ANTINEUTRINO NEUTRAL CURRENT INTERACTONS IN MINIBOONE

by

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Abstract

This dissertation reports the antineutrino-nucleus neutral current elastic scattering cross section on CH$_2$ measured by the MiniBooNE experiment located in Batavia, IL. The data set consists of 60,605 events passing the selection cuts corresponding to $10.1 \times 10^{20}$ POT, which represents the world’s largest sample of antineutrino neutral current elastic scattering events. The final sample is more than one order of magnitude larger than the previous antineutrino NCE scattering cross section measurement reported by the BNL E734 experiment. The measurement presented in this dissertation also spans a wider range in $Q^2$, including the low-$Q^2$ regime where the cross section rollover is clearly visible.

A $\chi^2$-based minimization was performed to determine the best value of the axial mass, $M_A$ and the Pauli blocking scaling function, $\kappa$ that matches the antineutrino NCE scattering data. However, the best fit values of $M_A=1.29$ GeV and $\kappa=1.026$ still give a relatively poor $\chi^2$, which suggests that the underlying nuclear model (based largely on the relativistic Fermi gas model) may not be an accurate representation for this particular interaction.

Additionally, we present a measurement of the antineutrino/neutrino-nucleus NCE scattering cross section ratio. The neutrino mode NCE sample used in this study, corresponding to $6.4 \times 10^{20}$ POT, is also the world’s largest sample (also by an order of magnitude). We have demonstrated that the ratio measurement is robust, as most of the correlated errors cancel, as expected. Furthermore, this ratio also proves to be rather insensitive to variations in the axial mass and the Pauli blocking parameter. This is the first time that this ratio has been experimentally reported. We believe this measurement will aid the theoretical physics community to test various model predictions of neutrino-nucleon/nucleus interactions.
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<tbody>
<tr>
<td>ADC</td>
<td>Analog-to-digital converter</td>
</tr>
<tr>
<td>AGS</td>
<td>Alternating Gradient Synchrotron</td>
</tr>
<tr>
<td>ATLAS</td>
<td>A Toroidal LHC Apparatus</td>
</tr>
<tr>
<td>BNB</td>
<td>Booster neutrino beamline</td>
</tr>
<tr>
<td>BNL</td>
<td>Brookhaven National Laboratory</td>
</tr>
<tr>
<td>CEBAF</td>
<td>Continuous Electron Beam Facility</td>
</tr>
<tr>
<td>CC</td>
<td>Charged current</td>
</tr>
<tr>
<td>CCQE</td>
<td>Neutrino-nucleon charge current quasi-elastic ($\nu_l + n \rightarrow l^- + p$)</td>
</tr>
<tr>
<td>CCPi+</td>
<td>Neutrino-nucleon charge current $\pi^+$ ($\nu_l + n \rightarrow l^- + \pi^+ + n$)</td>
</tr>
<tr>
<td>CERN</td>
<td>European Organization for Nuclear Research</td>
</tr>
<tr>
<td>CKM</td>
<td>Cabibo-Kobayashi-Maskawa</td>
</tr>
<tr>
<td>CMS</td>
<td>Compact Muon Solenoid</td>
</tr>
<tr>
<td>CP</td>
<td>Charge Parity</td>
</tr>
<tr>
<td>CV</td>
<td>Central Value</td>
</tr>
<tr>
<td>CVC</td>
<td>Conserved Vector Current</td>
</tr>
<tr>
<td>DAQ</td>
<td>Data acquisition</td>
</tr>
<tr>
<td>DIF</td>
<td>Decay in flight</td>
</tr>
<tr>
<td>DOF</td>
<td>Degree of freedom</td>
</tr>
<tr>
<td>FNAL</td>
<td>Fermi National Accelerator Laboratory or Fermilab</td>
</tr>
<tr>
<td>FSI</td>
<td>Final state interactions</td>
</tr>
<tr>
<td>HARP</td>
<td>Hadron Production Experiment</td>
</tr>
<tr>
<td>Abbreviation</td>
<td>Definition</td>
</tr>
<tr>
<td>--------------</td>
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</tr>
<tr>
<td>HPWF</td>
<td>Harvard-Penn-Wisconsin-Fermilab</td>
</tr>
<tr>
<td>HV</td>
<td>High voltage</td>
</tr>
<tr>
<td>GEANT</td>
<td>Geometry and Tracking (modelling software)</td>
</tr>
<tr>
<td>GWS</td>
<td>Glashow-Weinberg-Salam model</td>
</tr>
<tr>
<td>K2K</td>
<td>KEK to Kamioka</td>
</tr>
<tr>
<td>KamLAND</td>
<td>Kamioka Liquid Scintillator Antineutrino Detector</td>
</tr>
<tr>
<td>KATRIN</td>
<td>Karlsruhe Tritium Neutrino Experiment</td>
</tr>
<tr>
<td>LINAC</td>
<td>Linear accelerator</td>
</tr>
<tr>
<td>LSND</td>
<td>Liquid Scintillator Neutrino Detector</td>
</tr>
<tr>
<td>MC</td>
<td>Monte Carlo (Computer Simulated Data)</td>
</tr>
<tr>
<td>MINUIT</td>
<td>CERN function minimization and error analysis package</td>
</tr>
<tr>
<td>MiniBooNE</td>
<td>Mini Booster Neutrino Experiment</td>
</tr>
<tr>
<td>MINOS</td>
<td>Main Injector Neutrino Oscillation Search</td>
</tr>
<tr>
<td>MNS</td>
<td>Maki-Nakagawa-Sakata</td>
</tr>
<tr>
<td>NC</td>
<td>Neutral current</td>
</tr>
<tr>
<td>NCE</td>
<td>Neutrino-nucleon neutral current elastic</td>
</tr>
<tr>
<td>NuMI</td>
<td>Neutrinos from the Main Injector</td>
</tr>
<tr>
<td>PMT</td>
<td>Photomultiplier Tube</td>
</tr>
<tr>
<td>POT</td>
<td>Protons on target</td>
</tr>
<tr>
<td>$Q^2$</td>
<td>Momentum transfer squared</td>
</tr>
<tr>
<td>QCD</td>
<td>Quantum chromodynamics</td>
</tr>
<tr>
<td>QED</td>
<td>Quantum electrodynamics</td>
</tr>
<tr>
<td>SM</td>
<td>Standard Model</td>
</tr>
<tr>
<td>PE</td>
<td>Photo-electron</td>
</tr>
<tr>
<td>PDG</td>
<td>Particle Data Group</td>
</tr>
<tr>
<td>PID</td>
<td>Particle identification</td>
</tr>
<tr>
<td>RFG</td>
<td>Relativistic Fermi gas</td>
</tr>
<tr>
<td>Abbreviation</td>
<td>Description</td>
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<tr>
<td>--------------</td>
<td>--------------------------------------------</td>
</tr>
<tr>
<td>RENO</td>
<td>Reactor Experiment for Neutrino Oscillations</td>
</tr>
<tr>
<td>SNO</td>
<td>Sudbury Neutrino Observatory</td>
</tr>
<tr>
<td>SPE</td>
<td>Single photoelectron</td>
</tr>
<tr>
<td>T2K</td>
<td>Tokai to Kamioka</td>
</tr>
<tr>
<td>UA1</td>
<td>Underground Area 1</td>
</tr>
<tr>
<td>UV</td>
<td>Ultraviolet</td>
</tr>
<tr>
<td>WMAP</td>
<td>Wilkinson Microwave Anisotropy Probe</td>
</tr>
<tr>
<td>WNC</td>
<td>Weak neutral current</td>
</tr>
<tr>
<td>WS</td>
<td>Wrong sign</td>
</tr>
</tbody>
</table>
Acknowledgements

First and foremost, I would like to thank my advisor, Ion Stancu. Thank you Ion, for getting me interested in experimental neutrino physics. From you, I learnt the importance of having an eye for details which is crucial for an experimentalist, and also about working hard and enjoying life at the same time.

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Chapter 1

Introduction

The Standard Model of particle physics is the culmination of mankind’s attempt to understand the material world. It is a framework which describes the fundamental particles in nature and the forces of interaction among them. In this chapter, a brief overview of the Standard Model is presented with some emphasis on neutrinos and the theory of weak interactions, along with an outline of the thesis.

1.1 The Standard Model Particles

According to the Standard Model, the universe is ultimately composed of two kinds of particles, quarks and leptons – all spin 1/2 fermions.

The quarks are presently known to have six degrees of freedom or ‘flavors’, viz. up (u), down (d), strange (s), charm (c), bottom (b), and top (t). The leptons are also six in number: the electron (e), muon (µ), tau (τ) and their corresponding neutrinos ν_e, ν_µ, and ν_τ respectively. These particles can be arranged in doublets, in increasing order of mass forming three generations, as shown in Table 1.1. It should be noted that most of the known universe is composed of the particles from the first generation. The second and third generation particles are created at particle accelerators or cosmic rays and decay rapidly into the particles of the first generation. The upper components of lepton doublets all have
Table 1.1: Particles in the Standard Model. The quarks and leptons are spin 1/2 particles while the bosons are spin 1.

<table>
<thead>
<tr>
<th>Generation</th>
<th>I</th>
<th>II</th>
<th>III</th>
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<tbody>
<tr>
<td>Quarks</td>
<td></td>
<td></td>
<td></td>
</tr>
<tr>
<td>(u)</td>
<td>(c)</td>
<td>(t)</td>
<td></td>
</tr>
<tr>
<td>(d)</td>
<td>(s)</td>
<td>(b)</td>
<td></td>
</tr>
<tr>
<td>Leptons</td>
<td></td>
<td></td>
<td></td>
</tr>
<tr>
<td>(e)</td>
<td>(µ)</td>
<td>(τ)</td>
<td></td>
</tr>
<tr>
<td>(ν_ℓ)</td>
<td>(ν_µ)</td>
<td>(ν_τ)</td>
<td></td>
</tr>
</tbody>
</table>

| Bosons     |   |    |     |
| γ          | (EM interaction) |   |     |
| W^±, Z^0   | (Weak interaction) |   |     |
| (8)g       | (Strong interaction) |   |     |

Higgs boson    H

Table 1.1: Particles in the Standard Model. The quarks and leptons are spin 1/2 particles while the bosons are spin 1.

an electric charge of $-1$ (in units of the absolute electron charge), while the neutrinos have charge 0. In the quark sector the upper components have an electric charge of $+2/3$ while the lower components are $-1/3$. While the leptons can exist in isolation, the quarks, due to the fact that they possess an additional degree of freedom called “color”, are only found in color neutral states called baryons (e.g., proton = uud, neutron = udd, etc.), or mesons which are quark-antiquark pairs (e.g., $π^+ = u\bar{d}$, $K^+ = u\bar{s}$, etc.).

According to the Standard Model each of the fermions has a corresponding antiparticle. The antiparticles have the same mass and spin as their particle counterparts, but the opposite values of charge, color charge, and flavor. In the case of the neutrinos, it is still an open question if they are their own antiparticle or if the neutrino and antineutrino are distinct particles. Antiparticles are denoted by their charge labels (e.g., $e^−$ and $e^+$ for electrons and positrons, respectively) or a bar over the letter (e.g., $\bar{ν}$ and $ν$ for the neutrino and antineutrino, respectively). A list of all the quantum numbers of the quarks are given in
Table 1.2, while Table 1.3 gives the quantum numbers of the leptons.

<table>
<thead>
<tr>
<th>Quarks</th>
<th>$Q$</th>
<th>$I_3$</th>
<th>$S$</th>
<th>$C$</th>
<th>$B$</th>
<th>$T$</th>
<th>Mass</th>
</tr>
</thead>
<tbody>
<tr>
<td>$u$</td>
<td>$\frac{2}{3}$</td>
<td>$\frac{1}{2}$</td>
<td>0</td>
<td>0</td>
<td>0</td>
<td>0</td>
<td>$2.3^{+0.7}_{-0.5}$ MeV</td>
</tr>
<tr>
<td>$d$</td>
<td>$-\frac{1}{3}$</td>
<td>$-\frac{1}{2}$</td>
<td>0</td>
<td>0</td>
<td>0</td>
<td>0</td>
<td>$4.8^{+0.7}_{-0.3}$ MeV</td>
</tr>
<tr>
<td>$c$</td>
<td>$-\frac{1}{3}$</td>
<td>0</td>
<td>$-1$</td>
<td>0</td>
<td>0</td>
<td>0</td>
<td>$1.275 \pm 0.025$ GeV</td>
</tr>
<tr>
<td>$s$</td>
<td>$\frac{2}{3}$</td>
<td>0</td>
<td>0</td>
<td>$+1$</td>
<td>0</td>
<td>0</td>
<td>$95 \pm 5$ MeV</td>
</tr>
<tr>
<td>$t$</td>
<td>$-\frac{1}{3}$</td>
<td>0</td>
<td>0</td>
<td>0</td>
<td>$-1$</td>
<td>0</td>
<td>$173.5 \pm 0.6 \pm 0.8$ GeV</td>
</tr>
<tr>
<td>$b$</td>
<td>$\frac{2}{3}$</td>
<td>0</td>
<td>0</td>
<td>0</td>
<td>0</td>
<td>$+1$</td>
<td>$4.18 \pm 0.03$ GeV</td>
</tr>
</tbody>
</table>

Table 1.2: List of quarks with their quantum numbers and mass. $Q$: electric charge, $I_3$: 3rd component of isospin, $S$: strangeness, $C$: charmness, $B$: bottomness, $T$: topness. These quantum numbers change their signs for anti-quarks. The values for the quark masses are from Ref. [1]

The mediators of interactions between fermions are spin 1 particles called gauge bosons. They are the photon $\gamma$ for the electromagnetic interaction, the weak bosons $W^\pm$ and $Z^0$ for the weak interaction, and eight gluons $g$ for the strong interactions. The photon and the gluons are massless, while the weak bosons are massive, $M_{W^\pm} \simeq 80$ GeV and $M_{Z^0} \simeq 91$ GeV (throughout this thesis we use $c = 1$).

The final particle introduced in the Standard Model is the Higgs boson $H$, which is a spin 0 particle. Evidence for its existence has been reported only very recently by the ATLAS and CMS experiments at the Large Hadron Collider, with a mass of about 125 GeV [2, 3].

Leptons

<table>
<thead>
<tr>
<th>Leptons</th>
<th>Q</th>
<th>$L_e$</th>
<th>$L_\mu$</th>
<th>$L_\tau$</th>
<th>Mass</th>
</tr>
</thead>
<tbody>
<tr>
<td>$e$</td>
<td>-1</td>
<td>+1</td>
<td>0</td>
<td>0</td>
<td>0.511 MeV</td>
</tr>
<tr>
<td>$\nu_e$</td>
<td>0</td>
<td>+1</td>
<td>0</td>
<td>0</td>
<td>&lt; 2 eV</td>
</tr>
<tr>
<td>$\mu$</td>
<td>-1</td>
<td>0</td>
<td>+1</td>
<td>0</td>
<td>106 MeV</td>
</tr>
<tr>
<td>$\nu_\mu$</td>
<td>0</td>
<td>0</td>
<td>+1</td>
<td>0</td>
<td>&lt; 2 eV</td>
</tr>
<tr>
<td>$\tau$</td>
<td>-1</td>
<td>0</td>
<td>0</td>
<td>+1</td>
<td>1.78 GeV</td>
</tr>
<tr>
<td>$\nu_\tau$</td>
<td>0</td>
<td>0</td>
<td>0</td>
<td>+1</td>
<td>&lt; 2 eV</td>
</tr>
</tbody>
</table>

**Table 1.3:** List of leptons with their quantum numbers and mass. *Q*: electric charge, $L_e$: electron number, $L_\mu$: muon number, $L_\tau$: tau number. These quantum numbers change their signs for anti-leptons. The values for the lepton masses are from Ref. [1]

### 1.2 The Standard Model Forces

The quarks and leptons interact among themselves and each other via the four fundamental forces known so far, namely the electromagnetic force, the weak force, the strong force and gravity. Photons are the mediators of the electromagnetic force, the weak force is mediated by the massive weak bosons, while the strong force is mediated by the gluons. All fermions also interact via the gravitational force, but the interaction is so weak that it is beyond the realm of the Standard Model. The mediator for gravitational force is the graviton, a particle with spin 2 which has not been observed to date. The electromagnetic interaction was the first to be investigated and is described by a renormalizable gauge theory with an Abelian $U(1)$ symmetry called quantum electrodynamics (QED). All fermions, with the exception of neutrinos which do not have an intrinsic electric charge, experience the electromagnetic force.

