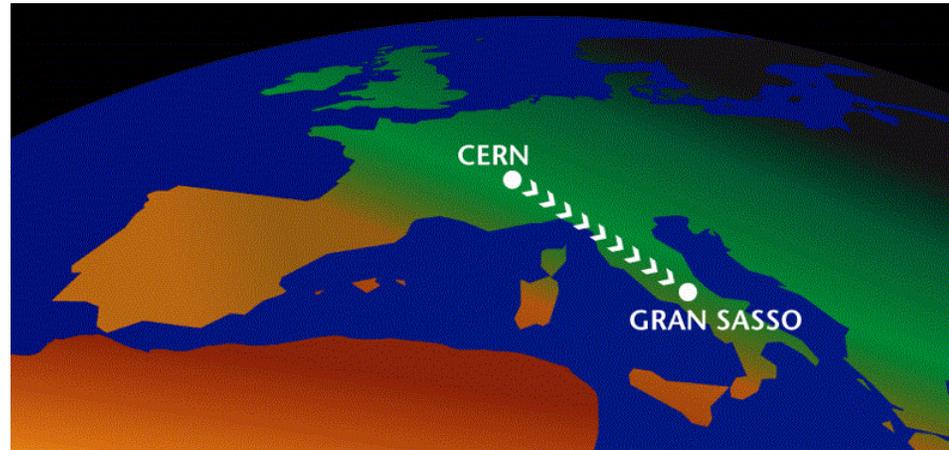
Conclusion:

- With reasonable detector can reach

$$\sin^2 2\theta_{13} \approx 0.02 \text{ at } 3\sigma$$

(about x10 better than CHOOZ)

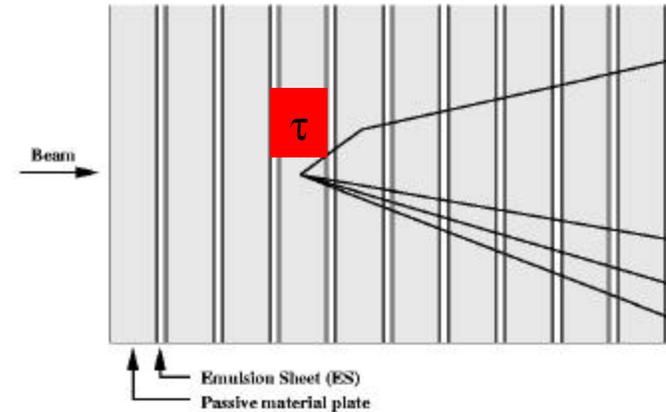
CERN to Gran Sasso n Osc. Program (CNGS)



- CERN has approved a program for a neutrino beam from CERN to Gran Sasso
 - Beam similar to Minos with ν_τ rate factor of two lower
 - Unlikely that a near detector hall would be built
- Emphasis on appearance experiments with ν_τ and ν_e identification
 - ***Opera Experiment***: Emulsion detector
 - ***ICARUS Experiment***: Liquid argon

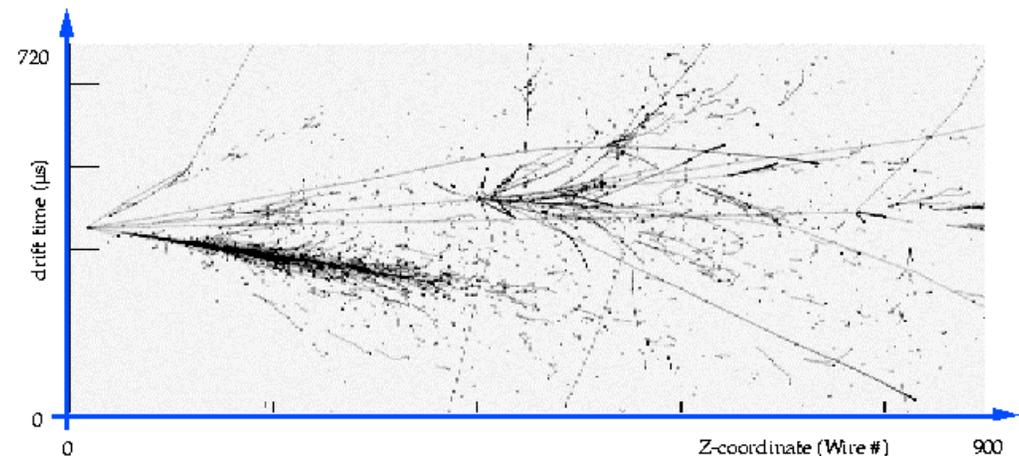
OPERA Hybrid Emulsion Experiment (Oscillation Project with Emulsion-tRacking Apparatus)

- Emulsion bricks interspersed with electronics trackers
 - See τ decay in emulsion
- Goal: 1.5 kton hybrid target
 - $\sim 3,600 \nu_{\mu}$ CC events/yr \times eff.
 - $\sim 45 \nu_{\tau}$ events/yr \times efficiency
 - efficiency: $\sim 10\%$?



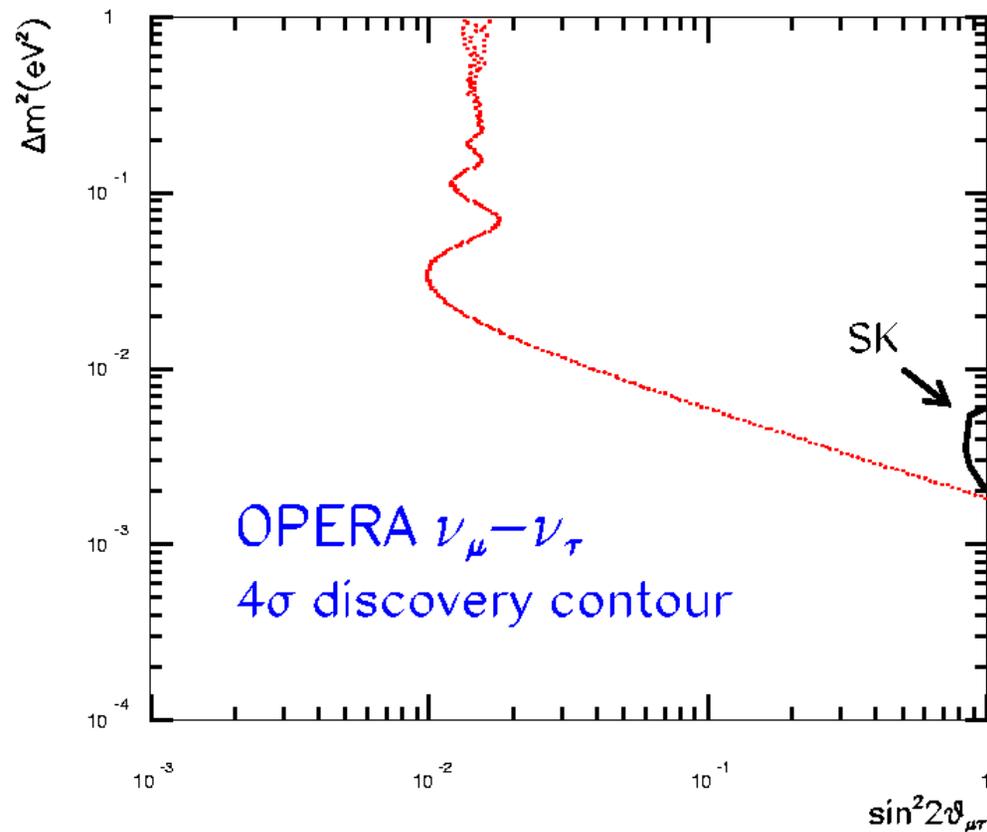
ICARUS Experiment

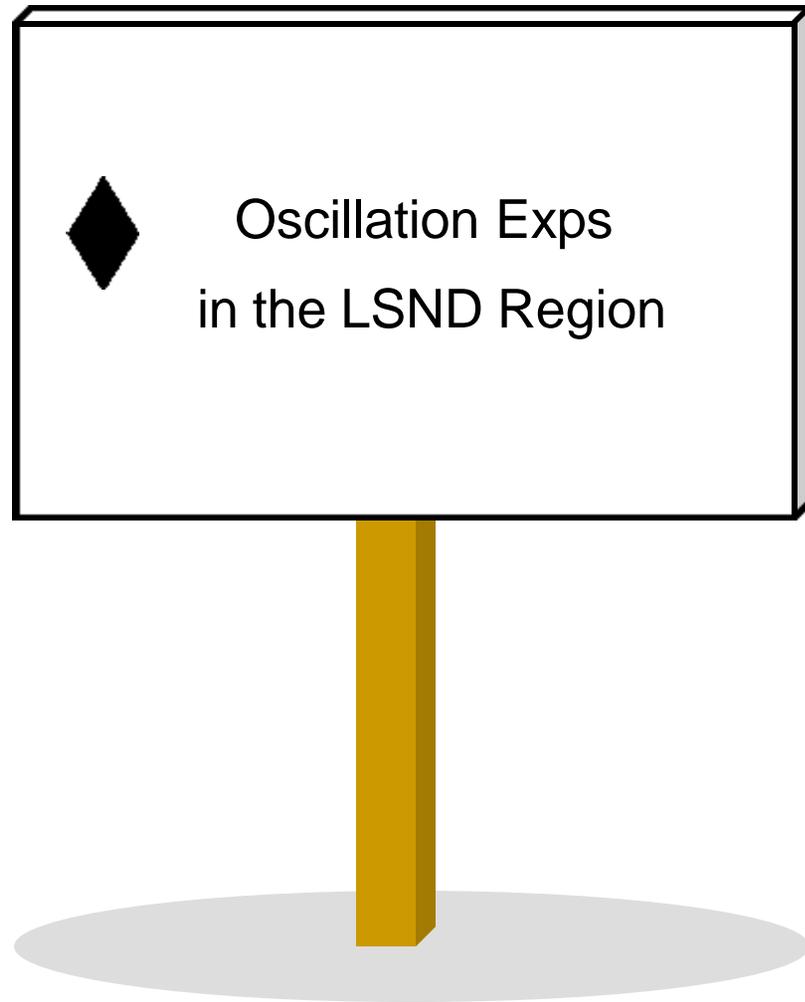
- Use liquid argon calorimeter
 - Liq Ar: 4 @ 1250 = 5000 tons
- Detect and identify all neutrino species



OPERA Sensitivity

- Very low background
 - Can confirm oscillations to ν_τ with a few events
- For five year exposure (2.25×10^{20} pot)
 - $\sim 25 \nu_\mu \rightarrow \nu_\tau$ osc. events @ $\Delta m^2 = 3.5 \times 10^{-3} \text{ eV}^2$
 - ~ 0.5 events background

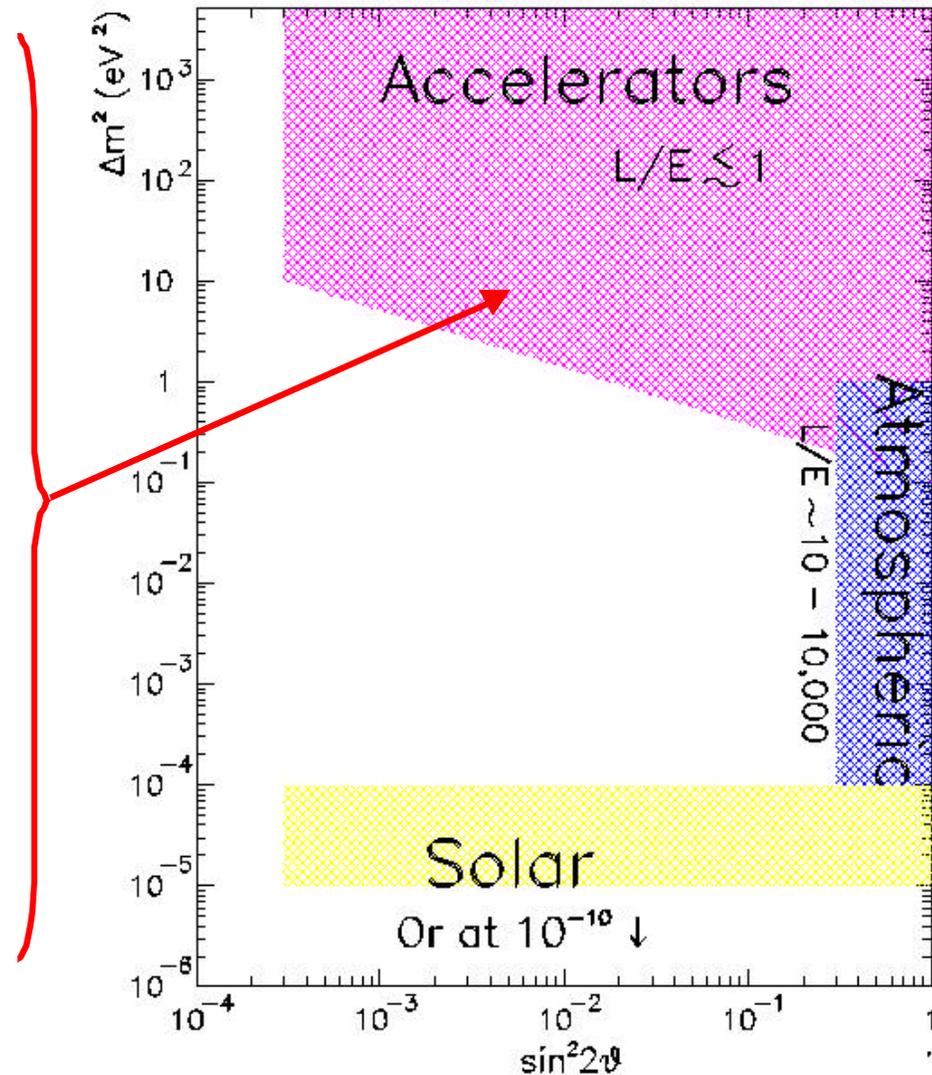




LSND, Karmen, and MiniBooNE

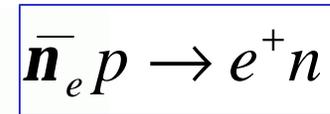
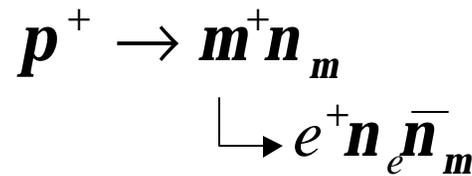
$n_m \textcircled{R} n_e$ at high Dm^2

- LSND (LANCE) sees positive indication of oscillations
 - Final results
- Karmen II (RAL, England) experiment sees no excess and limits the allowed LSND region
 - Almost final results
- MiniBooNE (Fermilab) will make a definitive search for oscillations in this region



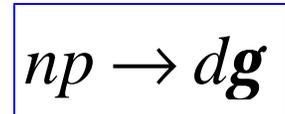
The LSND Experiment (1993-98)

See G. Mills Talk

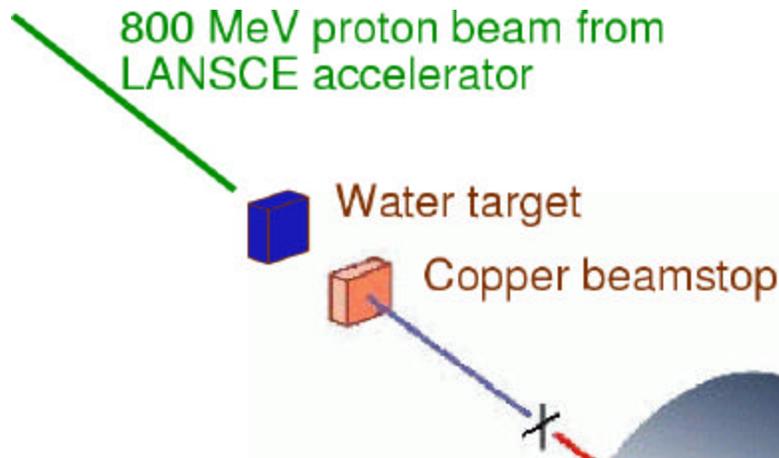


detect prompt e track,
 $20 < E_e < 60$ MeV

neutron capture:



2.2 MeV



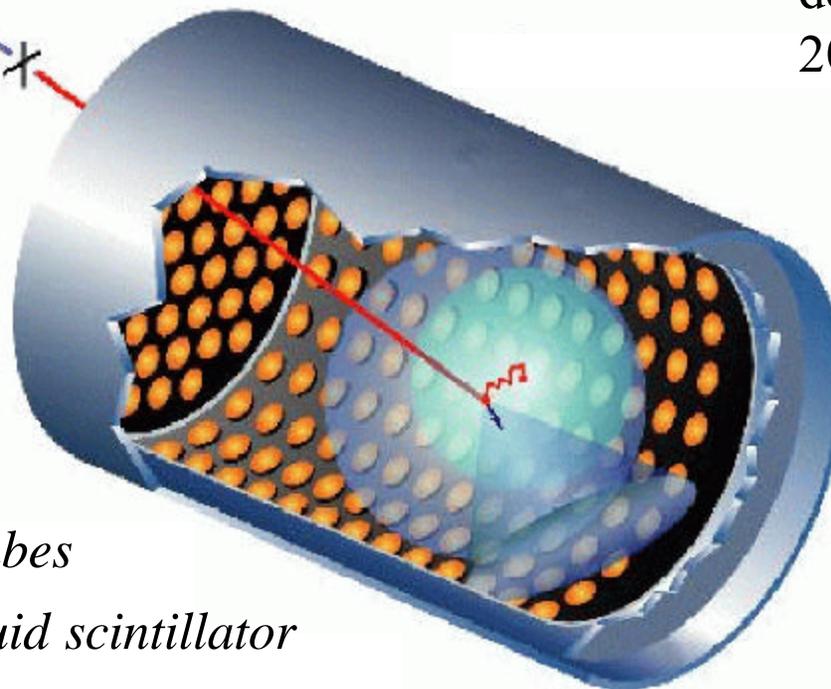
Baseline 30 m

*Neutrino Energy
 20-55 MeV,*

*Nearly 49,000 Coulombs
 of protons on target*

1280 phototubes

167 tons Liquid scintillator

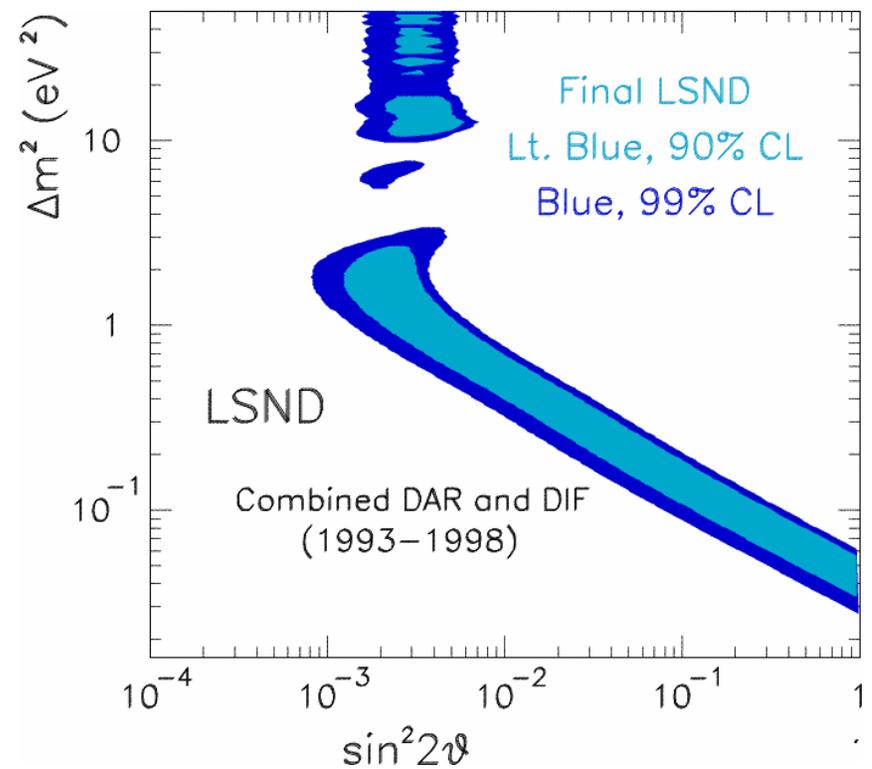
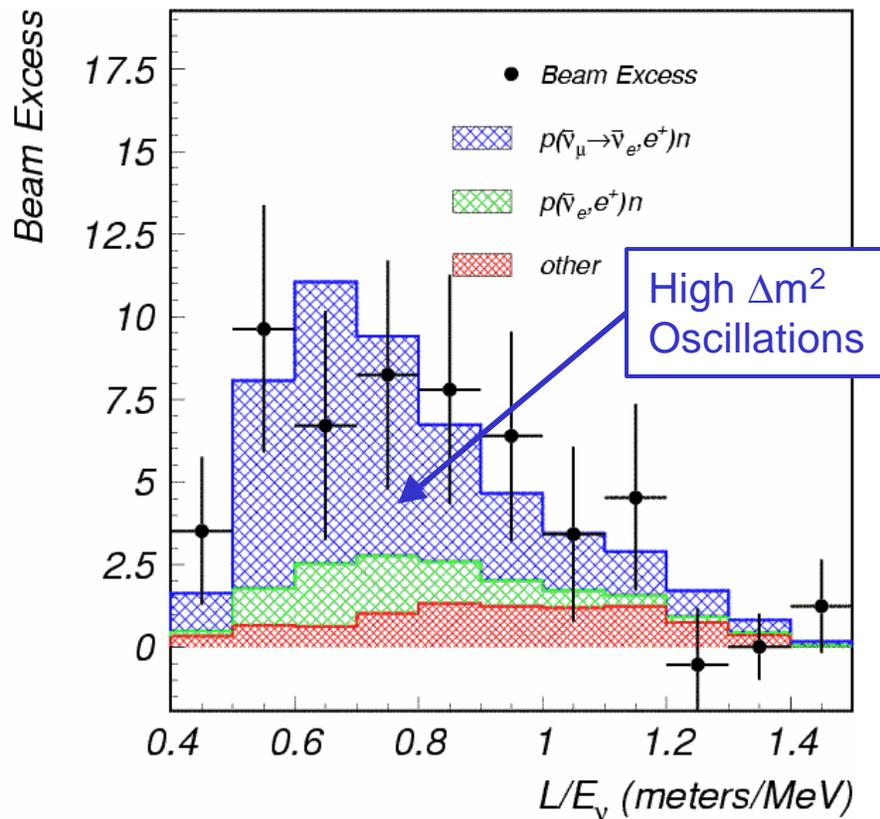