In the 1960’s the weak and the electromagnetic interactions were unified into a renor-
Table 1.4: The table shows the four basic forces of interaction. Gravity is not included in the Standard Model and its mediator the graviton has not been observed.

<table>
<thead>
<tr>
<th>Force</th>
<th>Participants</th>
<th>Mediator(s)</th>
<th>Spin</th>
</tr>
</thead>
<tbody>
<tr>
<td>Electromagnetic</td>
<td>all fermions except $\nu$'s</td>
<td>$\gamma$</td>
<td>1</td>
</tr>
<tr>
<td>Weak</td>
<td>all fermions</td>
<td>$W^\pm, Z^0$</td>
<td>1</td>
</tr>
<tr>
<td>Strong</td>
<td>only quarks &amp; gluons</td>
<td>gluons</td>
<td>1</td>
</tr>
<tr>
<td>Gravity</td>
<td>all fermions</td>
<td>graviton</td>
<td>2</td>
</tr>
</tbody>
</table>

malizable theory in the framework of a non-Abelian gauge theory with $SU(2)_L \otimes U(1)_Y$ symmetry called the electroweak standard model. The electroweak theory applies to all the fermions since they all experience the weak force. The neutrinos in particular only interact via the weak force. As this dissertation presents neutrino and antineutrino interaction measurements, we will discuss the development of the electroweak theory in some detail in the next section, §1.3.

The field theory for the strong interaction was put forth in 1970 by Gell-Mann et al. It is also a non-Abelian gauge theory with $SU(3)_C$ symmetry. The subscript C stands for the color charge, which is possessed by both the quarks and the mediator gluons. The theory, called quantum chromodynamics (QCD), describes the dynamics of quarks and gluons. A concise description of the QCD formalism can be found in Ref. [1].

Finally, the Higgs boson with spin 0 is introduced for the Higgs mechanism to work, in which the local gauge symmetry is spontaneously broken, giving rise to massive gauge bosons as well as masses to other fermions. The origin of neutrino masses remains an open issue and neutrinos have long been considered massless in the Standard Model. Recent results from neutrino oscillation experiments show that neutrinos must have non-zero masses, as we discuss in §1.5.
To sum up, the weak and electromagnetic interactions are formulated by the gauge theory with $SU(2)_L \otimes U(1)_Y$ symmetry and the strong interaction by a gauge theory with $SU(3)_C$ symmetry. Hence one can describe all the interactions of elementary particles by a gauge theory with some internal symmetry $G$, which can be constructed by taking the direct product of each of the individual symmetries:

$$G = SU(3)_C \otimes SU(2)_L \otimes U(1)_Y.$$  

The resultant theory is called the Standard Model of particle physics.

### 1.3 The Electroweak Theory

In 1930, Wolfgang Pauli proposed the existence of the neutrino [4] to explain the continuous spectrum of nuclear beta-decay and save the energy conservation principle from being violated. Enrico Fermi was the first to put forth a formal theory of the weak interaction including the neutrino in 1932 [5]. Using the analogy to the electromagnetic interaction he proposed an interaction equivalent to the following interaction Lagrangian,

$$\mathcal{L} = \frac{G_F}{\sqrt{2}} \bar{p}_\mu n \mu (\bar{e} \gamma_{\mu} \nu)$$

where $\gamma^\mu$ are the Dirac gamma matrices and $G_F$ is the Fermi constant.

It is a charged current interaction in which there is a net charge transfer from the hadronic to the leptonic current. The coupling constant, $G_F$, is universal, i.e., it is the same for all lepton flavors. Fermi predicted a value for $G_F$ for the first time, which is now known to be $1.166 \times 10^{-5}$ GeV$^{-2}$. However, there is no propagator, and the currents are purely vector as in the electromagnetic interaction. Moreover, the cross section predicted is extremely small and breaks down at high energies. Hence it was clear that a modification of the theory was required.
In 1956 T.D. Lee and C. N. Yang [6], while trying to solve the \(\tau - \theta\) problem, suggested that parity may be violated in the weak sector. \(\tau\) and \(\theta\), both strange mesons which appeared to be identical particles decayed differently, \(\tau\) to an parity odd state \((\pi^+, \pi^+, \text{and} \pi^-)\) and \(\theta\) to a parity even state \((\pi^+, \pi^0, \text{and} \pi^0)\). One year later C.S. Wu et al. [7] carried out an experiment which conclusively established that parity was maximally violated in the nuclear beta-decay of \(^{60}\text{Co}\).

In order to accommodate the observation of parity violation, Sudarshan and Marsak, in 1958 suggested a modification of the Fermi theory, the so called \(V-A\) model (vector minus axial vector) [8]. In the same year, Feynmann and Gell-Mann [9] independently arrived at the same conclusion; the proposed interaction Lagrangian reads now:

\[
\mathcal{L} = \frac{G_F}{\sqrt{2}} [\bar{p} \gamma^\mu (1 - \gamma_5) n] [\bar{e} \gamma^\mu (1 - \gamma_5) \nu].
\]

Meanwhile, in 1956, Reines and Cowan made the first direct observation of neutrinos [10] and in 1962 Lederman, Schwartz, Steinberg et al. showed that muon neutrino is different from an electron neutrino [11] which pointed to the existence of lepton families.

The experimental observations were presenting crucial clues about the underlying structure of the interactions, as follows:

- All particles show a \(U(1)\) group invariance which was later deduced to electromagnetic interactions.

- Handedness or chirality as a unique feature of interacting particles and left-handed and right-handed particles transform differently. Parity violation in weak interactions pointed to the existence of left-handed weak-isospin doublets (or their right-handed antiparticles).

- The weak bosons must be charged – because the weak interaction is charge changing, and massive – to explain the short range of the weak force.
- Neutrinos are exclusively left-handed and massless.

- The charged-current weak interaction is universal, which means any theory should be replicable across the three generations.

The resulting theory that incorporates all the information is called the Glashow-Weinberg-Salam (GWS) model for weak interactions [12, 13, 14]. It is a non-Abelian gauge theory with $SU(2)_L \otimes U(1)_Y$ symmetry accompanied by the Higgs mechanism [15]. We define the weak hypercharge $Y$ through the Gell-Mann–Nishijima relation between electric charge $Q$ and (weak) isospin ($I_3$),

$$Q = I_3 + \frac{1}{2}Y.$$

The introduction of Higgs mechanism leads to the spontaneous symmetry breaking $SU(2)_L \otimes U(1)_Y \rightarrow U(1)_{EM}$ and as a result the weak bosons acquire masses while the photon remains massless.

One may note that neutral current interactions are a theoretical consequence of the GWS model. Neutral currents were first observed in the Gargamelle experiment at CERN [16]. The discovery of $W^\pm$ and $Z^0$ at CERN in 1982 [17], at the mass range predicted by the theory was a great triumph for the model.

**For Leptons**

The Lagrangian for interaction of the leptons are given by [18]:

$$\mathcal{L}_{\text{leptons}} = \sum_{l=e,\mu,\tau} \frac{-g}{2\sqrt{2}} \left[ \bar{\nu}_l \gamma^\mu (1 - \gamma_5) l W^+_{\mu} + \bar{l} \gamma^\mu (1 - \gamma_5) \nu_l W^-_{\mu} \right]$$

$$- \frac{g}{4 \cos \theta_W} \bar{\nu}_l \gamma^\mu (1 - \gamma_5) \nu_l Z_\mu$$

$$- \frac{g}{4 \cos \theta_W} \bar{l} \left[ L_l \gamma^\mu (1 - \gamma_5) + R_l \gamma^\mu (1 + \gamma_5) \right] l Z_\mu$$

$$+ g \sin \theta_W \bar{l} \gamma^\mu l A_\mu ,$$
where the $L_l$ and $R_l$ are the chiral couplings, $g$ is the coupling constant, and $\theta_W$ is the weak mixing angle called the Weinberg angle.

**For Quarks**

The theory can be extended to include electroweak interactions of quarks by making the following observations:

- The quarks have 3 additional color degree of freedom, whereas the leptons are colorless. However since electroweak interactions are colorblind one can suppress the color index.

- All quarks are massive as opposed to the leptons, wherein the neutrinos are considered massless according to the GSW model. This introduces right-handed singlets for all the quarks, unlike in the case of leptons where the neutrinos were only left-handed.

- The quarks are fractionally charged whereas the charged leptons have unit charge. This results in the quarks having a different weak hypercharge as per the Gell-Mann–Nishijima relation used earlier.

- With respect to the weak interaction the quark mass eigenstates are different from their flavor eigenstates and are related by the Cabibo-Kobayashi-Maskawa (CKM) matrix [1].

The Lagrangian for interaction of the quarks are given by [18]:

$$
\mathcal{L}_{\text{quarks}} = -\frac{g}{2\sqrt{2}} \bar{u} \gamma^\mu (1 - \gamma_5) d' W^+ \mu - \frac{g}{2\sqrt{2}} \bar{d}' \gamma^\mu (1 - \gamma_5) u W^- \mu - \frac{g}{4 \cos \theta_W} \bar{u} \gamma^\mu \left[ 1 - \frac{8}{3} \sin^2 \theta_W - \gamma_5 \right] u Z_\mu + \frac{g}{4 \cos \theta_W} \bar{d}' \gamma^\mu \left[ 1 - \frac{4}{3} \sin^2 \theta_W - \gamma_5 \right] d' Z_\mu - \frac{2}{3} g \sin \theta_W \bar{u} \gamma^\mu A_\mu + \frac{1}{3} g \sin \theta_W \bar{d}' \gamma^\mu d' A_\mu + \text{corresponding higher generation terms for } (c,s) \text{ and } (t,b).
$$
In the above equation we chose the lower isospin quarks to acquire the CKM matrix. The mixing between the mass eigenstates and the flavor eigenstates of the bottom elements of the quark doublets is represented as:

\[
\begin{pmatrix}
\bar{d}' \\
\bar{s}' \\
\bar{b}'
\end{pmatrix}
= \begin{pmatrix}
V_{ud} & V_{us} & V_{ub} \\
V_{cd} & V_{cs} & V_{cb} \\
V_{td} & V_{ts} & V_{tb}
\end{pmatrix}
\begin{pmatrix}
\bar{d} \\
\bar{s} \\
\bar{b}
\end{pmatrix}
= V
\begin{pmatrix}
d \\
s \\
b
\end{pmatrix}
\]

where \( V \) is the CKM matrix. The current best measurements of the magnitudes of the CKM matrix elements is [1]:

\[
\begin{pmatrix}
|V_{ud}| & |V_{us}| & |V_{ub}| \\
|V_{cd}| & |V_{cs}| & |V_{cb}| \\
|V_{td}| & |V_{ts}| & |V_{tb}|
\end{pmatrix}
= \begin{pmatrix}
0.97427 \pm 0.00015 & 0.22534 \pm 0.00065 & 0.00351 \pm 0.00015 \\
0.22520 \pm 0.00065 & 0.97344 \pm 0.00016 & 0.0412 \pm 0.00011 \\
0.00867 \pm 0.00029 & 0.0404 \pm 0.00011 & 0.999146 \pm 0.000021
\end{pmatrix}.
\]

### 1.4 Limitations of the Standard Model

Although the Standard Model has been rigorously tested, physicists believe that it does not represent a complete picture of the universe [19]. Among the main shortcomings it lacks a theory of gravitation, and does not predict the existence of non-baryonic dark matter or dark energy.

The model has about 25 parameters which are experimentally determined. At present we do not know why these parameters have their respective values or if there are any relationships between them. Other questions include the strong CP problem and the hierarchy problem. The former is with regard to QCD and its adherence to CP-symmetry as opposed to the weak sector where it is readily broken, while the latter questions the discrepancy in the relative strengths of the fundamental forces.

There have been several experimental observations which disagree with the Standard Model predictions – like the muon anomalous magnetic moment [1], the di-muon charge
asymmetry [20], and of particular interest to us, the phenomenon of neutrino oscillations [21] and its consequence, i.e., massive neutrinos.

1.5 Neutrino Oscillations

The phenomenon of neutrino oscillation provides the best explanation for a long standing mystery in experimental physics, namely the solar neutrino problem. In 1968 Davis et al. [22] performed the first in a series of experiments to measure a deficit in the number of neutrinos observed coming from the sun as compared to the solar models [23]. An analogous deficit was seen in the atmospheric neutrinos by the Kamiokande experiment in 1988 [24]. A decade later, the Super-Kamiokande experiment accounted for the atmospheric neutrino deficit by enhancing the analysis techniques to become sensitive to other flavors of neutrinos [25]. In 2002 the Sudbury Neutrino Observatory (SNO) experiment accounted for the deficit of solar electron neutrinos [26], again by designing an experiment sensitive to all active neutrino flavors. In 2003, the reactor-based KamLAND experiment showed that neutrinos undergo an oscillatory flavor conversion in vacuum in the solar $\Delta m^2$ range – see Eq.(1.1) for an explanation of the neutrino oscillation parameters. In addition, accelerator-based experiments (K2K [27] and MINOS [28]) have independently confirmed the atmospheric neutrino oscillations.

Neutrino oscillation is a quantum mechanical phenomenon where a neutrino of a specific lepton flavor can be measured to have a different flavor after travelling some distance in space. This is due to the fact that the neutrino flavor eigenstates ($\nu_e$, $\nu_\mu$, and $\nu_\tau$) are different from their mass eigenstates denoted by $\nu_1$, $\nu_2$, and $\nu_3$. Each flavor eigenstate is a coherent superposition of the mass eigenstates, and their mixing is represented by the Maki-Nakagawa-Sakata (MNS) matrix – similar to the CKM matrix in the quark sector, discussed in §1.3:

$$\nu_l = \sum_{m=1}^{3} U_{lm} \nu_m \text{ where } l = e, \mu, \tau.$$
$U$ is the unitary MNS matrix; it is a $3 \times 3$ matrix relating the three flavor eigenstates with the three mass eigenstates:

$$U = \begin{pmatrix}
U_{e1} & U_{e2} & U_{e3} \\
U_{\mu 1} & U_{\mu 2} & U_{\mu 3} \\
U_{\tau 1} & U_{\tau 2} & U_{\tau 3}
\end{pmatrix} = \begin{pmatrix}
1 & 0 & 0 \\
0 & c_{23} & s_{23} \\
0 & -s_{23} & c_{23}
\end{pmatrix} \begin{pmatrix}
c_{13} & 0 & s_{13}e^{-i\delta} \\
0 & 1 & 0 \\
-s_{13}e^{i\delta} & 0 & c_{13}
\end{pmatrix} \begin{pmatrix}
c_{12} & s_{12} & 0 \\
-s_{12} & c_{12} & 0 \\
0 & 0 & 1
\end{pmatrix} \begin{pmatrix}
e^{i\alpha_1} & 0 & 0 \\
0 & e^{i\alpha_2} & 0 \\
0 & 0 & 1
\end{pmatrix},$$

where $\theta_{ij}$ are the three mixing angles, $c_{ij} = \cos \theta_{ij}$, $s_{ij} = \sin \theta_{ij}$, and $\delta$ is the CP phase. $\alpha_1$ and $\alpha_2$ are the Majorana phases which are non-zero if neutrinos are Majorana particles (§1.6). The probability of oscillation between two flavor states, in vacuum, is given by:

$$P_{\nu_a \to \nu_b} = \delta_{ab} - 4 \sum_{i>j} \text{Re}(U_{ai}^*U_{bi}U_{aj}U_{bj}^*) \sin^2 \left( \frac{\Delta m_{ij}^2 L}{4E_{\nu}} \right)$$

$$+ 2 \sum_{i>j} \text{Im}(U_{ai}^*U_{bi}U_{aj}U_{bj}^*) \sin^2 \left( \frac{\Delta m_{ij}^2 L}{2E_{\nu}} \right),$$

(1.1)

where $\delta_{ab}$ is the Kronecker delta, $U_{ai}$ is the lepton mixing matrix element with flavor index $a$ and mass eigenstate index $i$, $\Delta m_{ij}^2 = m_i^2 - m_j^2$ is the mass squared difference between the mass eigenstates $\nu_i$ and $\nu_j$, $L$ is the distance between the creation and the detection of the neutrino, and $E_{\nu}$ is the neutrino energy.