LSND Final Result

LSND sees excess above backgrounds

– Excess: $87.9 \pm 22.4 \pm 6.0$ evts.

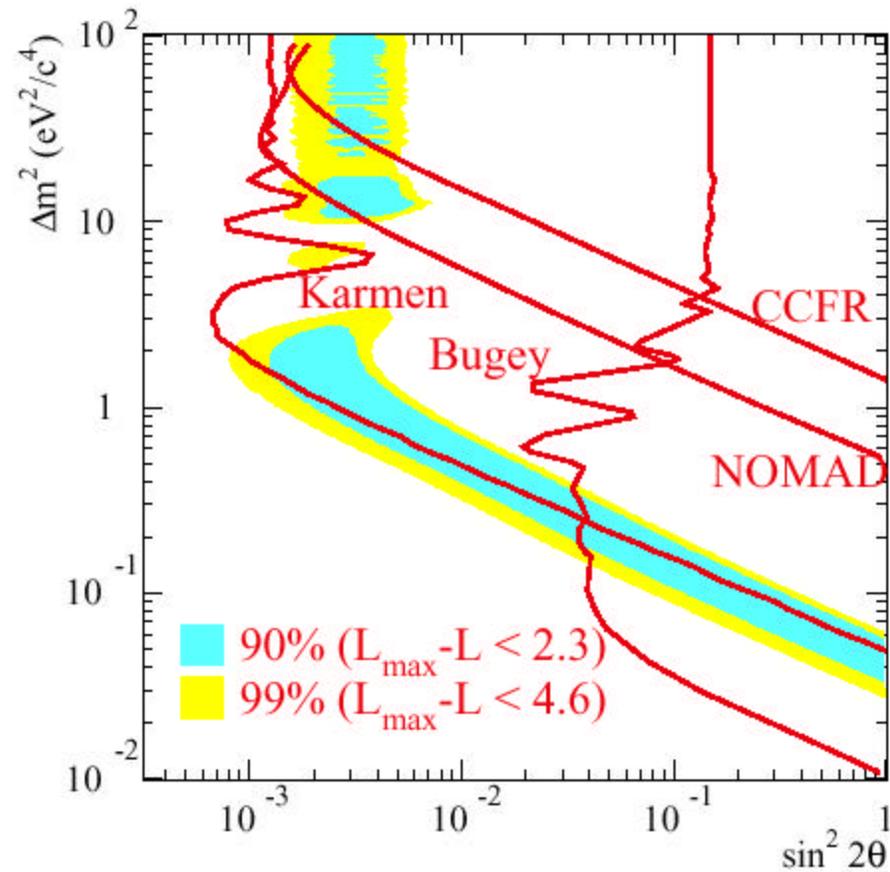
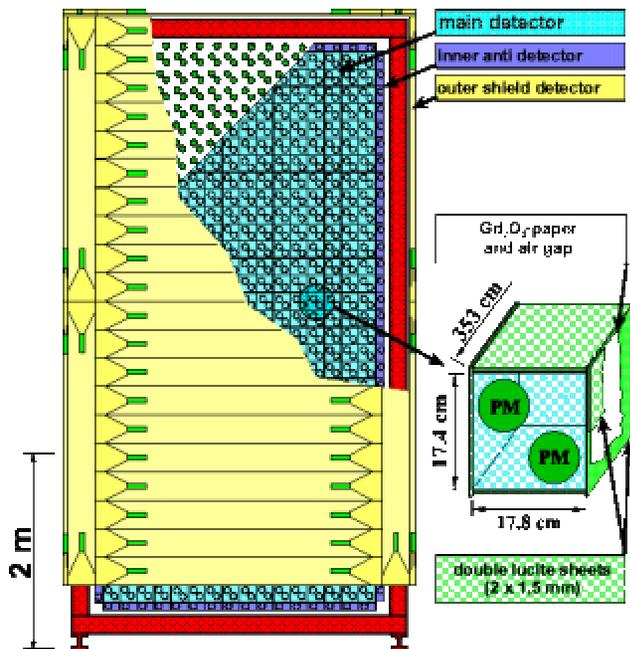
- Corresponding osc. probability: $(0.264 \pm 0.067 \pm 0.045)\%$
- 3.3σ evidence for oscillation.



Karmen II (1997-2001)

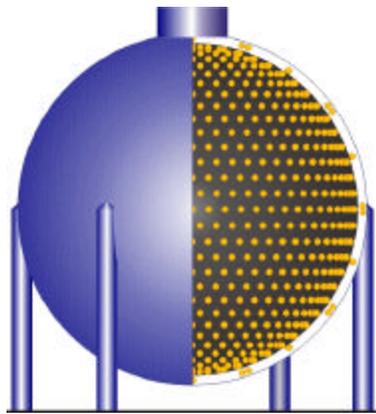
- Pulsed 800 MeV pot (ISIS)
 - DAR beam (90° to target)
 - 17.6 m baseline
- 56 tons of liquid scintillator
 - 512 modules
 - Gd-doped (8 MeV γ)
- $\times 10$ less statistics than LSND (less intensity & size)

- Almost final results
 - 11 events observed
 - 12.3 ± 0.6 events expected

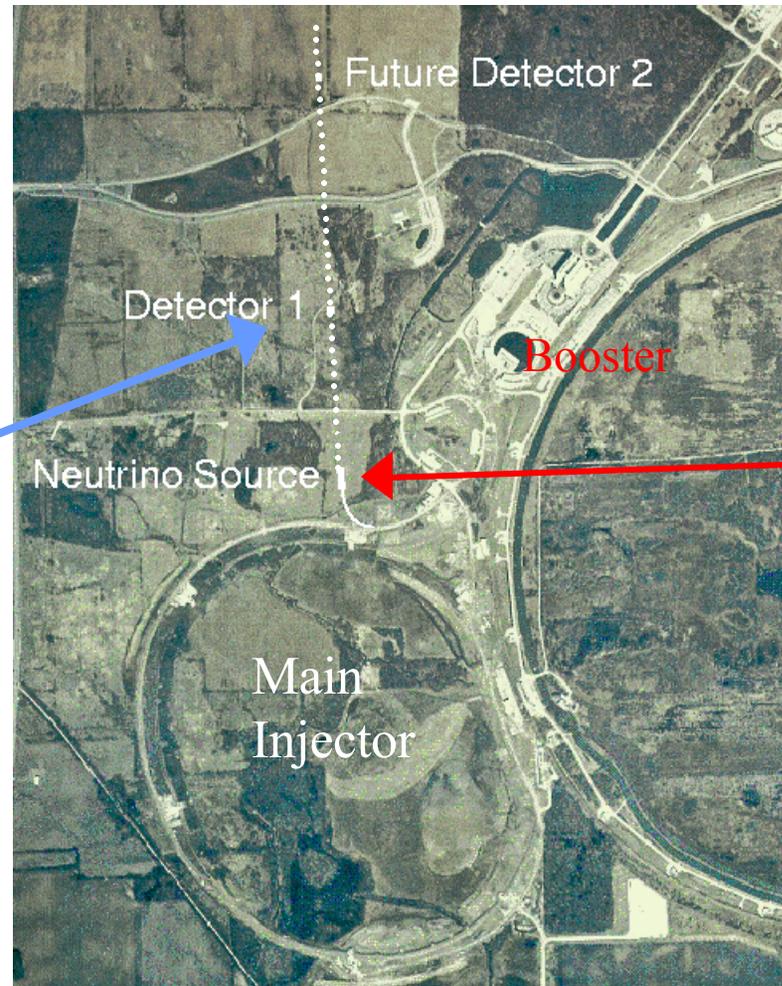


MiniBooNE Experiment

Need definitive study of $n_m \otimes n_e$ at high Dm^2 ... MiniBooNE



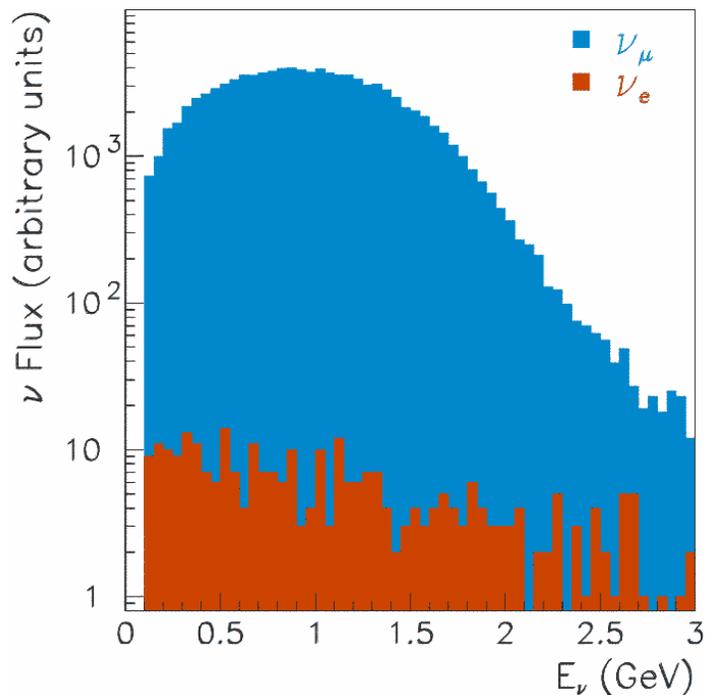
12m sphere filled with mineral oil and 1500 PMTs located 500m from source



Use protons from the 8 GeV booster
 \Rightarrow Neutrino Beam
 $\langle E_\nu \rangle \sim 1 \text{ GeV}$

MiniBooNE Neutrino Flux and Expected Events

The L/E is designed to be a good match to LSND at ~ 1 m/MeV.