One often uses a simplified, two neutrino oscillation formalism, where one of the mass eigenstates decouples. In this case the relation between the neutrino states is described by one mixing angle, $\theta$, and one mass difference, $\Delta m^2 = m_2^2 - m_1^2$. The mixing matrix then is simply:

$$U = \begin{pmatrix}
\cos \theta & \sin \theta \\
-\sin \theta & \cos \theta
\end{pmatrix},$$
while the oscillation probability formula is reduced to

\[
P(\nu_a \rightarrow \nu_b) = \begin{cases} 
1 - \sin^2 2\theta \sin^2 \left(1.27 \Delta m^2_{ij} \frac{L}{E}\right) & \text{if } a = b \\
\sin^2 2\theta \sin^2 \left(1.27 \Delta m^2_{ij} \frac{L}{E}\right) & \text{if } a \neq b.
\end{cases}
\]  

(1.2)

Here we use in standard units for neutrino oscillation experiments, namely

\[
\frac{\Delta m^2_{ij} L}{4E} = 1.27 \frac{\Delta m^2_{ij}(eV^2)L(m)}{E(MeV)}.
\]

Several neutrino oscillations experiments observing reactor, solar, and accelerator neutrinos have provided the current best known values of oscillation parameters as given in the Particle Data Group reference [1], as summarized in Table 1.5. However, recent results from reactor experiments (Double-Chooz, Daya Bay, and RENO) have shown that \(\theta_{13}\) is non-zero, with the following results:

<table>
<thead>
<tr>
<th>Parameter</th>
<th>best-fit (±1σ)</th>
</tr>
</thead>
<tbody>
<tr>
<td>(\Delta m^2_{21})</td>
<td>(7.58^{+0.22}_{-0.26} \times 10^{-5} \text{eV}^2)</td>
</tr>
<tr>
<td>(</td>
<td>\Delta m^2_{32}</td>
</tr>
<tr>
<td>(\sin^2 \theta_{12})</td>
<td>(0.306^{+0.018}_{-0.015})</td>
</tr>
<tr>
<td>(\sin^2 \theta_{23})</td>
<td>(0.42^{+0.08}_{-0.03})</td>
</tr>
<tr>
<td>(\sin^2 \theta_{13})</td>
<td>(0.0251 \pm 0.0034)</td>
</tr>
</tbody>
</table>

**Table 1.5:** Current values of neutrino oscillation mixing parameters from the Particle Data Group 2012 [1].

Double Chooz [29]: \(\sin^2 2\theta_{13} = 0.109 \pm 0.030 \text{ (stat.)} \pm 0.025 \text{ (syst.)}\),

RENO [30]: \(\sin^2 2\theta_{13} = 0.113 \pm 0.013 \text{ (stat.)} \pm 0.019 \text{ (syst.)}\),

Daya Bay [31]: \(\sin^2 2\theta_{13} = 0.092 \pm 0.016 \text{ (stat.)} \pm 0.005 \text{ (syst.)}\).
Even though neutrino flavor oscillations indicate that the neutrino mass is non-zero, it does not allow us to determine the absolute scale of neutrino masses. The current best limits on neutrino mass come from a direct electron antineutrino mass measurement from tritium beta decay by the Troitzk experiment [32];

\[ m_{\bar{\nu}_e} < 2.05 \text{ eV at 95\% CL.} \]

Stringent limits on the sum of the neutrino masses also come from cosmology as reported by the analyses of the WMAP data [33], namely:

\[ \sum m_\nu < 2.0 \text{ eV at 95\% CL.} \]

In the near future, the KATRIN experiment is expected to measure the electron antineutrino mass with sensitivity \( \sim 0.20 \text{ eV} \).

### 1.6 Antiparticles and Antineutrinos

P.A.M. Dirac was the first to introduce the concept of an antiparticle [34]. In 1928 he made the first attempt to combine the theory of quantum mechanics with special relativity and conceived the relativistic wave equation of the electron. However, the equation permitted solutions with negative energies which defied a physical interpretation. Dirac postulated that for every particle with positive energy solution there exists a corresponding antiparticle with the same mass but opposite charge.

In 1934 W. Pauli and V. Weisskopf [35] extended the theory to include fermions. The first experimental observation of an antiparticle was made in 1932 by C. Anderson [36], who discovered positrons (anti-electrons) while studying cosmic rays using a cloud chamber. Since then, many antiparticles have been observed, confirming the idea. Finally, the present QED picture of an antiparticle was proposed by E. Stuckelberg in 1942 [37] and later formalized by
R. Feynman in 1949 [38]. According to the Feynman-Stuckelberg interpretation the negative energy solution antiparticle is a particle propagating backward in time, while a positive energy particle is propagating forward in time, and vice-versa.

While charged particles have antiparticles with opposite charge, electrically neutral particles, like the photon or the $Z^0$, are self-conjugate, i.e., they are their own antiparticle. Note that both the photon and the $Z^0$ are bosons. Back in 1937 E. Majorana [39] postulated the possibility of self-conjugate fermions and the only possible candidates among the standard model particles are the electrically neutral neutrinos. Fermions which are self-conjugate are referred to as Majorana particles, while the other fermions are called Dirac particles. It is still an open question whether neutrinos are Majorana or Dirac particles.

### 1.7 The Aim of this Dissertation

This dissertation aims to make a high-statistics antineutrino neutral current elastic (NCE) scattering cross section measurement on carbon. The only previous measurement of this cross section was performed by the E734 experiment at the Brookhaven National Laboratory (BNL), where the antineutrino sample consisted of 1,821 events. The MiniBooNE antineutrino NCE sample, as we present in this analysis, has 60,605 candidate events with a purity of 48%. This is more than one order of magnitude increase in statistics over the previous measurement.

Neutrino and antineutrino cross section information in the energy regime of MiniBooNE ($\sim 0.8$ GeV in neutrino mode and $\sim 0.6$ GeV in antineutrino mode) is important not only for next-generation accelerator-based neutrino experiments, but also for testing the validity of various nuclear interaction models.

Recent results from the MiniBooNE neutrino charged-current quasielastic (CCQE) scattering measurement, as well as the neutrino NCE scattering measurements point to an enhancement in the cross section which has not been explained. A better agreement with the
standard theoretical predictions is achieved if the axial mass ($M_A$) is assumed to be about 20% to 30% higher than the accepted nominal value of about 1 GeV. However, there are many competing models which try to explain this discrepancy [40, 41, 42, 43, 44, 45]. A ratio measurement of the antineutrino to neutrino NCE scattering cross section will cancel many systematic errors and would be less model dependent as compared to the individual cross section measurements. In addition to the cross section measurement, this ratio should also yield a valuable input to the theoretical community to test various model predictions. This cross section ratio is also a part of the work done in this dissertation.

Finally, this dissertation also includes a $\chi^2$-based analysis to determine the best values of the axial mass and Pauli blocking parameter that best matches the antineutrino NCE scattering data.

1.8 Layout of this document

In Chapter 1 we briefly introduced the Standard Model of particle physics with an emphasis on the weak interaction. We also discussed some aspects of neutrino physics, the history, current knowledge and outstanding questions. Chapter 2 focuses on the neutral current elastic scattering interactions. We look at how scattering interactions provide us with information about the structure of matter. We go on to derive the theoretical neutrino neutral current elastic cross section formulae. We also present some previous neutral current measurements. Chapter 3 presents a description of the MiniBooNE experimental setup, in terms of both the hardware and software employed. The analysis of the antineutrino neutral current elastic scattering data in MiniBooNE is presented in Chapter 4, both in terms of the differential cross section and the underlying axial mass parameter. The analysis work done reported in Chapter 4 onwards represents the research work done as part of this dissertation, unless stated otherwise. MiniBooNE has accumulated the world’s largest samples of neutral current elastic scattering events (by more than one order of magnitude), both in the neutrino and
antineutrino mode, which makes these measurements of particular interest to the nuclear theory community. The ratio of the neutral current elastic scattering differential cross sections in neutrino and antineutrino modes is also presented in this chapter. This quantity is less dependent on the underlying parameters and has smaller systematic errors as the individual cross sections, which makes it a more robust measurement. The concluding remarks are summarized in Chapter 5, followed by an appendix which describes the possibility of using the MiniBooNE neutral current elastic scattering data to search for a light dark matter particle.
Chapter 2

Neutral Current Elastic Scattering

In this chapter we start with the history of electron scattering experiments and how they are used to probe the structure of matter. We move on to the discovery of neutral current neutrino scattering and develop the corresponding theoretical formalism. We also discuss the various form factors employed and their origins. Finally we present some of the previous neutral current elastic scattering measurements. The formalism in this chapter follows Ref. [46]

2.1 Elastic Scattering with Electrons

Elastic scattering experiments have long been a favorite tool for physicists to gain insight into the fundamental structure of matter. In fact, one of the early experiments which laid the foundation of subatomic physics was the $\alpha$ scattering experiment performed by Ernest Rutherford in 1911 [47]. Rutherford observed the scattering of $\alpha$ particles off a thin gold foil target, and observed that most of the particles went through, while a few of them scattered at high angles. His conclusion that the atom was mostly empty with a positively charged nucleus, debunked the “plum pudding” model prevalent at the time, according to which electrons were embedded in a positively charged “soup”.

Electrons were the first choice as projectiles in the early scattering experiments. The
choice was based on the fact that electrons were truly point-like and the resulting Coulomb scattering was a simple and well-understood interaction. Any deviation from the Coulomb interaction prediction would indicate that the target possessed extended structure. The elastic scattering of a relativistic electron on a spinless, point-like target of mass $M$ and charge $e$ is given by Mott’s formulae [48, 49] as:

$$
\left( \frac{d\sigma}{d\Omega} \right)_{\text{Mott}} = \frac{\alpha^2}{4e^2 \sin^2 \frac{\theta}{2}} \cdot \frac{e'}{e} \cos^2 \frac{\theta}{2},
$$

(2.1)

where $\alpha$ is a dimensionless constant which characterizes the electromagnetic force. The energy of the incident electron, $\epsilon$, and the energy of the scattered electron, $\epsilon'$, are related to the scattering angle $\theta$ in the laboratory frame by

$$
\epsilon' = \frac{\epsilon}{1 + \frac{2\epsilon}{M} \sin^2 \frac{\theta}{2}},
$$

and the momentum transfer squared is

$$
Q^2 = 4\epsilon \epsilon' \sin^2 \frac{\theta}{2}.
$$

The first evidence that the proton had a complex structure came in 1923 when O. Stern measured its anomalous magnetic moment [50], which was 2.79 times larger than that for a Dirac particle of the same mass.

R. Hofstader was the first to use electron scattering to directly probe the proton in 1955 [51] after the first high-energy electron beams (190 MeV) became available at Stanford. The experimental data differed from that of a proton possessing a point charge and point magnetic moment. He measured the charge radius of the proton to be 0.8 fm which is close to the modern value. Hofstader’s observation was understood in terms of the theoretical scattering law developed by M. Rosenbluth in 1950 [52]. This law described the composite
effect of charge and magnetic moment scattering and is given by:

\[
\frac{d\sigma}{d\Omega} = \left( \frac{d\sigma}{d\Omega} \right)_{\text{Mott}} \left\{ F_1^2(Q^2) + \frac{Q^2}{4M^2} \left[ F_2^2(Q^2) + 2(F_1(Q^2) + F_2(Q^2))^2 \tan^2 \frac{\theta}{2} \right] \right\}.
\] (2.2)

The Rosenbluth formula introduces the Dirac form factor \( F_1(Q^2) \) and the Pauli form factor \( F_2(Q^2) \). The former represents the proton’s charge and its associated Dirac magnetic moment, while the latter represents the anomalous magnetic moment of the proton. These form factors can be understood to describe the internal structure of the proton. For small four-momentum transfer squared, \( Q^2 \), they are Fourier transforms of the charge and magnetization distributions in the proton.

Theoretically, the neutron also possesses Dirac and Pauli form factors. However, the lack of a free neutron target makes measurements of the neutron form factors more difficult. Some of the difficulty was overcome by Hofstader and Yearian [53] by using a deuteron target as a carrier of neutrons and a difference method to compare the scattering from a deuteron target and a proton. These investigations first showed that the neutron could not be represented as a point nucleon and that its magnetic moment was distributed in a manner similar to that of the proton.

As more energetic electron beams became available, experiments have improved the measurement of the form factors of the nucleon. Currently, the best measurement of the proton form factors come from the Continuous Electron Beam Facility (CEBAF) at the Jefferson Laboratory [54] which employs the double polarization method – in which a polarized beam of electrons with energies up to 6 GeV are produced and polarized observables of the proton are measured using proton polarimeters.

### 2.2 Neutrino Elastic Scattering

One of the predictions of the GWS electroweak theory, developed through the 1960’s, was the existence of two charged gauge bosons, \( W^+ \) and \( W^- \), and a neutral gauge boson, \( Z^0 \), which
act as mediators to the weak force. The charged bosons $W^+$ and $W^-$ were responsible for the flavor-changing charged-current interaction, while the neutral $Z^0$ was responsible for the flavor conserving neutral-current interaction. The charged-current interaction mediated by $W^{\pm}$ is the classical nuclear $\beta$-decay which led to the discovery of the weak force and has been widely studied, but the $Z^0$ mediated weak neutral current (WNC) emerges as a result of the theoretical considerations of the GWS model; until then there was no search for experimental evidence for weak neutral current iterations.

Soon after the theoretical foundation was laid, the search began for $Z^0$ mediated neutral current interactions. The first observation of WNC was made in 1973 by the Gargamelle experiment [16] at CERN. Gargamelle was a giant bubble chamber detector which observed a single antineutrino-electron neutral current elastic interaction:

$$\bar{\nu}_\mu + e^- \rightarrow \bar{\nu}_\mu + e^-.$$ 

Later more WNC events were observed which were neutrino-nucleon neutral current deep inelastic events,

$$\bar{\nu}_\mu + N \rightarrow \bar{\nu}_\mu + X,$$

where $X$ is a hadronic final state. The HPWF (Harvard-Penn-Wisconsin-Fermilab) experiment at FNAL [55] also saw deep inelastic neutrino-nucleon neutral current events which confirmed the Gargamelle result.

The immediate fallout of the observation of WNC was the prediction of the mass value of the weak gauge vector boson $W^{\pm}$ on the basis of the GSW model combined with the first measurements of the weak mixing angle $\theta_W$. This led to the idea of building a proton-antiproton collider at CERN to search for the mediators of the weak iteration.

In 1982 the $W^{\pm}$ and $Z^0$ were discovered by the UA1 experiment [17] which was a great triumph for the standard model of weak interaction. The current values for the the masses
of the weak bosons are [1]:

\[ M_{W^\pm} = 80.399 \pm 0.023 \text{ GeV} \quad \text{and} \quad M_{Z^0} = 91.1876 \pm 0.0021 \text{ GeV}. \]

## 2.3 Neutrino-Nucleon Neutral-Current Elastic Cross Section

We now turn our attention to the theoretical aspects of WNC, specifically to the neutrino-nucleon neutral current elastic interaction. This analysis aims to measure the interaction in which the incoming antineutrino interacts with the quarks in the nucleus of the C or H atom (since the MiniBooNE mineral oil target is mainly CH₂). Following the theory developed in §1.3, the most general Lagrangian for neutrino-hadron neutral current can be written as [56]:

\[ \mathcal{L}^{\nu H}_{NC} = \sum_{l=e,\mu,\tau} -\frac{G_F}{\sqrt{2}} \bar{\nu}_l \gamma^\mu (1 - \gamma^5) \nu_l J^H_{\mu}, \quad (2.3) \]

Assuming contributions from not only the valence quarks u and d, but also from the sea quarks (s, c, t, b) we can expand the hadronic current as [56]:

\[ J^H_{\mu} = \sum_q [\varepsilon^q_L \bar{q} \gamma^\mu (1 + \gamma^5) q] + [\varepsilon^q_R \bar{q} \gamma^\mu (1 + \gamma^5) q] \]
\[ = \sum_q \bar{q} \gamma^\mu (g^q_V - g^q_A \gamma^5) q, \quad (2.4) \]

where the sum extends over the quark flavors (i.e., q = u, d, s, c, t, b). The vector and axial-vector couplings \( g^q_{V,A} \) are related to the chiral couplings \( \varepsilon^q_{L,R} \) by:

\[ g^q_V = \varepsilon^q_L + \varepsilon^q_R, \]
\[ g^q_A = \varepsilon^q_L - \varepsilon^q_R. \]

Further, even though it is not rigorously proven, an absence of experimental evidence of
flavor-changing neutral current effects allow us to assume that:

\[ \varepsilon^b_{L,R} = \varepsilon^s_{L,R} = \varepsilon^d_{L,R}, \]

\[ \varepsilon^t_{L,R} = \varepsilon^c_{L,R} = \varepsilon^u_{L,R}. \]

Experiments suggest that the contributions from the heavier quarks are negligible except from the strange quark sea which may add to the proton spin giving, rise to the so-called “proton spin crisis” [57].

We are now in a position to write the matrix element squared for the neutrino-nucleon neutral current interaction as:

\[
M = \frac{g^2}{2M_Z^2 \cos^2 \theta_W} [\bar{\nu} \gamma_\mu (1 - \gamma_5) \nu] \langle N_f | J^\mu_Z | N_i \rangle. \tag{2.5}
\]

The leptonic current in the square brackets is exactly calculable, but the hadronic current is quite complex due to strong interactions inside the nucleon. The matrix element of the neutral weak hadronic current between the nucleon states can be written as:

\[
\langle N_f | J^\mu_Z | N_i \rangle = \langle N_f | F_1^Z(Q^2) + F_2^Z(Q^2) \frac{i\sigma^{\mu\nu} q_\nu}{2M_N} + F_A^Z(Q^2) \gamma^\mu \gamma_5 | N_i \rangle, \tag{2.6}
\]

where the vector form factors, \( F_1^Z(Q^2) \) and \( F_2^Z(Q^2) \), are the Dirac and Pauli form factors which are taken from electron scattering experiments as discussed in §2.1. \( F_A^Z(Q^2) \) is the additional axial vector weak neutral current form factor, thus following the \( V - A \) form of the weak interaction.

### 2.4 Nucleon Form Factors

In scattering theory form factors provide a link between experimental observation and theoretical analysis. It is usually a multiplicative factor \( F(Q^2) \) – where \( Q^2 \) is the momentum
transfer squared. To be precise, the form factor can be shown to be the Fourier transform of the charge distribution within the nucleon.

In the present case the precise structure of the nucleon is not well known, and the nucleon form factors which are derived from various experiments – such as electron scattering data – encompass the best description of the nucleon as seen by the incoming neutrino.

In order to arrive at the nucleon form factors we start with the expression for the neutral weak current,

$$ J^Z = \frac{1}{2} \tau_3 J - 2 \sin^2 \theta_W J^{EM}, $$

where $J^Z$ is the weak neutral current, $J$ is the weak charged current, $J^{EM}$ is the electromagnetic current, $\theta_W$ is the Weinberg angle, and $\tau_3 = \text{diag}(1, -1)$. From the above equation we can write the neutral current form factors as:

$$ F^Z_i = (F_i - F^s_i) \frac{\tau_3}{2} - 2 \sin^2 \theta_W F^{EM}_i, \quad i = 1, 2 $$

$$ F^Z_A = (F_A - F^s_A) \frac{\tau_3}{2}, $$

where $F^Z_{1,2}$ is the weak vector form factor and $F^Z_A$ is the weak axial form factor. The charged current form factor $F_{1,2}$ is generalized to have an isoscalar part $F^s_{1,2}$ and $F^{EM}_{1,2}$ is the electromagnetic form factor.

The conserved vector current (CVC) hypothesis [58] allows us to relate $F^Z_1$ and $F^Z_2$ to the electromagnetic form factors for protons and neutrons which are better measured (see §2.1),

$$ F^Z_i = \left( \frac{1}{2} - \sin^2 \theta_W \right) \left[ F^{EM,p}_i - F^{EM,n}_i \right] \tau_3 $$

$$ - \sin^2 \theta_W \left[ F^{EM,p}_i - F^{EM,n}_i \right] - \frac{1}{2} F^s_i, \quad i = 1, 2. $$

$$ F^Z_A = \frac{\tau_3}{2} F_A - \frac{1}{2} F^s_A, $$

where we have used the relation:

$$ F_i = F^{EM,p}_i - F^{EM,n}_i, \quad \text{where} \quad i = 1, 2. $$
The superscripts \( p \) and \( n \) in the above equations stand for proton and neutron, respectively.

One can combine the Dirac and Pauli electromagnetic form factors to define the Sachs form factors,

\[
G_E = F_1^{EM} - \tau F_2^{EM},
\]
\[
G_M = F_1^{EM} + F_2^{EM}.
\]

According to scattering theory, the electric charge density distribution and the current density distributions are derived from the three dimensional Fourier transform of \( G_E(Q^2) \) and \( G_M(Q^2) \), respectively. In terms of the momentum transferred \( (Q^2) \) we can express the form factors as:

\[
F_1^{EM}(Q^2) = \frac{G_E(0) + \frac{Q^2}{4M^2}G_M(0)}{(1 + \frac{Q^2}{M^2})(1 + \frac{Q^2}{M^2})^2},
\]
\[
F_2^{EM}(Q^2) = \frac{G_M(0) - G_E(0)}{(1 + \frac{Q^2}{M^2})(1 + \frac{Q^2}{M^2})^2},
\]

where we use the fact that the experiments suggest that the \( Q^2 \) dependence is consistent
with the form factors having a dipole form,

\[
G_E^{Q^2} = \frac{G_E(0)}{(1 + \frac{Q^2}{M_V^2})}, \quad G_M^{Q^2} = \frac{G_M(0)}{(1 + \frac{Q^2}{M_V^2})}
\]

The vector mass, \( M_V = 0.843 \text{ GeV} \), is the same for both electric and magnetic form factors.
In the \( Q^2 \to 0 \) limit the form factors are normalized by the following conditions which give
the electric charge of the nucleon and the anomalous magnetic moment, respectively:

\[
G_E^p(0) = 1,
\]
\[
G_E^n(0) = 0,
\]
\[
G_M^p(0) = 1.793,
\]
\[
G_M^n(0) = -1.91,
\]
where again the superscripts $p$ and $n$ denote the proton and neutron, respectively. The axial isovector form factor is given by

$$F_A = \frac{F_A(0)}{\left(1 + \frac{Q^2}{M_A^2}\right)^2},$$

where $F_A(0) = g_A = 1.2671$ is measured precisely from neutron beta decay.

The axial vector mass $M_A$ is a bit of mystery. Previous measurements, which were mostly deuterium-based bubble chamber experiments, set a value of $M_A = 1.026 \pm 0.021$ GeV. Recent experiments on nuclear targets have reported $M_A$ values which are approximately 20-30% higher. MiniBooNE, using the charged-current quasi-elastic (CCQE) channel reported a value of $M_A = 1.35 \pm 0.17$ GeV [59]. Furthermore, in the neutrino mode NCE analysis a value of $M_A = 1.39 \pm 0.11$ GeV was reported [60], consistent with that from the CCQE channel.

Finally, the isoscalar form factors, $F_1^s$ and $F_2^s$, are contributions of the strange quarks to the electric charge and to the magnetic moment of the nucleon, and $F_A^s$ is the strange quark contribution to the nucleon spin. They are usually expressed in the dipole form, analogous to the isovector form factors discussed above:

$$F_1^s(Q^2) = \frac{F_1^s(0)}{(1 + \tau) \left(1 + \frac{Q^2}{M_V^2}\right)^2},$$

$$F_2^s(Q^2) = \frac{F_2^s(0)}{(1 + \tau) \left(1 + \frac{Q^2}{M_V^2}\right)^2},$$

$$F_A^s(Q^2) = \frac{F_A^s(0)}{\left(1 + \frac{Q^2}{M_A^2}\right)^2},$$

where $M_A$ and $M_V$ are assumed to have the same form as in the isovector case. For the
limiting case of zero momentum transfer we have

\[
F_s^1(0) = -\frac{1}{6} \langle r_s^2 \rangle, \\
F_s^2(0) = \mu_s, \\
F_A^s(0) = \Delta s.
\] (2.14)

where \( \langle r_s^2 \rangle \) is the strange radius, \( \mu_s \) is the strange magnetic moment of the nucleon, and \( \Delta s \) is the strange quark contribution to the nucleon spin.

Parity violating electron scattering experiments give us a measure of \( F_s^1 \) and \( F_s^2 \) and recent results show these to be consistent with 0. \( \Delta s \) can be extracted from neutrino-nucleus NCE experiment. The MiniBooNE neutrino mode NCE analysis reported a \( \Delta s \) consistent with 0.

![Figure 2.1: $\bar{\nu}$ quark level neutral current interaction. Plot (a) shows the the $\bar{\nu}$–proton interaction and (b) shows the interaction with the neutron.](image)

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2.5 MiniBooNE Neutral Current Elastic Cross Section

Using the vector and axial vector form factors the NCE neutrino nucleon cross section can
be written in the formalism of Llewellyn-Smith [61],
\[
\frac{d\sigma}{dQ^2} = \frac{G_F^2 Q^2}{2\pi E_\nu^2} \left[ A(Q^2) \pm B(Q^2) + C(Q^2)W^2 \right],
\]
where the + sign in front of the $B(Q^2)$ term is for neutrinos and − sign is for antineutrinos. $G_F$ is the Fermi constant, $W = 4E_\nu/M_N - Q^2/M_N^2$ with $M_N$ representing the nucleon mass, and $E_\nu$ is the energy of the incoming neutrino. The functions $A(Q^2)$, $B(Q^2)$ and $C(Q^2)$ contain the nucleon form factors:
\[
A(Q^2) = \frac{1}{4} \left[ (F_A^Z)^2 (1 + \tau) - ((F_1^Z)^2 - \tau(F_2^Z)^2)(1 - \tau) + 4\tau F_1^ZF_2^Z \right],
\]
\[
B(Q^2) = \frac{1}{4} F_A^Z (F_1^Z + F_2^Z),
\]
\[
C(Q^2) = -\frac{M_N^2}{16Q^2} \left[ (F_A^Z)^2 + (F_1^Z)^2 + \tau(F_2^Z)^2 \right],
\]
where $\tau = Q^2/4M_N^2$. $F_1$, $F_2$, and $F_A$ are the nucleon Dirac, Pauli, and axial form factors, and may be different for protons and neutrons.

2.6 Previous Neutral Current Elastic Cross Section Measurements

The first neutrino-nucleon NCE scattering experiments were conducted in 1976 by the Columbia-Illinois-Rockefeller and HPWF experiments. The BNL E734 experiment was the first experiment to measure the NCE scattering cross section on protons in both $\nu$ and $\bar{\nu}$ mode with high statistics [62]. BNL E734 was a 170 ton high-resolution target detector on the BNL AGS source. The proton beam had an energy of 28 GeV and resulted in neutrinos and antineutrinos of mean energy 1.3 GeV and 1.2 GeV respectively. The NCE flux-averaged
cross section is shown in Fig. 2.2. The experiment obtained a total of 1,686 neutrino proton scattering events and 1,821 antineutrino proton scattering events.

Figure 2.2: Neutrino and antineutrino cross section measurements as reported by the BNL E734 experiment – figure from Ref. [62].

The BNL E734 experiment also measured the parameter $\Delta s$, or to be precise, using their
NCE cross section data they obtained an allowed region for $\eta$ and $M_A$, where $\eta$ is directly related to $\Delta$, namely $\eta = -\Delta s/g_A$. The allowed regions at the 67% and 90% confidence levels, are shown in Fig. 2.3.

Figure 2.3: BNL E734 allowed region for $M_A$ and $\eta$ ($\eta = -\Delta s/g_A$) – figure from Ref. [62].
2.7 MiniBooNE Neutrino Neutral Current Elastic Cross Section Measurement

MiniBooNE collected $6.46 \times 10^{20}$ protons on target (POT) running in neutrino mode, resulting in 94,531 NCE events which passed the NCE selection criteria. This is the largest NCE sample collected to date, with an efficiency of 35% and purity of 65%. Here efficiency refers to the detector efficiency in discerning NCE events, and purity refers to the NCE composition of the sample.

After background subtraction MiniBooNE reported [60] a flux-averaged differential cross section in terms of momentum transferred squared to the nucleon, $Q_{QE}^2$, as illustrated in Fig. 2.4. Note that in MiniBooNE $Q_{QE}^2$ is the total kinetic energy of the outgoing nucleons in the interaction, assuming the target nucleon to be at rest:

$$Q_{QE}^2 = 2M_N \sum_i T_i = 2M_N T,$$

where $M_N$ is the nucleon mass, and $T$ is the sum of the kinetic energies of the final state nucleons. In MiniBooNE, $T$ is proportional to the total visible charge recorded by the photomultiplier tubes (PMTs) of the detector. This makes the MiniBooNE NCE cross section measurement less sensitive to final state interactions (FSI) as compared to tracking detectors – where low energy outgoing nucleons may not be fully visible.

Finally, it should be noted that the NCE scattering discussed here is off both bound nucleons in carbon and free nucleons in the hydrogen atom of the target mineral oil (CH$_2$).
A $\chi^2$ goodness of fit test was performed using the reconstructed NCE energy spectrum to find the set of $M_A$ and $\kappa$ (Pauli blocking scaling parameter) that best matches the data. Assuming $\Delta s=0$, the MiniBooNE NCE sample yields:

$$M_A = 1.39 \pm 0.11 \text{ GeV},$$

with $\chi^2_{\text{min}}/DOF = 26.9/50$.

Even though the ratio $\nu p \rightarrow \nu p$ to $\nu n \rightarrow \nu n$ is more sensitive to $\Delta s$ [63] than the ratio of $\nu p \rightarrow \nu p$ to $\nu N \rightarrow \nu N$ (where $N$ is any nucleon, either $p$ or $n$), a neutron can only be detected in MiniBooNE if it has a further strong interaction with a proton, which at low energies is difficult to distinguish from single proton events. Hence a sample of single protons above 350 MeV (the Cherenkov threshold for protons in MiniBooNE) was used and the ratio
of $\nu p \to \nu p$ to $\nu N \to \nu N$ as a function of reconstructed nucleon energy from 350 MeV to 800 MeV was studied to measure $\Delta s$. Additionally looking at such a ratio reduces the effect of FSI$s$ and also some systematic errors. Assuming a value of $M_A = 1.39 \pm 0.11$ GeV, the $\chi^2$ tests of $\Delta s$ to the MiniBooNE measured $\nu p \to \nu p$ to $\nu N \to \nu N$ ratio gives:

$$\Delta s = 0.08 \pm 0.26,$$

with $\chi^2_{\text{min}}/DOF = 34.7/29$. This is consistent with the result obtained by the BNL E734 experiment [62].
Chapter 3

The MiniBooNE Experiment

In this chapter we start with the motivation for designing the experiment. We then describe the detailed setup for generating the neutrino/antineutrino flux. Next we give a description of the detector itself. Finally we describe our prediction for both the neutrino flux and the detector response.