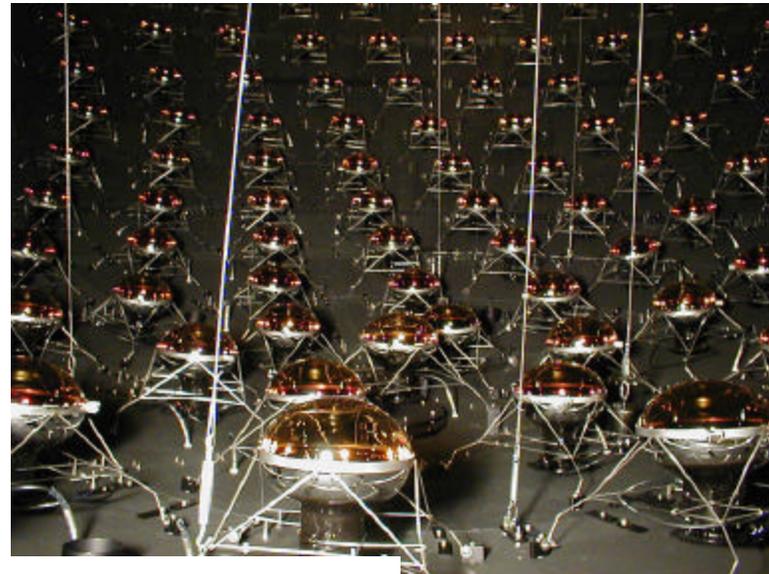
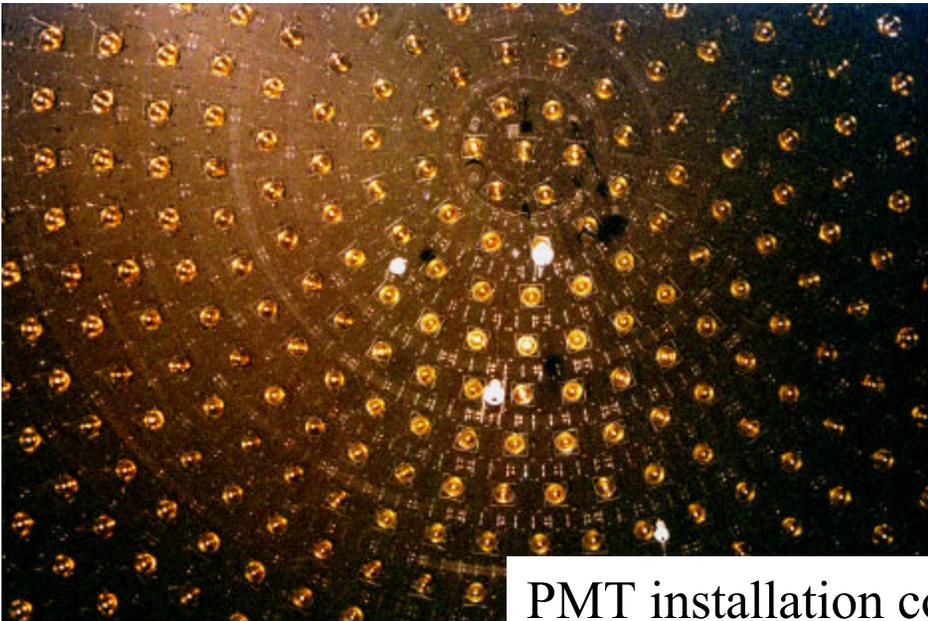
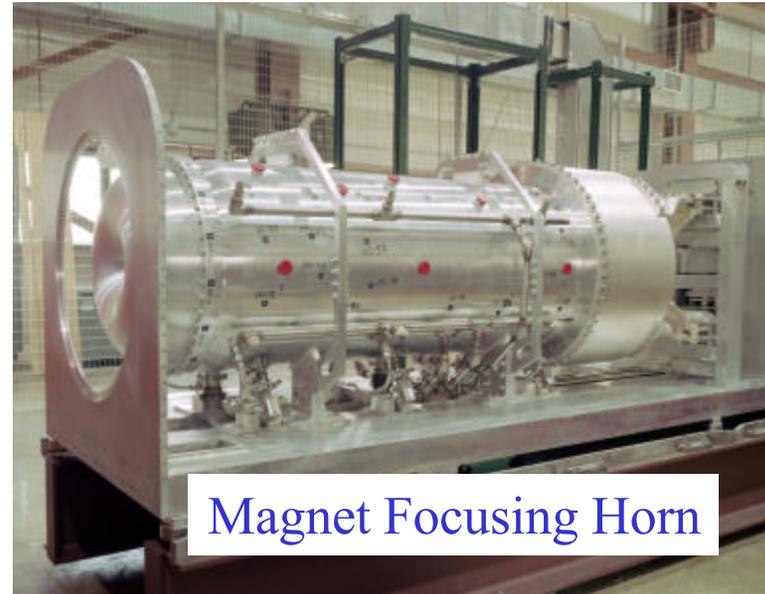
Expected intrinsic ν_e flux is small compared to the ν_μ flux.

Expectation for electron-like events/2yrs

- Intrinsic ν_e background: **1,000 events**
- μ mis-ID background: **500 events**
- π^0 mis-ID background: **500 events**
- **LSND-based $n_m \otimes n_e$: 1,000 events**
- **Backgrounds can be separated from signal**
 - Osc. signal has different energy spectrum than intrinsic ν
 - Experimental determinations of all backgrounds.

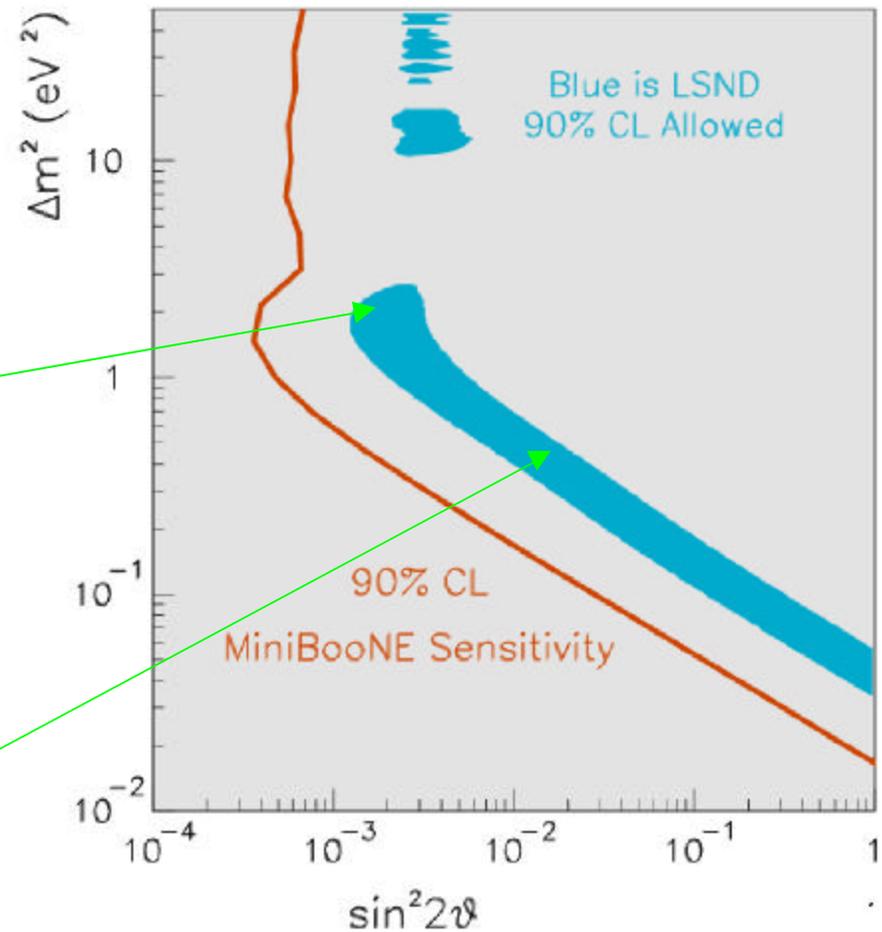
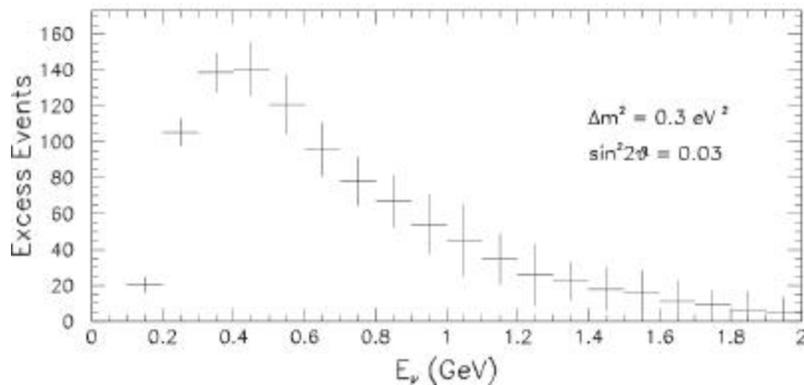
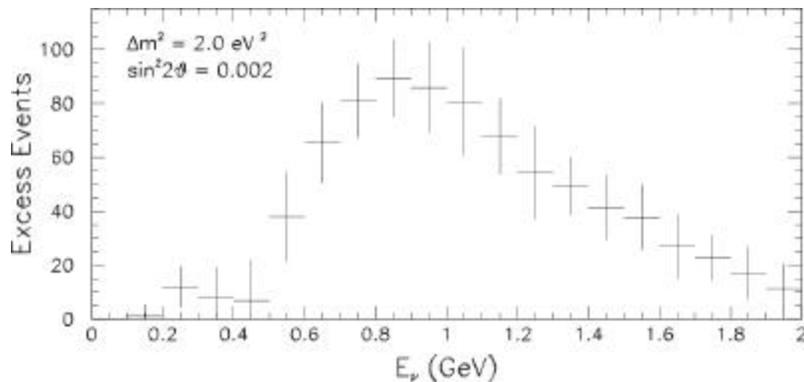
MiniBooNE is about to Start