3.1 Motivation

The Mini Booster Neutrino Experiment (MiniBooNE) [64] was proposed to verify or dismiss the possible indication for neutrino oscillations reported by the LSND experiment. In 1997 the Liquid Scintillator Neutrino Detector (LSND) experiment at the Los Alamos Meson Physics Facility, reported an excess of $87.9 \pm 22.4 \text{(stat)} \pm 6.0 \text{(syst)}$ $\bar{\nu}_e$ events in a $\bar{\nu}_\mu$ beam produced by the decay at rest of positive pions [65]. Assuming that this excess is due to $\bar{\nu}_\mu \rightarrow \bar{\nu}_e$ oscillations, the LSND signal corresponds to neutrino oscillations with $\Delta m^2 \sim 1 \text{eV}^2$, as shown in Fig. 3.1. This in turn suggests the existence of a new type of neutrino, as the solar and atmospheric neutrinos already set two distinct values for the mass squared differences [1], namely

$$\Delta m_{sol}^2 = \Delta m_{21}^2 = (7.58^{+0.22}_{-0.26}) \times 10^{-5} \text{eV}^2$$
and

$$\Delta m_{atm}^2 = \Delta m_{31}^2 = (2.35^{+0.12}_{-0.09}) \times 10^{-3} \text{eV}^2.$$ 

Therefore, this new neutrino would have to be sterile, and consequently would point to significant new physics beyond the Standard Model.

In order to be sensitive to the same values of $\Delta m^2$, MiniBooNE was designed to have a similar average value of $L/E$ as LSND, where $L = 32$ m and $E_{avg} \simeq 45$ MeV. However, MiniBooNE operates at higher energies and longer baseline, namely $E_{avg} \simeq 700$ MeV and $L = 545$ m, respectively, which allows for a cross check of the LSND signal, with completely different signal and backgrounds.
Figure 3.1: The LSND signal. The plot shows the $(\sin^2 2\theta, \Delta m^2)$ favored regions obtained from the $\bar{\nu}_\mu \rightarrow \bar{\nu}_e$ decay at rest oscillations search. The dark-shaded region correspond to 90% likelihood and the light-shaded region correspond to 99% likelihood. Also shown are the 90% confidence limits from the KARMEN experiment (dashed), BNL-E776 (dotted), and the Bugey reactor experiment (dot-dashed). Figure taken from Ref. [66].

After 10 years of continuous running, MiniBooNE has not been able to clearly confirm or dismiss the LSND signal. Small excesses have been reported in both the neutrino and antineutrino oscillation channels, but they remain below the $3\sigma$ level [67, 68, 69]. MiniBooNE has stopped running as of April 24, 2012. Nonetheless, despite the fact that the primary purpose of MiniBooNE was to search for neutrino oscillations, the detector has proven to be very well suited to measure a variety of neutrino cross sections, most of which to yield the best measurements in the world.
3.2 The MiniBooNE Experiment

MiniBooNE is located at the Fermi National Accelerator Laboratory (FNAL, or Fermilab) in Batavia, IL. The experiment began collecting data in 2001 and reported the neutrino mode $\nu_\mu \to \nu_e$ oscillation search result in 2007 [67]. Since then it has been running in the antineutrino mode looking for $\bar{\nu}_\mu \to \bar{\nu}_e$ oscillations, which is a direct search of the LSND result. Initial antineutrino mode results were published in 2010 [69].

The experimental layout is shown in Fig. 3.2. Protons from the Fermilab Booster are extracted and impinge upon a beryllium target. The resulting mesons decay in flight to neutrinos in the decay region and reach the MiniBooNE detector. A detailed description of the detector hardware can be found in Ref. [70].

3.3 The MiniBooNE Neutrino Beam

Like any other neutrino oscillations experiment, MiniBooNE requires a high neutrino flux and an accurate knowledge of the flux composition at the same time. The MiniBooNE flux production can be divided into 3 stages: the primary proton beam extracted from the Booster, the secondary meson beam which is the result of proton-target interaction, and finally the tertiary neutrino beam which results from the meson decay. The rest of this section describes each of these stages in detail.
3.3.1 Primary Proton beam

The primary protons begin their journey at the Cockroff-Walton generator where hydrogen gas is turned into $\text{H}^-\text{ ions}$ and accelerated out by the 750 keV electrostatic gap of the Cockroff-Walton generator. The next step is the linear accelerator (LINAC) which ramps up the $\text{H}^-\text{ ions}$ to 400 MeV kinetic energy. Right before entering the next accelerator, the Booster, the $\text{H}^-\text{ ions}$ pass through a stripping foil which converts them into $\text{H}^+\text{ ions}$ (protons). The Fermilab Booster is a 468 m circumference synchrotron where the proton beam kinetic energy is boosted to 8.89 GeV and sent towards the Main Injector via a transfer beamline. Beam extraction from the Booster ring is done in a single turn by a kicker magnet.

![Figure 3.3: The Booster neutrino beamline. Figure appears in Ref. [64]](image)

Each extracted collection of protons is called a spill. Each spill has, on average, $4 \times 10^{12}$ protons. The spills are not uniform in structure; the protons are divided into 81 bunches, each approximately 6 ns wide and 19 ns apart. The 81 bunches define the *microstructure*
of the beam; they combine to a *macrostructure* approximately 1.6 μs wide within a 19.2 μs window (as shown in Fig. 3.4). At the end of the transfer beamline, just before the Main Injector, a switch magnet diverts the spills to the Booster Neutrino Beamline (BNB). The BNB contains the MiniBooNE target, onto which the beam is focused using a series of dipole and focusing-defocusing magnets.

The beam position and width is known to within 0.1 mm due to the beam position monitor (BPM) and a multiwire chamber. The beam current is measured by two toroids upstream of the target. Together they can measure the number of protons on target (POT) to within 2%.

**Figure 3.4:** The microstructure (a) and macrostructure (b) of the proton beam.

### 3.3.2 Secondary meson beam

The MiniBooNE target consists of seven cylindrical beryllium slugs, which add up to 71.12 cm in total length. The slugs are enclosed in two beryllium tubes enclosed by a beryllium cap. The protons impinging on the beryllium target create a shower of secondary particles,
mostly pions ($\pi^+$ and $\pi^-$) and kaons ($K^+, K^+$, and $K^0$). The proton target interaction generates heat which necessitates continuous cooling of the target. The target is air cooled by circulating air between the slugs via tubes which open into the target assembly.

![The MiniBooNE magnetic focussing horn. Also seen are the plumbing for water cooling. Figure from Ref. [71], courtesy of Bartoszek Engineering [72]](image)

**Figure 3.5:** The MiniBooNE magnetic focussing horn. Also seen are the plumbing for water cooling. Figure from Ref. [71], courtesy of Bartoszek Engineering [72]

The whole target assembly is placed in a pulsed electromagnet called the “horn”, as shown in Fig. 3.5. The horn is a toroidal electromagnet which sign selects the positive or negative mesons depending on the direction of current flow. The magnetic field additionally increases the neutrino flux at the detector by a factor of 6. The horn operates on a 173 kA peak current resulting in a peak magnetic field of 1.5 T. The horn also has additional plumbing to water cool itself. A collimator located downstream from the horn removes large angle particles before the next stage.

### 3.3.3 Tertiary neutrino beam

After passing through the collimator the secondary meson beam enter the decay pipe. It is a 2 m wide and 50 m long air-filled decay region where the mesons decay in flight (DIF) to
neutrinos. The primary source of neutrino is the decay of pions and kaons. At the end of the decay pipe there is a steel and concrete beam stop to stop all particles except neutrinos to pass through. After exiting the decay region the neutrinos travel through about 540 m of dirt. This is the oscillation region where the neutrino oscillation can take place before the beam reaches the detector.

3.4 The MiniBooNE Neutrino Flux

MiniBooNE employs the GEANT4 simulation package [73] to model the neutrino flux. GEANT (GEometry ANd Tracking) uses Monte Carlo methods to describe the passage of elementary particles through matter. The framework can account for energy losses and electromagnetic and hadronic processes that alter the kinematics of the propagating particles. Within each medium, Coulomb scattering and energy loss are calculated in each step of the tracking and particle trajectory updated accordingly. GEANT4 is also capable of tracking charged particles in a magnetic field.

GEANT4 accepts as input the full geometry of the domain to be simulated, as well as the initial conditions of the particles.

The GEANT4 geometry consists of the last 50 m of the booster beamline, the MiniBooNE target hall, and the meson decay volume. It specifies the shape, location and composition of the components of BNB through which the the primary protons and other particles propagate. The geometry description is defined to match the actual beamline as closely as possible, with simplifications made which are not expected to affect the flux predictions.

The initial conditions of particles used for GEANT4 input depends on the specific process in the beamline and comes from a combination of sources which includes other particle production software, external measurements by MiniBooNE or other experiments in similar energy regime, theoretical predictions, and sometimes extrapolation of measurements to MiniBooNE energies. The details for each of the processes are discussed below.
3.4.1 Modelling the Primary Proton Beam and Horn

The beam optics characteristics are used to generate the primary protons before the target and the TRANSPORT software package [74] was used to simulate properties like position and profile. The rate of interactions for protons, neutrons, and charged pions on beryllium and aluminum are determined by customized cross section tables. The cross sections for these particles fall into three categories: elastic scattering, inelastic scattering, and quasielastic scattering. The Glauber model [75] was used to calculate the total cross section and subtracting the measured inelastic cross section to give the elastic cross section. In the case of inelastic scattering, available measurements for p-Be and p-Al, in the momentum range of MiniBooNE exist [76]. For quasi-elastic scattering, very few measurements are available, hence we make use of theoretical calculations. The calculation along with the sparse measurements are extrapolated for beryllium. For explicit forms of the cross sections which are inspired by the Regge theory [77], see Ref. [78].

3.4.2 Secondary Particle Production Model

Of special interest to MiniBooNE is the p-Be interaction at 8.89 GeV. Most of the neutrinos seen by MiniBooNE come from the decay of $\pi^+$ and $\pi^-$ and other associated secondaries of the p-Be interaction at this particular energy. The HARP experiment [79] at CERN studied the pion production on a replica Be target at MiniBooNE energy. The HARP measurements were used to generate the $\pi^{\pm}$ production tables and a Sanford and Wang model [80] was used to parametrize the differential production cross section at different incident primary beam momenta and extrapolate it to regions where production data do not exist.

The Sanford-Wang parametrization is given by

$$\frac{d^2\sigma}{dpd\Omega} = c_1p^{c_2} \left( 1 - \frac{p}{p_B - c_3} \right) \exp \left[ -c_3 \frac{p^{c_4}}{p_B^{c_5}} - c_6\theta(p - c_7p_B \cos c_8 \theta) \right], \quad (3.1)$$

where $p_B$ is the incident proton beam momentum, $p$ is the outgoing meson momentum, and
θ is the outgoing meson direction relative to the proton direction. Fits to the available measurements of the differential cross section $d^2\sigma/dpd\Omega$ were done using a $\chi^2$ minimization to determine the $c_1$–$c_9$ Sanford-Wang parameters for each meson. Figure 3.6 shows data from the HARP experiment fit to the Sanford-Wang parametrization above.

Data from the BNL E910 experiment [81] which measured $\pi^\pm$ differential cross section for p-Be interaction at different energies was used to cover the energy regime not covered by the HARP data.

For $K^+$ production, since no measurements at 8.89 GeV exist, measurements by other experiments [82, 83] close to 8.89 GeV are used and the Feynman scaling hypothesis is employed to extrapolate to MiniBooNE energies. The $K^0$'s have an equal content of $K^0_L$'s and $K^0_S$'s. The long lifetime of $K^0_L$'s reduces the neutrino contribution and the $K^0_S$'s production properties can be measured from the external measurements [84]. Once again, a Sanford-Wang...
Wang parametrization of these data was employed to extrapolate to MiniBooNE energies and constrain the neutral kaons.

Neutrino flux contributions from $K^+$ and other semileptonic hyperon decays (e.g., $\Lambda, \Sigma$) are negligible. In the absence of measured data, the MARS hadronic interaction package [85] was used to estimate the $K^+$ production. The FLUKA simulation package [86] was used to constrain the semileptonic hyperon decays.

The results of the neutrino flux simulations are shown in Fig. 3.7 for both the neutrino and antineutrino running modes.
Figure 3.7: The MiniBooNE flux predictions for the neutrino and antineutrino modes, top and bottom, respectively. The solid lines show the $\nu_\mu$ (black) and $\nu_e$ (red) while the dashed lines show the $\bar{\nu}_\mu$ (dashed black) and $\bar{\nu}_e$ (dashed red). Note the neutrino background in the antineutrino mode is higher than the corresponding antineutrino background in the neutrino mode. Figure taken from Ref. [78]
3.5 The MiniBooNE Detector

The MiniBooNE detector is a mineral oil Cherenkov detector, as shown schematically in Fig. 3.8. It is a 610 cm radius sphere with two optically isolated regions separated by a spherical shell of radius 575 cm. The inner region, also referred to as the *signal* region is lined with 1,280 8-inch photomultiplier tubes (PMTs) pointed inwards. The outer region, which is the *veto* region, has 240 PMTs arranged in back-to-back pairs pointed along the circumference of the detector. The signal region is painted black to minimize reflections, whereas the veto region is painted white in order to maximize light collection at the PMTs.

![Figure 3.8: A schematic of the MiniBooNE detector. From Ref. [87].](image)

Figure 3.9 shows a snapshot of the signal and veto regions of the detector, which also illustrates the PMT orientations in the two volumes.
Figure 3.9: A snapshot of the signal and veto regions. Note the orientations of the PMTs in the two regions and the colors of the two regions – the signal region is painted black to minimize reflections, whereas the veto region is painted white to maximize light collection.

The detector is supported by six steel legs and is situated in a vault at about 545 m from the MiniBooNE target. The area above the vault houses the detector electronics and DAQ systems, as well as the pumps for oil circulation. The entire assembly is buried under approximately 3 m earth equivalent of overburden – see Fig. 3.10. This overburden reduces somewhat the number of cosmic muons entering the detector (however, the main reduction of the cosmic-ray backgrounds comes from the shortness of the beam spills). Further details of the MiniBooNE detector can be found in Ref. [70].
Figure 3.10: A schematic of the MiniBooNE detector in the vault. Also shown is the electronics room at the surface level, the location of the overflow tank, and the overburden. From Ref. [87].

3.5.1 The MiniBooNE Target–Mineral oil

The detector is filled with 807 tons of Marcol-7 (produced by EXXON/MOBIL) mineral oil which functions as the target for the neutrino beam as well as the medium for light production. The choice of this particular detector medium was driven by various physics goals of MiniBooNE.

Mineral oil has a higher index of refraction ($n = 1.47$) as compared to water ($n = 1.33$) which improves the sensitivity to lower energy particles like protons and corresponds to higher Cherenkov yields. Having an index of refraction closely matching that of the PMT glass ($n \approx 1.5$) also minimizes the losses through reflections. A lower Cherenkov threshold for heavy particles like protons allows to measure their direction. Mineral oil also has low $\mu^-$ capture rate as compared to water. This improves our ability to identify charged current neutrino interactions as we rely on the Michel electron from the $\mu^-$ decay for tagging such
events. The light extinction length of the MiniBooNE oil is approximately 18 m.

Detailed studies of the various properties of the oil were carried out. As an example, the temperature and wavelength dependence of the refractive index were measured using an Abbe refractometer, to yield [88]

\[
n(\lambda, T) = \left[ n_D + B \left( \frac{1}{\lambda^2 - \lambda_D^2} \right) \right] \left[ 1 - \beta(T - T_0) \right],
\]

where the index of refraction was measured at the mean of the Fraunhofer \( D_1 \) and \( D_2 \) lines – the sodium doublet \( \lambda_D = 589.3 \) nm. Here \( n_D = 1.4684 \pm 0.0002 \), \( B = 42040 \pm 157 \) nm\(^2\), \( \beta = (3.66 \pm 0.04) \times 10^{-4}/^\circ\)C, and \( T_0 = 20^\circ\)C. Details of all studies performed on the MiniBooNE mineral oil can be found in Ref. [89].

Nitrogen gas is continuously bubbled through the oil so as to purge it of oxygen, which is corrosive for the detector structure, and a nitrogen environment is maintained within the detector. Mineral oil needs no continuous purification like water; nothing grows in it and once it is clean, any remaining impurities will either float to the surface or sink to the bottom of the detector. An overflow tank is provided to cope with any thermal expansion of the oil.