- Everything on schedule for ***June, 2002 Start***
 - Detector half filled with oil
 - Horn tested (10^7 pulses)
 - Proton extraction ready



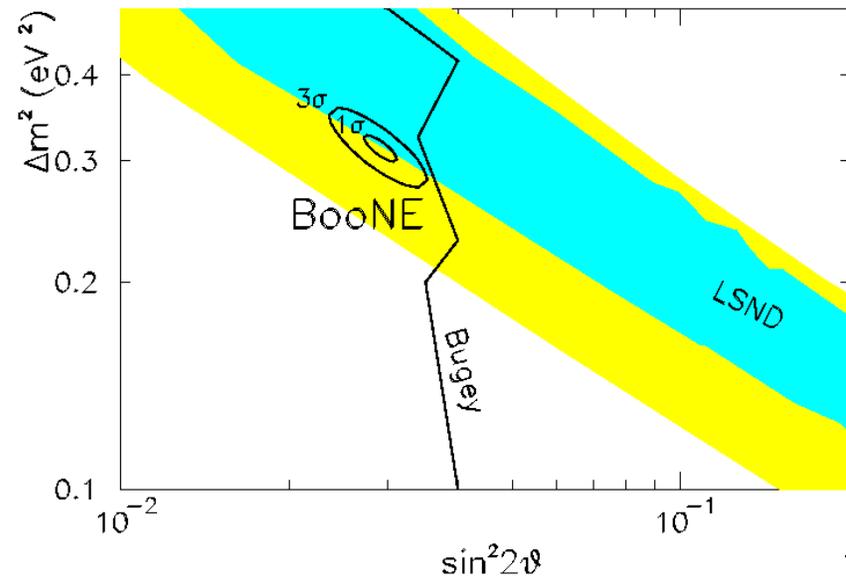
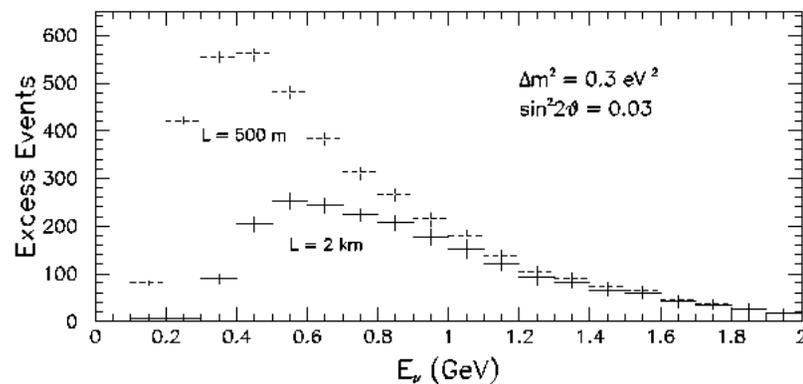
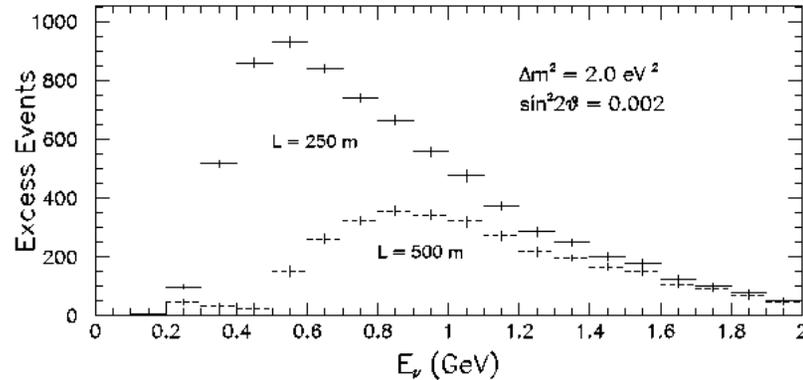
MiniBooNE Sensitivity to LSND

With two years of running MiniBooNE should be able to completely include or exclude the entire LSND signal region.



MiniBooNE $\bar{\nu}$ BooNE

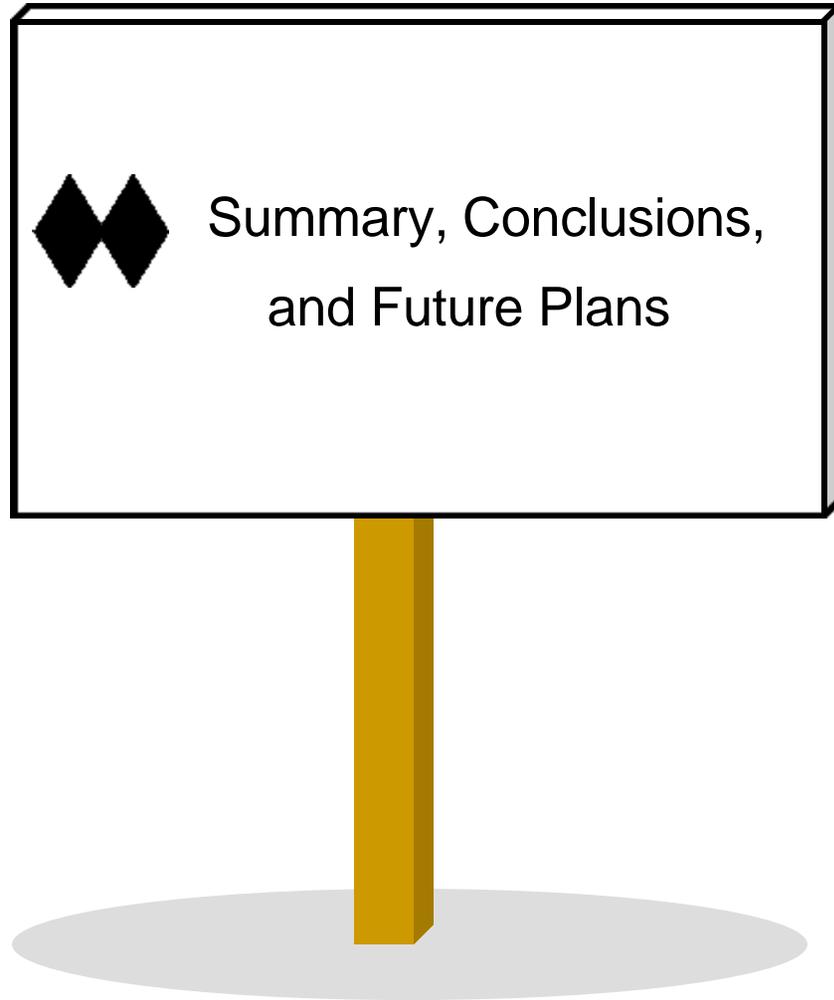
- If signal is observed in MiniBooNE, then add second detector at appropriate distance $\bar{\nu}$ **Two detector BooNE experiment**



Measure:

$$\Delta m^2 \text{ to } \pm 0.014 \text{ eV}^2$$

$$\sin^2 2\theta \text{ to } \pm 0.002$$



Summary, Conclusions,
and Future Plans

Summary

Expectations for the Next ~5 years

- LSND Δm^2
 - Definitive determination if osc.
 - Measure $\Delta m^2/\sin^2 2\theta$ to 5-10%
 - If positive \Rightarrow New round of experiments: ν_μ and $e^- \rightarrow \nu_\tau$

- Atmospheric Δm^2
 - Know if $\nu_\mu \rightarrow \nu_\tau$ or ν_s
 - Measure $\Delta m^2/\sin^2 2\theta$ to 10% if $\Delta m^2 > 2 \times 10^{-3} \text{eV}^2$
 - Maybe see $\nu_\mu \rightarrow \nu_e$

- Solar Δm^2
 - Restrictions to one solar solution
 - Know if $\nu_e \rightarrow \nu_{\mu,\tau}$ or ν_s

\ddot{U} *Results from MiniBooNE*

\ddot{U} *Results from K2K, MINOS, CNGS*

\ddot{U} *MINOS Off-axis?*

\ddot{U} *Results from Kamland, Borexino, SNO*

Next Step Driven by Near Term Results

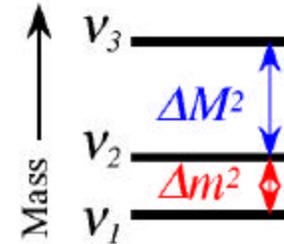
- If MiniBooNE sees $\nu_\mu \rightarrow \nu_e$ oscillations then
 - Investigate the oscillation phenomenology at high Δm^2
 - Need at least 4 mass eigenstates ... **Sterile Neutrinos!**
What is the pattern ... 2+2 , 3+1
- If MiniBooNE refutes LSND then Minos/CNGS
 - Push to measure oscillation parameters with best precision
 - Search/measure $\nu_\mu \rightarrow \nu_e$ at the atmospheric Δm^2
- If MINOS/CNGS fail to measure $\nu_\mu \rightarrow \nu_e$ then
 - Design new exp's to measure θ_{13} (also sign of Δm^2)
 - Long-baseline “Superbeams” or ν -factory sources will be needed
- If parameters are reasonable, then move to a CP violation experiment
 - Experiment must be sensitive to
 - Δm^2_{23} and $\Delta m^2_{12} \Rightarrow$ requires the LMA
 - mixing at the θ_{13} level \Rightarrow requires θ_{13} large enough to see

Scenario: MiniBooNE Confirms LSND

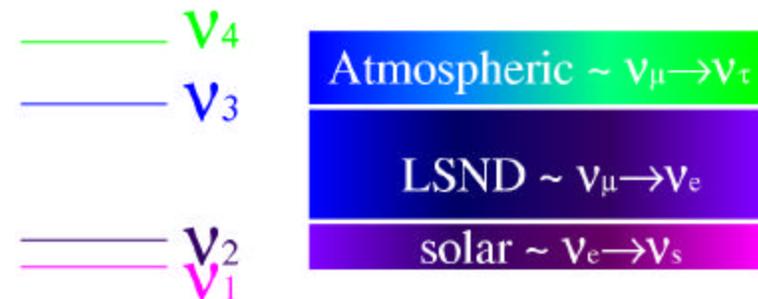
Three $\Delta m^2_{\text{solar}}$, Δm^2_{atm} , Δm^2_{LSND}

Possible explanations

- Atmospheric result is a mixture of $\Delta m^2_{\text{solar}}$ and Δm^2_{LSND}
 - Difficult to fit all data with this model (hep-ph/000416)

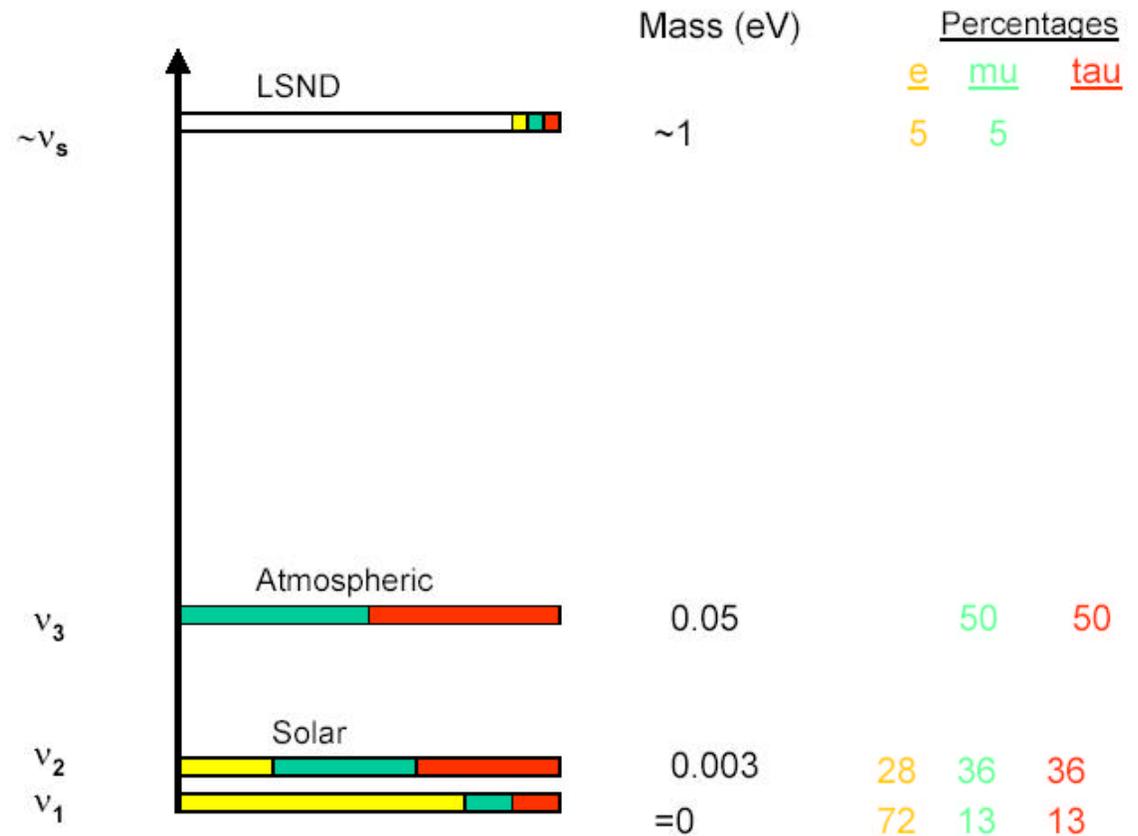


- Introduce a 4th (or more) sterile neutrino
 - **2+2 Model:**
 - Atmospheric or Solar (or both) have oscillation fractions to ν_s such that $f_{\text{Solar}} + f_{\text{Atmos}} = 1$
 - Super-K Atmospheric:**
 $f_{\text{Atmos}} < 0.25$ @ 90%CL
 - SNO + Super-K Solar:**
 $f_{\text{Solar}} < 0.50$ @ 90%CL
 - Model still possible but at the edge (Extension: 3active +3sterile model can work)



3+1 Model

- **3+1 Model:**
 - Atmospheric: $\nu_\mu \rightarrow \nu_\tau$
 - Solar: LMA $\nu_e \rightarrow \nu_{\mu,\tau}$
 - LSND: $\nu_\mu \rightarrow \nu_s \rightarrow \nu_e$
- Solar oscillations are to a 50%/50% mixture of ν_μ and ν_τ
- LSND $\nu_\mu \rightarrow \nu_e$ oscillations are through high mass, mainly ν_s state with small admixture of ν_μ and ν_e



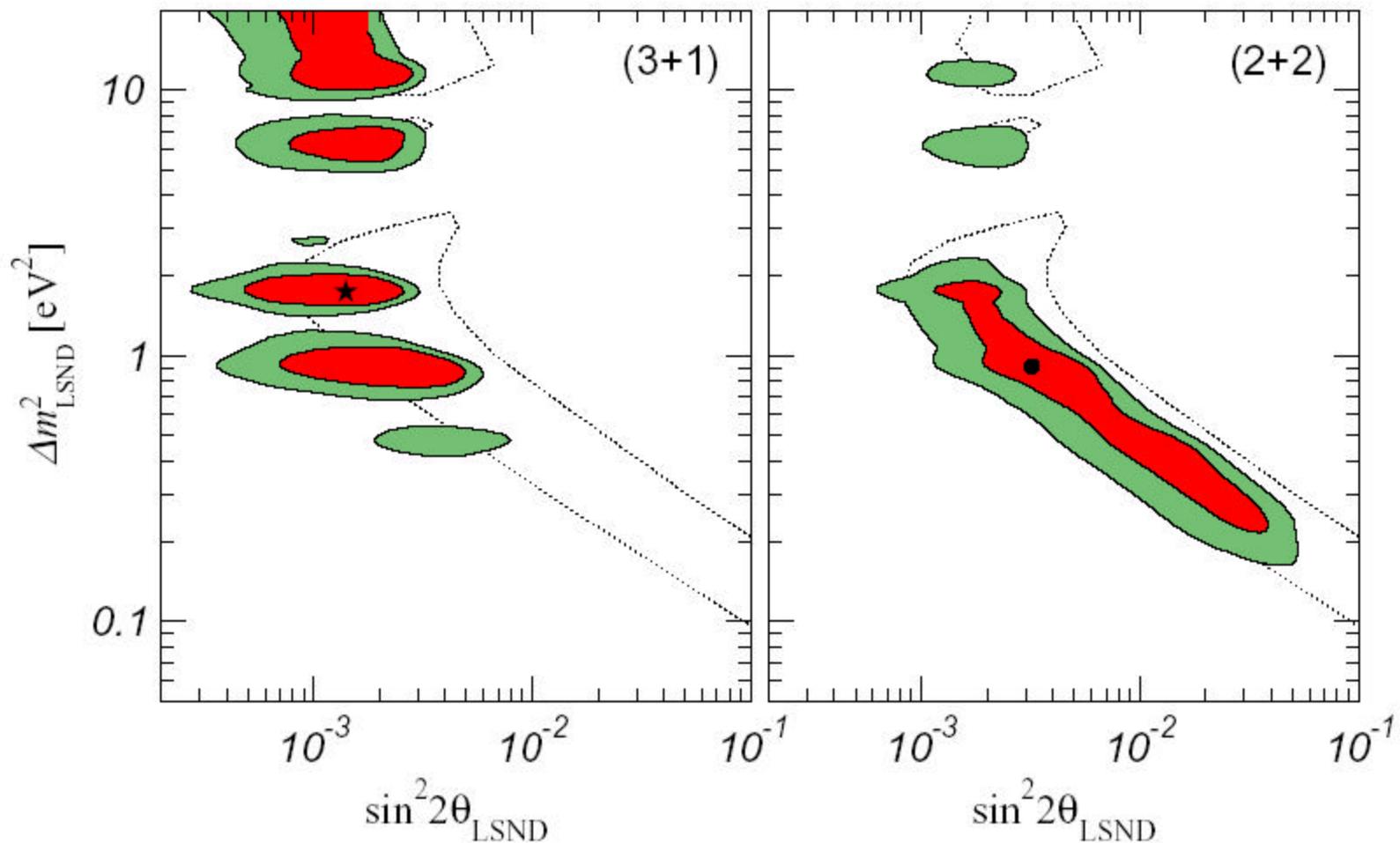
$$\nu_e = 0.85\nu_1 + 0.51\nu_2$$

$$\nu_\mu = -0.36\nu_1 + 0.60\nu_2 + 0.71\nu_3$$

$$\nu_\tau = 0.36\nu_1 - 0.60\nu_2 + 0.71\nu_3$$

Global Analysis

- Global analysis: **Solar, Atmospheric, LSND/Karmen, Reactor**
(Maltoni, Schwetz, and Valle hep-ph0112103)