### 3.5.2 The Photomultiplier Tubes

A total of 1,520 PMTs are used in the MiniBooNE detector. Of these, 1,198 are Hamamatsu R1408 recycled from the LSND experiment, and the remaining 322 are Hamamatsu R5912 purchased specifically for MiniBooNE. Figure 3.11 shows an inner region PMT with the supporting steel wire structure.
Both the R1480 and the R5912 PMTs, referred to as old and new PMTs, respectively, are of 8 inch in diameter and have similar geometry and quantum efficiency; the new PMTs however have a slightly higher light collection efficiency. Since the new PMTs have a better time resolution $\sim 1.1$ ns and a better single photoelectron (SPE) charge resolution (about 50%) as compared to the old ones (with a time resolution of 1.7 ns and a SPE charge resolution of about 140%), all the new PMTs are equally dispersed in the signal region. In the veto region 240 of the old PMTs with the lowest dark rate are used. Figure 3.13 shows the layout of old and new PMTs in the detector.

All the PMTs were tested at Fermilab in a dark room to study their time and charge resolution, dark rate, angular acceptance and operating voltage. Details on the PMT design and testing can be found in Refs. [90, 91].
Figure 3.12: The MiniBooNE PMT support structure. Also shown is the location and orientation of the veto PMTs. From Ref. [87].

Figure 3.13: Distribution of the old and new PMTs within the MiniBooNE detector, as labeled. From Ref. [87].
3.6 Data Acquisition, Digitization and Trigger

In the MiniBooNE data acquisition (DAQ), the digitization of signals and data storage is achieved in conjunction with a trigger system, which is a set of conditions which, when true, stores the corresponding information in the DAQ system as data. We describe below how the data acquisition and digitization is achieved followed by a brief description of the trigger system.

3.6.1 Data Acquisition and Digitization

The MiniBooNE data acquisition and associated systems are housed in the detector hall above the vault where the detector is situated. High voltage (HV) to the PMTs and the signals from them to be digitized are carried by equal length cables. The overall charge and time associated with each PMT hit is recorded.

A schematic of the charge and time information is shown in Fig. 3.14. The system is driven by a 10 MHz clock. The preamplified PMT signal $V_{pmt}$ is continuously integrated via a capacitive circuit in the so-called QT boards, with an exponential decay time of about 1200 ns, generating a second signal $V_{q}$. If the PMT signal $V_{pmt}$ exceeds 0.25 photoelectron equivalent, a PMT discriminator signal is activated, and a linear time ramp $V_{t}$ is started. The time signal $V_{t}$ is also continuously digitized every 100 ns. The time ramp is reset to baseline when two 100 ns time intervals are elapsed after the PMT signal crossed threshold. The linear extrapolation of the $V_{t}$ and $V_{t+1}$ values to the baseline allows to determine the so-called “fine time”, i.e., the hit time.

The charge and time ADC (Analog-to-Digital Converter) values are stored in 204.8 µs circular dual port buffers. If the trigger system (explained below) responds to the stored charge and time, the values are passed on to storage, otherwise they are overwritten. For each PMT hit four consecutive values of $V_{q}$ and $V_{t}$ (each of them therefore called a quad) are stored in the buffer. These quads are later used to calculate the charge and time of the
hit PMT’s, if the event is read out.

**Figure 3.14:** A schematic diagram of MiniBooNE signal processing. The schematic appears in Ref. [87]

### 3.6.2 The Trigger System

The MiniBooNE trigger system is a set of conditions which, when true, instructs the DAQ system to store the information currently in the buffer. The trigger system collects information from 3 external triggers, as well as seven comparators in a 200\,ns window. The external sources are two from the accelerator and one from the calibration systems; the comparator levels correspond simply to seven different levels of PMT hit multiplicities. Details of
MiniBooNE external triggers and comparator settings are as listed in Table 3.1.

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<th>PMT hits</th>
<th>Purpose</th>
</tr>
</thead>
<tbody>
<tr>
<td>External 1</td>
<td>n/a</td>
<td>Beam to MiniBooNE</td>
</tr>
<tr>
<td>External 2</td>
<td>n/a</td>
<td>Strobe, NuMI, Debuncher</td>
</tr>
<tr>
<td>External 3</td>
<td>n/a</td>
<td>Calibration Event</td>
</tr>
<tr>
<td>Comparator 1</td>
<td>Tank hits $\geq 10$</td>
<td>Activity Monitor</td>
</tr>
<tr>
<td>Comparator 2</td>
<td>Tank hits $\geq 24$</td>
<td>Michel electron</td>
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<td>Tank hits $\geq 200$</td>
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</tr>
<tr>
<td>Comparator 4</td>
<td>Tank hits $\geq 100$</td>
<td>$\nu$ candidate</td>
</tr>
<tr>
<td>Comparator 5</td>
<td>Tank hits $\geq 60$</td>
<td>Supernova $\nu$ candidate</td>
</tr>
<tr>
<td>Comparator 6</td>
<td>Tank hits $\geq 6$</td>
<td>Cosmic Veto</td>
</tr>
<tr>
<td>Comparator 6</td>
<td>Tank hits $\geq 4$</td>
<td>Cosmic Activity</td>
</tr>
</tbody>
</table>

Table 3.1: MiniBooNE trigger inputs and comparator settings. From Ref. [87]

The principal physics trigger requirement is that beam was sent to the MiniBooNE target, regardless of the activity in the detector. When this trigger is set, any activity in the detector before and after the beam spill is recorded. When the beam trigger is set, $19.2 \, \mu s$ of data are read beginning $5 \, \mu s$ before the beam arrives. There are also a number of special purpose triggers for calibration (such as the Michel electron, laser, or strobe trigger) or to record various physics event samples (such as the NuMI or supernova trigger). The detector takes data for a $19.2 \, \mu s$ window of which $1.6 \, \mu s$ is the beam time. The beam-off data recorded during the remaining $17.6 \, \mu s$ is used to remove the cosmic ray event contamination – see Fig. 3.4(b). Additionally, there is also a cosmic trigger (Comparator 6 in Table. 3.1) which is used to ignore cosmic ray contaminated data during beam up-time.
3.7 Calibration

MiniBooNE employs two *in situ* calibration tools: a pulsed laser calibration system and a cosmic muon calibration system. In addition, calibration is also done by using MiniBooNE data to reconstruct certain known physical quantities, such as the $\pi^0$ mass and the Michel electron energy spectrum. This section describes these methods in some detail.

Figure 3.15: Schematic of the MiniBooNE laser calibration system. From Ref. [87]
3.7.1 Laser Calibration System

The laser calibration system consists of a pulsed diode laser and four dispersion flasks, installed at various locations in the detector (see Fig. 3.15). Optical fibers connect the laser to the dispersion flasks through which short light pulses (<1 ns) with a peak wavelength of 397 nm is transmitted. The dispersion flasks, each 10 cm in diameter, are filled with Ludox colloidal silica for uniform light dispersion. In addition to the four flasks there is also a bare optical fiber that emits light in a cone of about 10° opening angle illuminating PMTs in a small circle near the bottom of the detector.

The primary purpose of the laser system is to quantify and monitor individual PMT performance parameters. The raw charge and time information for each PMT, as described in the previous section, are converted to calibrated charge and time using the information provided by the analysis of the laser calibration data. This quantities, called calibration constants (gains and time offsets, respectively), are used to account for individual differences in the charge and time response among the PMTs.

In addition, the laser system also allows for in situ monitoring of the oil parameters over the lifetime of the experiment.

3.7.2 Muon Calibration System

Muon decay is a well known physical process which results in a neutrino-antineutrino pair and an electron, with a decay time of 2.2 µs (in vacuum):

\[
\mu^- \rightarrow e^- + \bar{\nu}_e + \nu_\mu \quad \text{or} \quad \mu^+ \rightarrow e^+ + \nu_e + \bar{\nu}_\mu. 
\]

For decays at rest, the resulting electron (also called a Michel electron) has a continuous energy spectrum of a precisely known shape

\[
f(E) = x^2(x - 1) \quad \text{where} \quad x = \frac{E}{E_{\text{end}}}
\]
with an end-point energy of \( E_{\text{end}} = 52.8 \text{ MeV} \) (half the muon mass if we neglect the electron mass) – see Fig. 3.17. MiniBooNE uses a muon calibration system where the muon decay spectrum has been used extensively to tune and verify not only the Monte Carlo simulations, but also the event reconstruction algorithms.

The muon calibration system consists of a scintillator hodoscope placed above the detector and seven scintillator cubes deployed within the detector. The hodoscope has two layers of plastic scintillator, each with an \( x \) and \( y \) plane, to determine the position and directions of muons entering the detector. The scintillator cubes are placed at various distances from the optical barrier. The cubes are connected by optical fibers to a 1 inch PMT for readout. A muon entering the detector passes through the tracker and stops in a scintillation cube and decays. The Cherenkov light produced by the muon is seen by the PMTs as well as the scintillation cube. The decay electrons are also seen by the tank PMTs. Those events where the location and momentum of the muon and the origin of the electron can be determined by the muon hodoscope help in tuning and verifying the reconstruction algorithms.
Figure 3.16: Muon energy calibration with the cosmic muon calibration system. The $x$-axis shows the energy calculated using the stopping muon range tables and the $y$-axis shows the reconstructed energy assuming an electron hypothesis (no dedicated muon fitters were available when these calibration measurements were first performed. The size of the circles indicates the size of the error bars. From Ref [92]

3.7.3 Michel Electron Calibration

As mentioned before, the muon decay is a well studied process with a known spectrum which is used in the muon calibration system in MiniBooNE. Another aspect of muon decay is the fact that resultant Michel electrons have a well-known end point energy, $E_{\text{end}} = 52.8 \text{ MeV}$, which is used to calibrate electrons.

In MiniBooNE a muon candidate event generates more than 200 hits in the main tank and more than 6 hits in the veto PMTs. The subsequent Michel electron is recorded after an average delay of about $2.2 \mu$s with a main tank multiplicity below 200 and veto hit multiplicity below 6. Figure 3.17 shows the observed spectrum of Michel electron candidate events together with the best fit to the data. The smearing in the spectrum is due to the limited energy resolution. From a fit around the end point the energy resolution was
determined to be about 14.8% in this energy regime.

Figure 3.17: Michel electron reconstructed energy spectrum (gray) and the best fit (red), obtained by smearing the Michel electron kinetic energy spectrum with a Gaussian of width proportional to $\sqrt{E}$.

### 3.7.4 Neutral Pion Mass Calibration

The reconstructed $\pi^0$ mass (referred to as $M_{\gamma\gamma}$ henceforth), as calculated from the beam-induced neutral current $\pi^0$ events, is another calibration employed in MiniBooNE. The $\pi^0$ meson (with a rest mass of 135 MeV) decays almost immediately after production (decay time $8.4 \times 10^{-17}$ s), via the following modes:

$$\pi^0 \rightarrow \gamma + \gamma \quad \text{(branching fraction 98.987%)}$$

$$\pi^0 \rightarrow \gamma + e^- + e^+ \quad \text{(branching fraction 1.198%)}.$$

The resulting gammas convert into electron-positron pairs after travelling $\sim 0.5$ m and produce an electromagnetic shower in the detector emitting both Cherenkov and scintillation light. The electrons (assumed massless) also retain the same direction as the original gamma as the gamma is massless.
The $\pi^0$ $M_{\gamma\gamma}$ distribution is used to calibrate photons in the energy range between 50 MeV and 350 MeV. Fig. 3.18 shows the comparison between the reconstructed $M_{\gamma\gamma}$ distributions for data and Monte Carlo in various $\pi^0$ momentum bins. Details of NC $\pi^0$ sample selection and reconstruction (including 4-vertex, directions of the two gammas, their conversion lengths and energies) are given in Ref. [93].

Figure 3.18: NC $\pi^0$ mass calibration. The plots show reconstructed $M_{\gamma\gamma}$ distributions for data (black points with statistical error bars) along with the uncorrected (dashed histogram) and corrected MC (red) with systematic errors in bins of reconstructed $\pi^0$ momentum from 0 GeV/c to 1.5 GeV/c. Also shown are the MC estimate for NC $\pi^0$ backgrounds (blue). From Ref. [93]
3.8 The MiniBooNE Cross section model

Neutrino interaction rates, products, and their kinematics in the MiniBooNE detector are predicted using a neutrino event generator which is based on the NUANCE v3 [94], but has been customized to the MiniBooNE experiment. The various parameters within the generator are tuned to the current best-known cross section information. It accepts as input the neutrino flux prediction described in §3.4, as well as the detector target material and geometry. The mineral oil target is simulated as CH$_2$ with a density of 0.845 g/cm$^3$. NUANCE can simulate 99 distinct neutrino/antineutrino interactions, in a wide energy range (100 MeV to $10^3$ GeV). Tables 3.2 and 3.3 list the interaction processes simulated by NUANCE along with the channel numbers. Table 3.4 lists the cross section parameters and the assigned uncertainties used in the MiniBooNE cross section model.

The following sections describe in detail the interaction channels important for this analysis:

3.8.1 Neutral Current Elastic Scattering

Antineutrino NCE scattering, the signal for this analysis, and the neutrino NCE scattering background, both correspond to channel #2 in NUANCE. The neutrino scattering off of six bound nucleons in the carbon atom and two free protons in hydrogen atom of the MiniBooNE target CH$_2$ is modelled by different methods in NUANCE. For the scattering off free protons, the Llewellyn-Smith formalism [61] (described in §2.2) is used, while for bound nucleons the relativistic Fermi gas (RFG) model of Smith and Moniz [95] is used.

The vector form factors are taken from Ref. [96], while other form factors are customized as follows: the isoscalar form factor is taken to be $\Delta s=0$, while the axial vector mass is

- $M_A = 1.23$ GeV for scattering off bound nucleons (taken from MiniBooNE CCQE measurement [59]),
- $M_A = 1.13$ GeV for scattering off free protons. This corresponds to the average between
the value obtained from deuterium-based CCQE measurements ($M_A = 1.03 \text{ GeV}$) and
the MiniBooNE CCQE measurement above.

### 3.8.2 Charged Current Elastic Scattering

**NUANCE** channel#1 corresponds to both neutrino and antineutrino CCQE interactions which
are a background for this analysis. The neutrino CCQE interaction happens off neutrons
($\nu_\mu + n \rightarrow \mu^- + p$) in the bound carbon atom, hence the Smith-Moniz [95] formalism is
employed, whereas the antineutrino CCQE happens off protons ($\bar{\nu}_\mu + p \rightarrow \mu^+ + n$) which
are both free (H atom) and bound (C atom), hence a combination of the Llewellyn-Smith
and Smith-Moniz formalism is used as in the case of NCE scattering. The CCQE scattering
model is similar to the NCE scattering model described in §2.2 with the difference that
the form factors do not include additional coupling factors and contributions from strange
quarks.

The form factors have the same values as in the NCE case, i.e., the axial vector mass
$M_A = 1.23 \text{ GeV}$ for the bound nucleons and $M_A = 1.13 \text{ GeV}$ for the free nucleons.