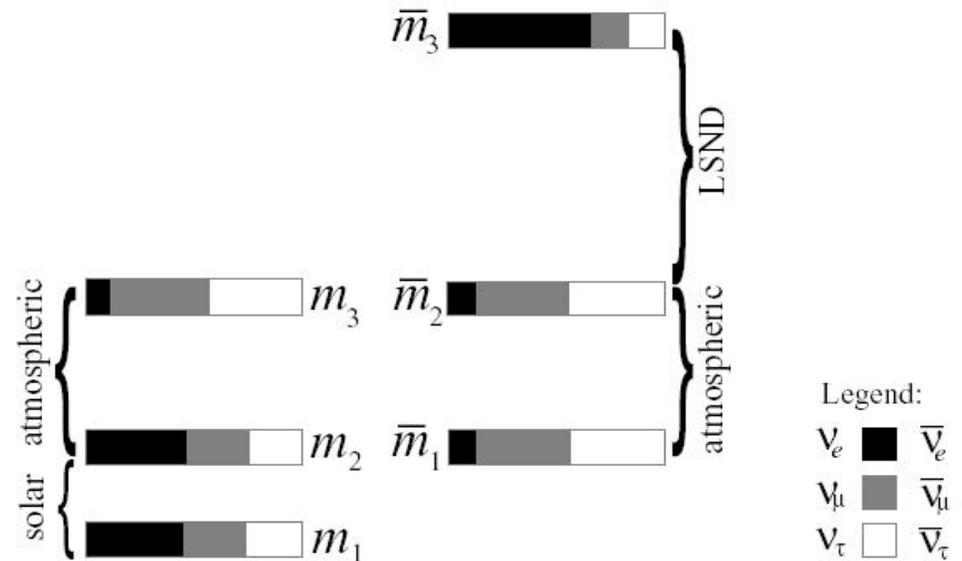


CPT Violation

- If CPT is violated the
 $Mass(\mathbf{n}_i) \neq Mass(\bar{\mathbf{n}}_i)$

⇒ Now LSND sees $\bar{\mathbf{n}}_m \rightarrow \bar{\mathbf{n}}_e$
 but Solar sees $\mathbf{n}_e \rightarrow \mathbf{n}_m$

- Model accommodates solar, atmospheric, and LSND without sterile neutrinos
 - Just allow the antineutrino Δm^2 to be bigger than the neutrino



(Barenboim, Borissov, Lykken, Smirnov, Murayama, Yanagida; hep-ph 0201080)

- Leptogenesis
 - After the EW phase transition since the neutrinos are lighter than antineutrinos
 $number(\mathbf{n}) > number(\bar{\mathbf{n}})$
 - B-L processes then convert neutrino excess to baryon excess.
 - Sign and magnitude ~correct to generate baryon asymmetry in the universe.

Scenario: MiniBooNE Refutes LSND

- 3-generation Mixing

Atmospheric: θ_{23}

Solar: θ_{12}

$$\begin{pmatrix} \mathbf{n}_e \\ \mathbf{n}_m \\ \mathbf{n}_t \end{pmatrix} = \begin{pmatrix} c_{12}c_{13} & s_{12}c_{13} & s_{13}e^{-id} \\ -s_{12}c_{23} - c_{12}s_{23}s_{13}e^{id} & e_{12}c_{23} - s_{12}s_{23}s_{13}e^{id} & s_{23}c_{13} \\ s_{12}s_{23} - c_{12}c_{23}s_{13}e^{id} & -c_{12}s_{23} - s_{12}c_{23}s_{13}e^{id} & c_{23}c_{13} \end{pmatrix} \begin{pmatrix} \mathbf{n}_1 \\ \mathbf{n}_2 \\ \mathbf{n}_3 \end{pmatrix}$$

Need to measure:

Sign of Δm_{23}^2

\mathbb{CP} phase δ

$\theta_{13} (\nu_e \rightarrow \nu_\mu)$

- Measurements of $\mathbf{n}_m \rightarrow \mathbf{n}_e$ and $\bar{\mathbf{n}}_m \rightarrow \bar{\mathbf{n}}_e$ yields \mathbf{q}_{13} and \mathbf{d}
 - θ_{13} key parameter for osc. phenomenology since θ_{12} and θ_{23} are both large
 - Determines whether CP violation is accessible

High Intensity Conventional Beam As Next Step “Superbeams”

- Need high intensity proton source
 - Upgraded FNAL/AGS booster, JHF, new Proton Drivers (FNAL/CERN)
- Need to construct high intensity neutrino beam pointed at long-baseline detector about 3000 km away.
 - Reduce background
 - Sensitivity to matter effects
- Need a massive (30 - 50 kton) detector
 - Need good backgrnd rejection (10^{-3}) (Liquid argon may be best)

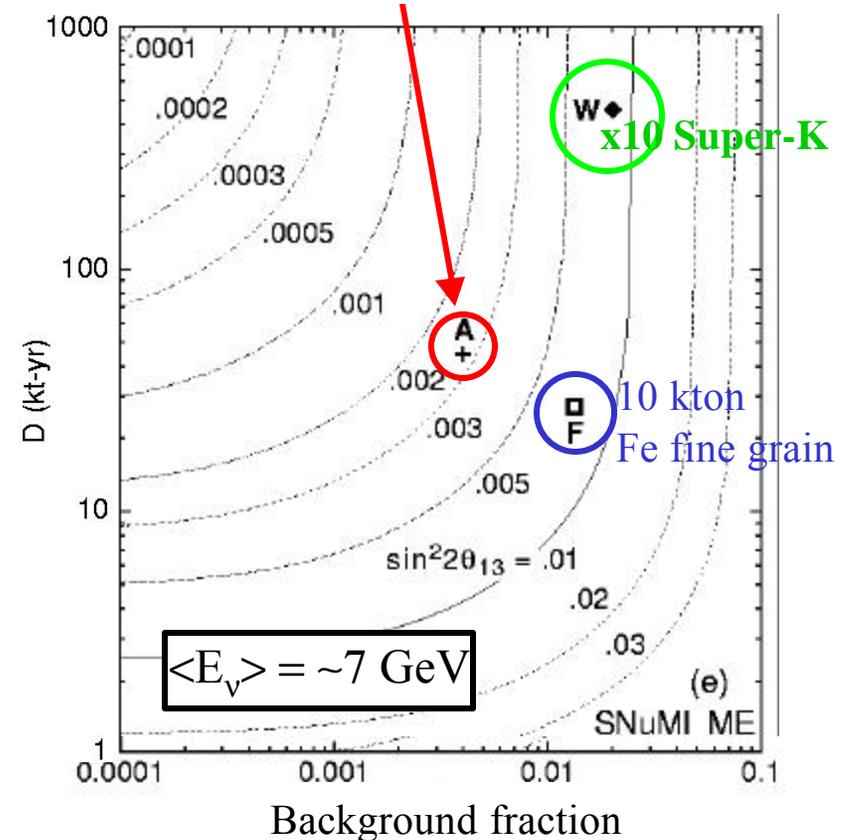
$\sin^2 2\theta_{13}$ at 3σ vs. Size & Bkgnd

Super ($\times 4$) NuMI beam for 3yrs

30 kton Liq. Argon Detector

Baseline = 2900 km

Reach $\sin^2 2\theta_{13} \approx 0.003$ at 3σ



Possible Future Step: Muon Storage Ring n-Factory

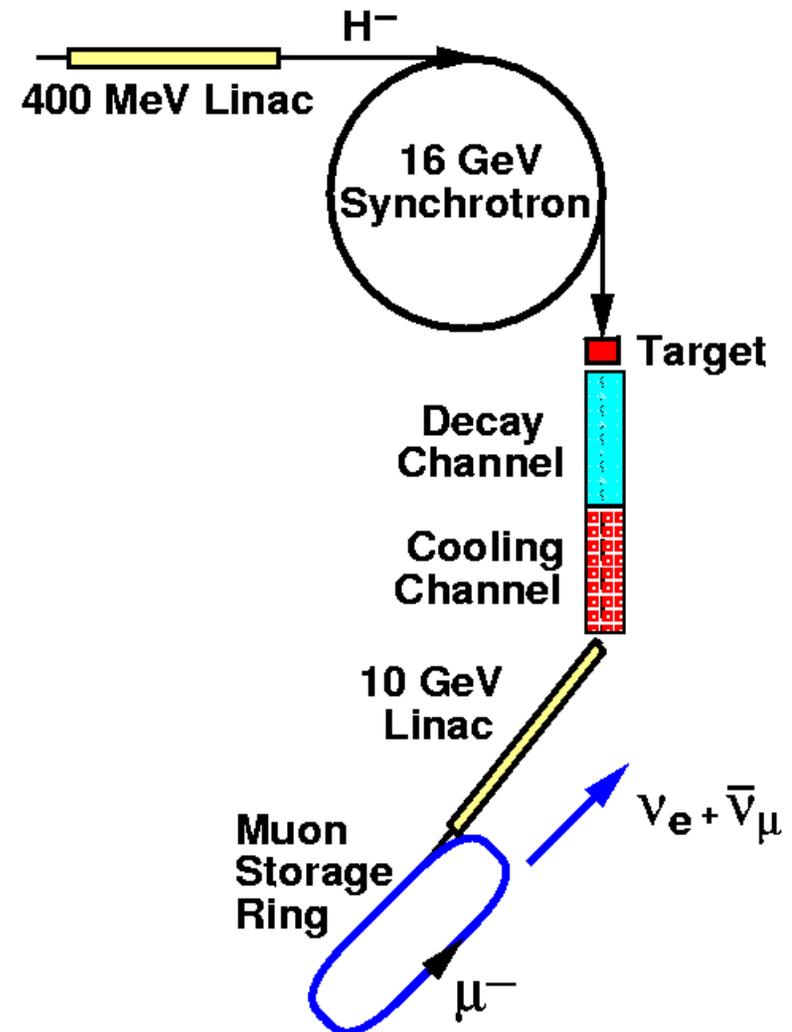
- Muon storage ring
 - Provides a super intense neutrino beam with a wide range of energies.
 - High intensity, mixed beam allows investigation of all mixings
($n_e \text{ @ } n_{m \text{ or } t}$)

- Flavor composition/energy selectable and well understood:

$$m^- \rightarrow e^- + n_m + \bar{n}_e \quad \text{or}$$

$$m^+ \rightarrow e^+ + \bar{n}_m + n_e$$

- Highly collimated beam
 - Very long baseline experiments possible
i.e. Fermilab to California

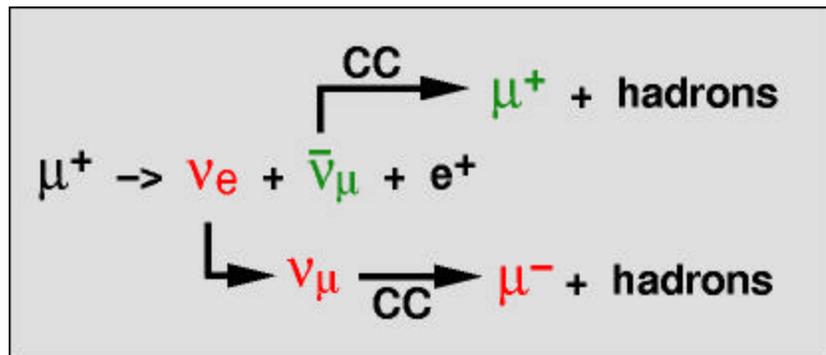


$\nu_e \leftrightarrow \nu_\mu$ Oscillation Measurements at a ν -Factory

- For the atmospheric Δm^2 region, use $\nu_e \rightarrow \nu_\mu$ to determine $\sin^2 2\theta_{13}$

$$P(\nu_e \rightarrow \nu_\mu) = \sin^2 \theta_{23} \sin^2 2\theta_{13} \sin^2 \left(1.27 \Delta m_{32}^2 L / E_\nu \right)$$