Finally, a Pauli blocking scaling parameter $\kappa = 1.022$ is used here, which modifies the
shape of the CCQE cross section at low values of momentum transfer. See ref [59] for details.
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<td>$\nu_\mu n \rightarrow \nu_\mu n$</td>
<td></td>
<td>41</td>
<td>CC</td>
<td>$\nu_\mu n \rightarrow \mu^- n p^+(770)$</td>
</tr>
<tr>
<td></td>
<td></td>
<td>($\overline{\nu}<em>\mu n \rightarrow \overline{\nu}</em>\mu n$)</td>
<td></td>
<td>42</td>
<td>NC</td>
<td>$\nu_\mu p \rightarrow \nu_\mu p n^0(770)$</td>
</tr>
<tr>
<td></td>
<td></td>
<td>$\nu_\mu p \rightarrow \nu_\mu p$</td>
<td></td>
<td>43</td>
<td>NC</td>
<td>$\nu_\mu p \rightarrow \nu_\mu n p^+(770)$</td>
</tr>
<tr>
<td></td>
<td></td>
<td>($\overline{\nu}<em>\mu p \rightarrow \overline{\nu}</em>\mu p$)</td>
<td></td>
<td>44</td>
<td>NC</td>
<td>$\nu_\mu n \rightarrow \nu_\mu n n^0(770)$</td>
</tr>
<tr>
<td></td>
<td></td>
<td></td>
<td></td>
<td>45</td>
<td>NC</td>
<td>$\nu_\mu n \rightarrow \nu_\mu n p^0(770)$</td>
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<tr>
<td></td>
<td></td>
<td>Resonant single pion</td>
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<td>46–52</td>
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<td>Corresponding $\overline{\nu}_\mu$ processes</td>
</tr>
<tr>
<td></td>
<td></td>
<td>production</td>
<td></td>
<td></td>
<td></td>
<td></td>
</tr>
<tr>
<td>3</td>
<td>CC</td>
<td>$\nu_\mu p \rightarrow \mu^- p \pi^+$</td>
<td></td>
<td>53</td>
<td>CC</td>
<td>$\nu_\mu p \rightarrow \mu^- \Sigma^+ K^+$</td>
</tr>
<tr>
<td>4</td>
<td>CC</td>
<td>$\nu_\mu n \rightarrow \mu^- p \pi^0$</td>
<td></td>
<td>54</td>
<td>CC</td>
<td>$\nu_\mu n \rightarrow \mu^- \Sigma^0 K^+$</td>
</tr>
<tr>
<td>5</td>
<td>CC</td>
<td>$\nu_\mu n \rightarrow \mu^- n \pi^+$</td>
<td></td>
<td>55</td>
<td>CC</td>
<td>$\nu_\mu n \rightarrow \mu^- \Sigma^+ K^0$</td>
</tr>
<tr>
<td>6</td>
<td>NC</td>
<td>$\nu_\mu p \rightarrow \nu_\mu p \pi^0$</td>
<td></td>
<td>56</td>
<td>NC</td>
<td>$\nu_\mu p \rightarrow \nu_\mu \Sigma^0 K^+$</td>
</tr>
<tr>
<td>7</td>
<td>NC</td>
<td>$\nu_\mu p \rightarrow \nu_\mu n \pi^+$</td>
<td></td>
<td>57</td>
<td>NC</td>
<td>$\nu_\mu n \rightarrow \nu_\mu \Sigma^+ K^0$</td>
</tr>
<tr>
<td>8</td>
<td>NC</td>
<td>$\nu_\mu n \rightarrow \nu_\mu n \pi^0$</td>
<td></td>
<td>58</td>
<td>NC</td>
<td>$\nu_\mu n \rightarrow \nu_\mu \Sigma^0 K^0$</td>
</tr>
<tr>
<td>9</td>
<td>NC</td>
<td>$\nu_\mu n \rightarrow \nu_\mu n \pi^-$</td>
<td></td>
<td>59</td>
<td>NC</td>
<td>$\nu_\mu n \rightarrow \nu_\mu \Sigma^- K^+$</td>
</tr>
<tr>
<td>10–16</td>
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<td>Corresponding $\overline{\nu}_\mu$ processes</td>
<td></td>
<td>60–66</td>
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<td>Corresponding $\overline{\nu}_\mu$ processes</td>
</tr>
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<td></td>
<td></td>
<td>67</td>
<td>CC</td>
<td>$\nu_\mu n \rightarrow \mu^- p \eta$</td>
</tr>
<tr>
<td></td>
<td></td>
<td></td>
<td></td>
<td>68</td>
<td>NC</td>
<td>$\nu_\mu p \rightarrow \nu_\mu p \eta$</td>
</tr>
<tr>
<td></td>
<td></td>
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<td></td>
<td>69</td>
<td>NC</td>
<td>$\nu_\mu n \rightarrow \nu_\mu n \eta$</td>
</tr>
<tr>
<td></td>
<td></td>
<td></td>
<td></td>
<td>70–72</td>
<td></td>
<td>Corresponding $\overline{\nu}_\mu$ processes</td>
</tr>
<tr>
<td></td>
<td></td>
<td></td>
<td></td>
<td>73</td>
<td>CC</td>
<td>$\nu_\mu n \rightarrow \mu^- K^+ \Lambda$</td>
</tr>
<tr>
<td></td>
<td></td>
<td></td>
<td></td>
<td>74</td>
<td>NC</td>
<td>$\nu_\mu p \rightarrow \nu_\mu K^+ \Lambda$</td>
</tr>
<tr>
<td></td>
<td></td>
<td></td>
<td></td>
<td>75</td>
<td>NC</td>
<td>$\nu_\mu n \rightarrow \nu_\mu K^0 \Lambda$</td>
</tr>
</tbody>
</table>

Table 3.2: Processes available within NUANCE. The numbers in the leftmost column indicate the assigned reaction code (channel number) in NUANCE (continued on the next page).
<table>
<thead>
<tr>
<th>#</th>
<th>CC / NC</th>
<th>Reaction</th>
<th>#</th>
<th>CC / NC</th>
<th>Reaction</th>
</tr>
</thead>
<tbody>
<tr>
<td>76–78</td>
<td>CC / NC</td>
<td>Corresponding $\nu_\mu$ processes</td>
<td>96</td>
<td>NC</td>
<td>$\nu_\mu A \rightarrow \nu_\mu A \pi^0$</td>
</tr>
<tr>
<td>79</td>
<td>CC</td>
<td>$\nu_\mu n \rightarrow \mu^- p \pi^+ \pi^-$</td>
<td>97</td>
<td>CC</td>
<td>$\nu_\mu A \rightarrow \nu_\mu A \pi^+$</td>
</tr>
<tr>
<td>80</td>
<td>CC</td>
<td>$\nu_\mu n \rightarrow \mu^- p \pi^0 \pi^0$</td>
<td></td>
<td>NC</td>
<td>$\nu_\mu A \rightarrow \nu_\mu A \pi^0 \pi^0$</td>
</tr>
<tr>
<td>81</td>
<td>NC</td>
<td>$\nu_\mu p \rightarrow \nu_\mu p \pi^+ \pi^-$</td>
<td></td>
<td>NC</td>
<td>$\nu_\mu A \rightarrow \nu_\mu A \pi^+ \pi^-$</td>
</tr>
<tr>
<td>82</td>
<td>NC</td>
<td>$\nu_\mu p \rightarrow \nu_\mu p \pi^0 \pi^0$</td>
<td></td>
<td>NC</td>
<td>$\nu_\mu p \rightarrow \nu_\mu p \pi^0 \pi^0$</td>
</tr>
<tr>
<td>83</td>
<td>NC</td>
<td>$\nu_\mu n \rightarrow \nu_\mu n \pi^+ \pi^-$</td>
<td></td>
<td>NC</td>
<td>$\nu_\mu A \rightarrow \nu_\mu A \pi^+ \pi^-$</td>
</tr>
<tr>
<td>84</td>
<td>NC</td>
<td>$\nu_\mu n \rightarrow \nu_\mu n \pi^0 \pi^0$</td>
<td></td>
<td>NC</td>
<td>$\nu_\mu A \rightarrow \nu_\mu A \pi^+ \pi^-$</td>
</tr>
<tr>
<td>85–90</td>
<td>CC / NC</td>
<td>Corresponding $\nu_\mu$ processes</td>
<td></td>
<td></td>
<td>$\nu_\mu e \rightarrow \nu_\mu e$</td>
</tr>
<tr>
<td></td>
<td></td>
<td></td>
<td></td>
<td></td>
<td>$(\nu_\mu e \rightarrow \nu_\mu e)$</td>
</tr>
<tr>
<td></td>
<td></td>
<td></td>
<td></td>
<td></td>
<td>$\nu \nu$ inverse $\mu$ decay</td>
</tr>
<tr>
<td></td>
<td></td>
<td></td>
<td></td>
<td></td>
<td>$\nu_\mu e \rightarrow \mu^- \nu_e$</td>
</tr>
</tbody>
</table>

Table 3.3: Processes available within NUANCE (continued from the previous page). The numbers in the leftmost column indicate the assigned reaction code (channel number) in NUANCE.

<table>
<thead>
<tr>
<th>Parameter</th>
<th>Value</th>
<th>Uncertainty</th>
</tr>
</thead>
<tbody>
<tr>
<td>$M_A$ for QE events on carbon</td>
<td>1.2341 GeV</td>
<td>0.077 GeV</td>
</tr>
<tr>
<td>Binding energy for carbon</td>
<td>34.0 MeV</td>
<td>9.0 MeV</td>
</tr>
<tr>
<td>Fermi momentum for carbon</td>
<td>220.0 MeV</td>
<td>30.0 MeV</td>
</tr>
<tr>
<td>$\Delta s$, the axial vector isoscalar term</td>
<td>0.0</td>
<td>0.1</td>
</tr>
<tr>
<td>$M_A$ for CC and NC single pion events</td>
<td>1.1 GeV</td>
<td>0.27 GeV</td>
</tr>
<tr>
<td>$M_A$ for CC and NC multiple pion events</td>
<td>1.3 GeV</td>
<td>0.52 GeV</td>
</tr>
<tr>
<td>Scale factor for NC coherent $\pi^0$ events</td>
<td>1.302</td>
<td>0.14</td>
</tr>
<tr>
<td>Scale factor for NC and CC $\Delta$ radiative events</td>
<td>1.00</td>
<td>0.12</td>
</tr>
<tr>
<td>Scale factor for deep inelastic scattering events</td>
<td>1.00</td>
<td>0.25</td>
</tr>
<tr>
<td>Pauli blocking scale factor, $\kappa$</td>
<td>1.0220</td>
<td>0.0205</td>
</tr>
<tr>
<td>$M_A$ for CC single pion coherent events (not coherent NC $\pi^0$)</td>
<td>1.030 GeV</td>
<td>0.275 GeV</td>
</tr>
<tr>
<td>Scale factor for NC resonant $\pi^0$ events</td>
<td>1.00</td>
<td>0.14</td>
</tr>
<tr>
<td>$M_A$ for QE events on hydrogen</td>
<td>1.13 GeV</td>
<td>0.10 GeV</td>
</tr>
</tbody>
</table>

Table 3.4: Cross-section parameters and their 1-$\sigma$ uncertainties used in the MiniBooNE MC. Here the abbreviations are: QE = quasi-elastic, NC = neutral current, and CC = charge current.
3.8.3 Neutral-Current Single Pion Production

The neutral current single pion production channels (channels 6–9 for neutrinos and 10–16 for antineutrinos) are a major background for this analysis. In neutrino-nucleus interactions single pion production happens when a nucleon is excited to a resonant state and subsequently decays to a pion and a nucleon. The pions may experience absorption in the nucleus through final state interactions (FSI) in which case the final product of the interaction is a nucleon, similar to the NCE interaction. MiniBooNE has tuned NUANCE to assign a probability of about 20% that the outgoing pion is absorbed.

The resonant pion production is modelled in NUANCE using the Rein and Sehgal model [97]. At MiniBooNE energies (∼ 1 GeV) the interaction is dominated by the ∆(1232) resonance, although higher mass resonances are included in the simulation. The form factors are assumed to be identical to those used in NCE and CCQE interaction, with the exception of the axial vector mass, where we take $M_A=1.1$ GeV—see Ref. [98].

3.8.4 Nuclear effects

In the case of bound nucleons, nuclear effects modify the above interaction rates. NUANCE employs the RFG model of Smith and Moniz to incorporate these effects. In the RFG model, target nucleons are assumed to have a uniform momentum density distribution up to a cutoff Fermi momentum of $p_F=220$ MeV. A scattering interaction is only allowed if the outgoing nucleon has a momentum greater than $p_F$. This effect is called Pauli blocking and suppresses the cross section at low values of the momentum transfer.

The low $Q^2$ regime, where nuclear effects are dominant, is untested by other experiments and the RFG model of Smith and Moniz strain to match the observed data. Hence in MiniBooNE the Pauli blocking parameter is scaled by a scaling factor $\kappa = 1.022$, whereas in the RFG model of Smith and Moniz $\kappa$ is unity—see Ref. [99] for details.

Last of the nuclear effects are final state interactions (FSI). This internuclear effect refers to the strong interaction the recoil hadrons experience due to the surrounding nucleons inside
the carbon nucleus. NUANCE accounts for this effect based on models of nuclear density and Fermi momentum, and generating new final state particles at each step if the MC determines that a FSI has occurred.

### 3.8.5 Dirt Interactions

NUANCE also simulates the neutrino interactions with the material surrounding the detector and the detector material (collectively called as “dirt” interactions). The interactions are simulated the same way as the in-tank interactions however the cross sections are reweighted according to the density of the material relative to that of mineral oil.

### 3.9 The MiniBooNE Detector Monte Carlo

The MiniBooNE neutrino event generator (NUANCE) outputs a set of neutrino-generated particles and channels. This information is used by the detector simulation to model particle propagation, the resulting light emission and propagation, and the PMT response. MiniBooNE uses the GEANT3 simulation software [100] in conjunction with a customized optical model to simulate interactions in the detector.
The geometric domain of the MiniBooNE GEANT3 simulation. The dirt region and the overburden are indicated by the thick-lined cylinder and the conical frustum, the thin-lined cylinders indicate the electronics room and vault, the sphere and the top-hat determine the detector tank and the tophat. From Ref. [101]

The geometric domain of simulation includes the tank, surrounding dirt and the the vault housing electronics above the tank. In the simulation, the mineral oil is assumed to be CH$_2$ with a density of 0.845 g/cm$^3$. The details of the PMT structure and calibration devices like the scintillator cubes and laser flasks are also included. The dirt surrounding the detector is assumed to be composed of a mixture of silicon, aluminum, and oxygen with respective densities.

The default GEANT3 tracking algorithm is employed to propagate the particles resulting from the neutrino interactions. Some modifications to the standard routines include an improved model for Dalitz decay ($\pi^0 \rightarrow e^+e^-\gamma$), muon decay ($\mu \rightarrow e\nu\nu$), and the possibility of $\mu^-$ capture by carbon. The default hadronic interaction package, GFLUKA, was replaced with GCALOR [102].

### 3.9.1 The MiniBooNE Optical Model

MiniBooNE has developed a custom made optical model to characterize the optical photons which are produced by the charged particles traversing the detector. The MiniBooNE optical
model characterizes both the production of photons and propagation within the detector until it reaches a PMT. The MiniBooNE PMTs are sensitive to photons over the wavelength range of 280–640 nm, as shown in Fig. 3.20 below.

![Figure 3.20: Quantum efficiency of R5912 PMT obtained from Hamamatsu measurements.](image)

**3.9.1.1 Light production**

Light production in MiniBooNE occurs through Cherenkov radiation, scintillation, and fluorescence, as described below:

- **Cherenkov radiation**

  Whenever a charged particle moves with a velocity faster than the velocity of light in that medium it emits Cherenkov light. Cherenkov radiation is prompt and directional. The angle between the particle track and the emitted photons is governed by the formula:

  \[
  \cos \theta_c = \frac{1}{\beta n},
  \]

  where \( n \) is the refractive index of the medium and \( \beta \) is the particle velocity with respect to the speed of light, \( \beta = \frac{v}{c} \). The rate of photon emission as a function of wavelength
is given by:
\[
\frac{dN}{dx d\omega} = \alpha q^2 \left[ 1 - \frac{1}{\beta^2 n^2(\omega)} \right], \tag{3.3}
\]
where \(x\) is the path-length, \(\omega\) is the photon frequency, \(n\) is the refractive index, \(\alpha\) is the fine structure constant, and \(q\) is the particle charge.

Using Eq. (3.2), the particle velocity can be expressed through its kinetic energy, \(T\),
\[
\cos\theta_{\text{cer}} = \frac{1}{\beta n} = \frac{1}{n} \left[ \frac{(T + m)^2}{(T + m)^2 - m^2} \right]^{\frac{1}{2}}, \tag{3.4}
\]
where \(m\) is the rest mass of the particle. The minimum kinetic energy to produce Cherenkov light is obtained from \(\beta = 1/n\), which yields for the Cherenkov kinetic energy threshold
\[
T_{Ch} = m \left( \frac{n}{\sqrt{n^2 - 1}} - 1 \right).
\]
Herewith, the Cherenkov threshold for protons in the MiniBooNE target oil is approximately \(T_{Ch} \approx 350\,\text{MeV}\).