- By using $\nu_e \rightarrow \nu_\mu$, signal becomes a search for wrong-sign muons which allows good sensitivity to low $\sin^2 2\theta_{13}$



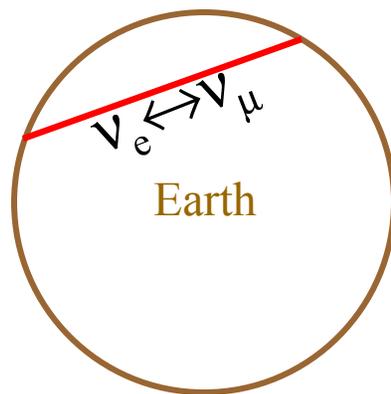
Background is low ($\text{few} \times 10^{-4}$)

- Can reach $\sin^2 2\theta_{13} \approx 0.001$ for 2×10^{20} μ -decay

Matter (and ~~CP~~) Effects for $\nu_e \leftrightarrow \nu_\mu$

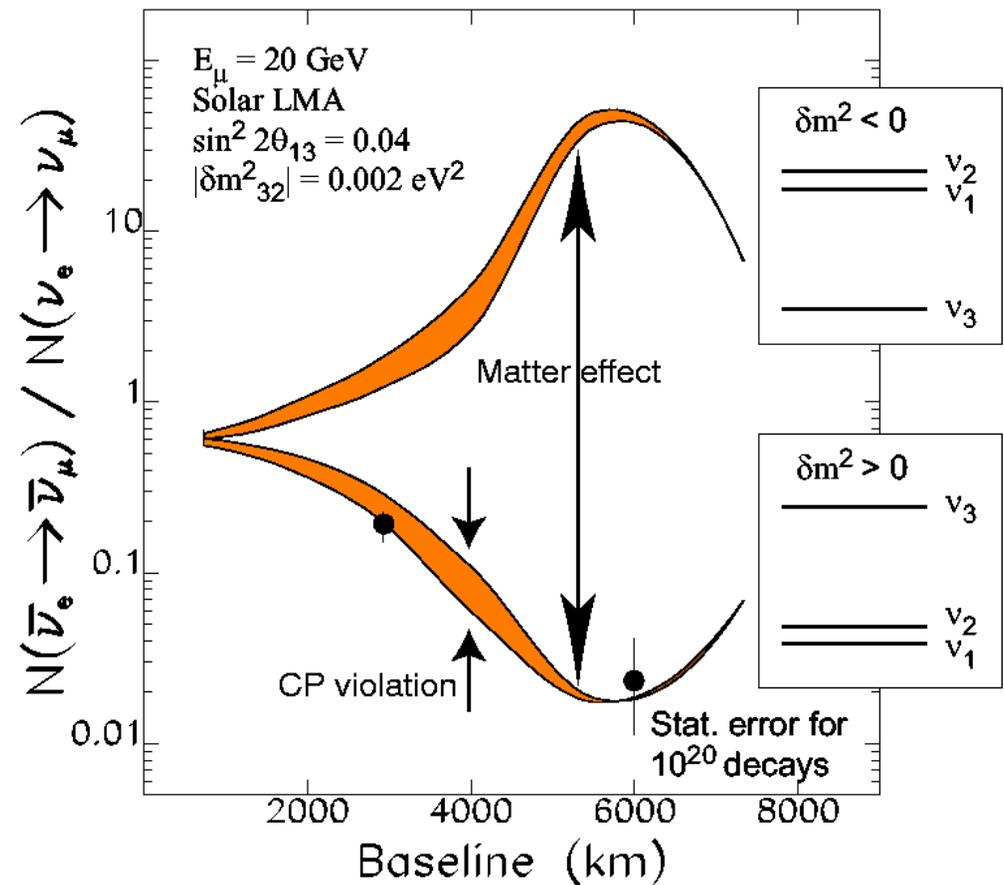
- For long baseline experiments, matter effects change the oscillation formula:

- $\nu_e e \rightarrow \nu_e e$ NC and CC
- $\nu_\mu e \rightarrow \nu_\mu e$ NC only

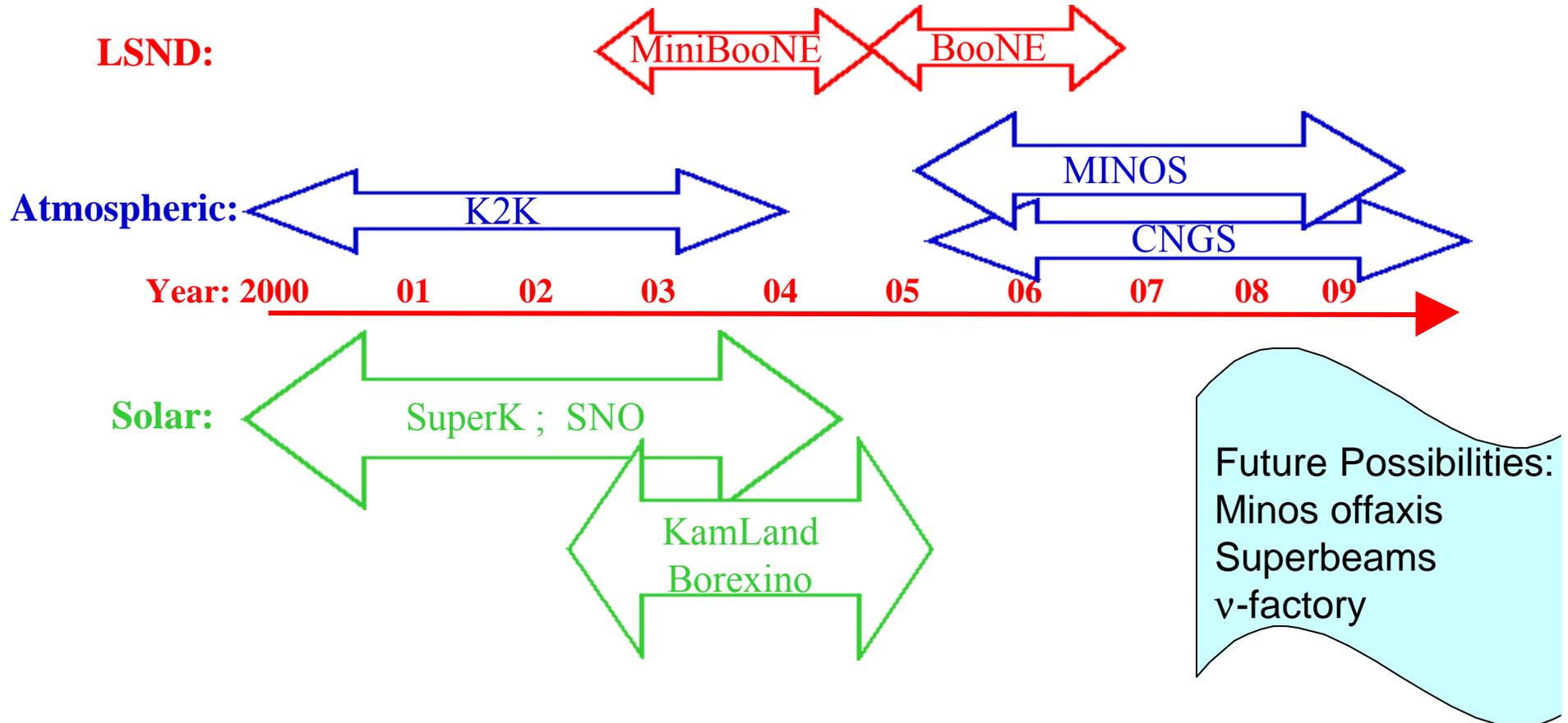


- Oscillation probability is modified depending on sign of $\Delta m^2 = m_3^2 - m_2^2$
 - Measure sign of Δm_{32}^2 to determine if $m_3^2 > m_2^2$

Wrong-Sign Muon Measurements

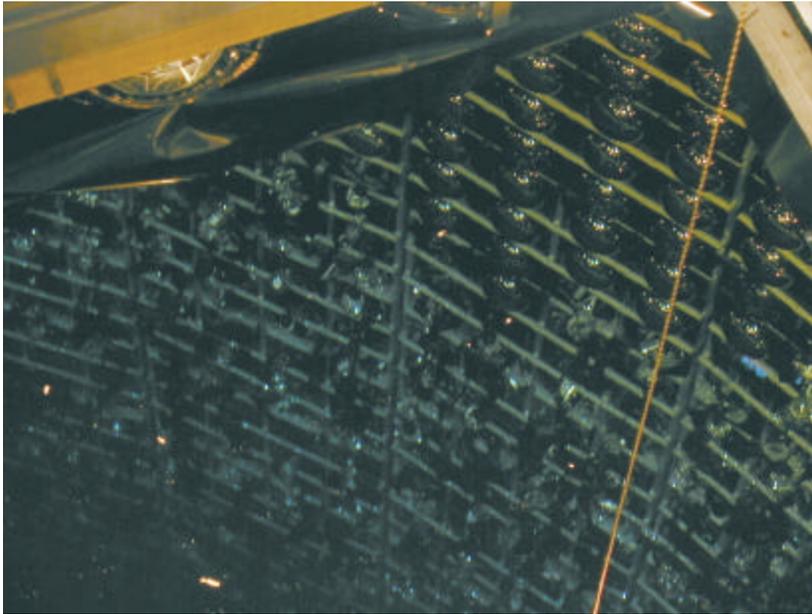


Oscillation Experiment Timeline



Exciting Times for Neutrino Experimentation over the next decade !!

Super-K Accident



- On Nov. 12, after refilling Super-K to the 80% level
 - Chain reaction happened started by the implosion of one tube at the bottom of the tank.

6777 (out of 11146) 20-inch tubes destroyed

1149 (out of 1849) 8-inch veto tubes destroyed

- Developed methods to stop future chain reaction
 - Plan to replace tubes for 50% coverage and restart K2K in January, 2003
 - Detector will be fully repaired for running with JHF beam (Take 3 to 4 years & \$30M)