• Scintillation and Fluorescence

The ionization tracks of particles excite the electrons in the \(\text{CH}_2\) atom, the subsequent de-excitation results in the emission of energy in the form of photons. This is known as scintillation light and is delayed and isotropic in nature. When optical photons are responsible for excitation and de-excitation of the target molecules, as opposed to ionization tracks, the process is known as fluorescence.

The characteristics of scintillation and fluorescence (the wavelength spectra and emission spectra) are determined by the chemical composition of the oil, in particular the various flours and vitamin E added for oil preservation. The scintillation light yield is proportional to the particle ionization loss, while quenching effects reduce this light yield. Birk’s law is used to convert ionization energy loss per unit length per unit
medium density, $dE/dx$, to scintillation light production,

$$\frac{dE_{sci}}{dx} = \frac{dE}{dx} \left[ 1 + k_B \frac{dE}{dx} + k'_B \left( \frac{dE}{dx} \right)^2 \right]$$

(3.5)

where the value of the coefficients $k_B = 0.014$ g cm$^2$ MeV$^{-1}$ and $k'_B = 0$ were obtained empirically.

![Graph of fluors in MiniBooNE oil](image)

**Figure 3.21:** Fluors in MiniBooNE oil. (Top) Likelihood of photon excitation for the fluors in the MiniBooNE mineral oil. (Bottom) Emission probability and wavelength for the same fluors; also shown here are the lifetime for the corresponding emission photons. Figure from Ref. [93]
3.9.1.2 Light transmission

The propagation or transmission of photons in MiniBooNE occurs through processes such as scattering, fluorescence, and absorption.

- **Scattering**
  When an optical photon interacts with a target molecule and is deflected and changes its polarization state while keeping the same original wavelength, the process is known as scattering. Scattering measurements in the MiniBooNE oil were done externally [103] and are due to Rayleigh and Raman scattering.

- **Fluorescence**
  Fluorescence is when optical photons (created by both Cherenkov and scintillation) are absorbed and reemitted later by target molecules at a different wavelength and/or direction. Details of the measurements which was conducted at Johns Hopkin University are given in Ref.[104]

  Of particular importance is the fluorescence due to ultraviolet (UV) photons. They have a wavelength less than 250 nm and are not registered by the PMTs, as the PMT quantum efficiency is zero below 280 nm, as shown in Fig. 3.20. However, the UV photons may be absorbed and remitted with a photon spectrum above 250 nm with an attenuation length of the order 1–10 cm.

  In the MC simulation the original UV photons are not propagated; however the UV fluorescent photons are generated along the particle track similar to the scintillation photons.

- **Absorption**
  The difference between the total extinction rate and the sum of attenuation due to scattering and fluorescence is attributed to the absorption of photons in oil.
Figure 3.21 shows the excitation wavelength and the emission wavelength for the fluors in the MiniBooNE mineral oil. The extinction rate as a function of wavelength for the fluors together with some of the processes contributing to the extinction is shown in Fig 3.22.

![Figure 3.22: Extinction rate as a function of wavelength in the Marcol 7 mineral oil and some of the processes contributing to it. Figure from Ref. [87]](image)

### 3.9.2 Simulation of Photomultiplier tube Response and Digital Acquisition

The final step in the simulation is generating the PMT response of the GEANT3 photoelectrons that reach the PMT. After that the information is passed through a FORTRAN-based code which replicates the passage of data through the DAQ electronics. This ensures that the final MC output is structurally the same as the data.
The PMT response is simulated by smearing the time and charge accumulated for each photon hit to account for effects like pre-pulsing, late pulsing, and individual PMT behavior, as obtained from the PMT studies mentioned in §3.5 and also using the data collected from the laser flask calibration described in §3.7. A time offset $\Delta t_{\text{off}}$ corresponding to the particular channel is also added.

Digitization of the output of the PMT response simulation is achieved by creating a triangular anode pulse according to the charge drawn for the PE. This pulse is then used to create a set of charge and time quad outputs by simulating the effects of MiniBooNE DAQ as seen in §3.6.1.

3.10 Event Reconstruction

Different events (such as electrons, muons, protons, etc.) have different topologies, and consequently different event reconstructions must be applied. Since the event identity is not known a priori, each event is normally reconstructed under different hypotheses, after which particle identification (PID) cuts may be applied, depending on the particular analysis strategy. This section follows Ref. [105].

A NCE scattering event in MiniBooNE results in an outgoing nucleon with nuclear recoil. For the purpose of the reconstruction we ignore the nuclear recoil and reconstruct the outgoing nucleon. The reconstruction applied here is under the assumption that the outgoing nucleon is a proton, while neutrons – if ejected – are only seen through their secondary interaction with a proton.

Protons have a different light emission profile as compared to other particles reconstructed in MiniBooNE (electrons, muons, or pions). Being heavier, protons mostly emit isotropic scintillation light and only emit Cherenkov light above $350\text{ MeV}$, their Cherenkov threshold in the MiniBooNE medium. The NCFitter reconstruction package utilizes both the scintillation and the Cherenkov light to reconstruct the outgoing nucleons. Each of the 1,280 PMTs in
the main region stores the following information:

- if the PMT registered a hit;
- if the PMT was hit, the measured charge of the hit;
- if the PMT was hit, the measured time of the hit;

Using the above information the reconstruction algorithm reconstructs the particle track. A reconstructed track in MiniBooNE is a vector \( \mathbf{X} = (x_0, y_0, z_0, t_0, \theta_0, \phi_0, E_0) \), where \( x_0, y_0, z_0 \) is the event vertex in the coordinate system of the detector, \( t_0 \) is the event time, \( \theta_0 \) and \( \phi_0 \) define the event direction, and \( E_0 \) is the kinetic energy.

![Reconstruction geometry](image)

**Figure 3.23:** Reconstruction geometry.

To reconstruct any event MiniBooNE employs a method of charge and time likelihood maximization. Assuming that the PMTs behave independently, for a given set of PMT
measurements and track parameters $X$, the event likelihood is defined as:

$$
\mathcal{L}(X) = \prod_{i, \text{nohits}} f_q(\theta, X) \prod_{i, \text{hit}} f_q(q_i, X)f_t(t_i, X) 
$$

(3.6)

where products are taken over unhit and hit PMTs and

- $q_i$ and $t_i$ are the measured charge and time at the $i^{th}$ PMT,
- $f_q(q_i, X)$ is the probability distribution function (PDF) for the measured charge on the $i^{th}$ PMT, given $X$, evaluated at $q_i$ and
- $f_t(t_i, X)$ is the PDF for the measured time given $X$, evaluated at $t_i$.

The $X$ dependence of the PDFs can be expressed using the predicted charge ($\mu_i$) for each PMT:

$$
f_q(q_i, X) = f_q(q_i, \mu_i(X)),$$

$$
f_t(t_i, X) = f_t(t_i, \mu_i(X), E),
$$

(3.7)

where an additional energy dependence is associated with the time likelihood. As we explain later, the particle’s path-length depends on its energy, which in turn affects directly its timing characteristics.

Figure 3.24: Geometry of a long outgoing event.
The predicted charge as a function of the track parameters, $\mu_i(X)$, is for both light components, scintillation and Cherenkov light, as follows:

$$
\mu_{sci}(X) = \epsilon \phi_{sci}(E) \frac{\exp(-r/\lambda_{sci}(R))}{r^2} f(\cos \eta) F_{sci}(E, \cos \theta, R) \text{Corr}(E, \cos \alpha)
$$

$$
\mu_{cer}(X) = \epsilon \phi_{cer}(E) \frac{\exp(-r/\lambda_{cer})}{r^2} f(\cos \eta) F_{cer}(E, \cos \theta, R) \text{Corr}(E, \cos \alpha)
$$

(3.8)

where the subscripts $sci$ and $cer$ stand for scintillation and Cherenkov, respectively, and:

- $\epsilon$ is the quantum efficiency, i.e., the probability that a photon is detected by a PMT; $\epsilon$ is different for old and new PMTs in MiniBooNE.

- $\phi$ is the light flux – the total number of photons per solid angle created in an event.

- $\lambda$ is the effective attenuation length; for scintillation light this parameter also depends on the radial shell of the event vertex, $R$, which models relatively well other effects besides attenuation, such as scattering, absorption and reemission, etc.

- $f(\cos \eta)$ accounts for the angular acceptance of the PMTs, where $\eta$ is the angle of the incident light with respect to the PMT normal.

- $F(E, \cos \theta, R)$ is the angular emission profile with dependence on energy, $E$, $\theta$ (the angle between the particle’s direction and the line from the PMT to the vertex), and radial shell $R$.

- $\text{Corr}(E, \cos \alpha)$ is a correction function for outgoing events where an energetic proton may leave the tank before losing all its energy and $\alpha$ being the angle between the event direction and the line from center of the tank – see Fig. 3.24.

For a clear picture of the geometric angles refer to Fig. 3.23 and Fig. 3.24.

The charge likelihood $f_q(q > 0, \mu)$ is used by all reconstruction algorithms, and was obtained from the MiniBooNE laser calibration data described in §3.7.1. The time likelihood,
\[ f_i(t_i, \mu_i(X), E) \]

is calculated as:

\[
 f_i(t_{\text{corr}}, X, E) = \frac{\mu_{\text{sci}}}{\mu_{\text{sci}} + \mu_{\text{cer}}} f^{\text{sci}}_i(t_{\text{corr}}, \mu_{\text{sci}}, E) + \frac{\mu_{\text{cer}}}{\mu_{\text{cer}} + \mu_{\text{sci}}} f^{\text{cer}}_i(t_{\text{corr}}, \mu_{\text{sci}}, E), \tag{3.9}
\]

with contributions from both scintillation and Cherenkov light, as explained below. The event time \( t \) was corrected to \( t_{\text{corr}} \) to adjust for the time of photon propagation from the vertex to the PMT using:

\[
 t_{\text{corr}, i} = t_i - t_0 - \frac{r_i}{c_n}
\]

where \( t_i \) is the PMT hit time, \( t_0 \) is the event time, \( r_i \) is the distance to the PMT, and \( c_n = 19.50 \text{ cm/ns} \) represents the effective speed of light in the detector medium.

A Gaussian distribution is used to represent the Cherenkov light component,

\[
 f^{\text{cer}}_i(t_{\text{corr}}, \mu_{\text{cer}}, E) = \frac{1}{\sqrt{2\pi} \sigma(E, \mu_{\text{cer}})} \exp \left[ -\frac{(t_{\text{corr}} - t_0(E, \mu_{\text{cer}}))^2}{2\sigma^2(E, \mu_{\text{cer}})} \right] \tag{3.10}
\]

while a slightly more complicated expression is used the model the scintillation part, namely:

\[
 f^{\text{sci}}_i(t_{\text{corr}}, \mu_{\text{sci}}, E) = (1 - B) \frac{1}{2\tau_1} \exp \left( \frac{\sigma^2}{2\tau_1^2} - \frac{t_{\text{corr}} - t_0}{\tau_1} \right) \text{Erfc} \left[ \frac{\sigma}{\sqrt{2\tau_1}} - \frac{t_{\text{corr}} - t_0}{\sigma} \right] + B \frac{1}{2\tau_2} \exp \left( \frac{\sigma^2}{2\tau_2^2} - \frac{t_{\text{corr}} - t_0}{\tau_2} \right) \text{Erfc} \left[ \frac{\sigma}{\sqrt{2\tau_2}} - \frac{t_{\text{corr}} - t_0}{\sigma} \right] \tag{3.11}
\]

where Erfc is the error function complement,

\[
 \text{Erfc}(x) = 1 - \text{Erf}(x) \quad \text{with} \quad \text{Erf}(x) = \frac{2}{\sqrt{\pi}} \int_0^x e^{-t^2} dt.
\]

The expression for the scintillation light is nothing else but the result of the convolution of a Gaussian (representing the PMT response) with two exponentials (of time constants \( \tau_1 \) and \( \tau_2 \)) representing the exponential time response of the scintillator. As for Cherenkov light, the widths and the offsets, \( \sigma \) and \( t_0 \), respectively, as well as the time “constants” \( \tau_1 \) and \( \tau_2 \), are actually functions of the predicted charge and event energy. For example, for
a given energy, the widths of the Cherenkov distributions become narrower with increasing amount of charge, whereas for the same amount of light the distributions become wider with increasing energy – as the particle path-length increases.

For details on reconstruction methods used in MiniBooNE, see Ref. [106]; for the NCE reconstruction in particular and the development of the \textit{NCFitter} see Ref. [105].
Chapter 4

Analysis

In this chapter we present the analysis of the antineutrino nucleus NCE scattering data. After defining our signal, we define the selection cuts and describe the background subtraction. We then describe the procedure employed for unfolding the data to extract the cross section. We also present the error estimation method. Using the extracted antineutrino cross section we take a ratio of the antineutrino nucleus NCE cross section to the neutrino nucleus NCE cross section along with the associated errors. Finally we extract, the axial mass from the antineutrino NCE sample using a $\chi^2$ minimization method.

The work presented in this chapter was done as a part of this dissertation research unless otherwise stated.

4.1 Cross section and Flux Integrated Differential Cross Section

Before we embark on our stated aim to measure the antineutrino nucleus NCE scattering differential cross section, we clarify some basic terms.

Whenever one set of particles, $N^s$ (the source), is impinged upon another set of particles, $N^{tar}$ (the target), then the cross section ($\sigma$) is a measure of the probability that a source
particle will hit or interact with a target particle. In the present experimental setup, the number of source particles ($\bar{\nu}$) is designated as flux ($\Phi$) and is measured as a function of velocity or energy, and $\sigma$ is measured in terms of the momentum transferred squared ($Q^2$) to the nucleon by the antineutrino. Finally, since measurements can only be made in terms of certain values of $Q^2$, we introduce the differential cross section. The flux is also integrated over the neutrino energy spectrum, as the incoming antineutrino energy cannot be reconstructed. The resulting flux-integrated differential cross section in terms of $Q^2$ is

$$\frac{d\sigma}{dQ^2} = \frac{N^{int}/\left(\frac{dQ^2}{dT^{int}} \Delta T^{int}\right)}{N^{tar} N^{POT} \int \Phi_{\bar{\nu}} dE_{\bar{\nu}}}$$  \hspace{1cm} (4.1)$$

where $N^{int}$ is the number of interactions; $dQ^2/dT^{int}$ is the momentum transferred per interaction, $\Delta T^{int}$ is the bin width of the interaction spectrum, and $\int \Phi_{\bar{\nu}} dE_{\bar{\nu}}$ is the total integrated flux – a particle flux integrated over time is also called fluence.

4.2 Signal definition

![Figure 4.1: Antineutrino nucleon NCE interaction.](image)

In this analysis, our aim is to measure the neutral current elastic scattering of antineutrinos off nucleons, which happens via an exchange of a $Z^0$ boson. There is no flavor change and
the particles remain in the initial states:

\[ \bar{\nu} + N \rightarrow \bar{\nu} + N. \]

Complications to the measurement of the above signal arise due to the fact that MiniBooNE has a nuclear target (CH\textsubscript{2}). The target nucleon can be any one of the 2 protons in the H atom, 6 protons in the C atom, or 6 neutrons in the C atom. In case of the nucleons in the carbon atom, a nucleon, after interacting with the antineutrino, may undergo additional interactions within the nucleus. These interactions are referred to as final state interactions (FSI). MiniBooNE can only detect neutrons if they undergo FSI that result in a proton emission. The final state interactions are not discernible by the detector and we have an “observable” scattering which has to be defined more broadly than shown above. However it should be pointed out that since an “observable” scattering is exactly what the detector sees, it is practically more useful.

To sum up, the observed signal for the antineutrino neutral current elastic cross section, an antineutrino interacting with a nucleon is defined to include:

- an antineutrino interacting with a proton and the proton is knocked out of the nucleus;

- an antineutrino interacts with a proton and the proton undergoes FSI, resulting in multiple nucleons exiting the nucleus; the average energy of the antineutrino beam (\(\sim 0.6\) GeV) is lower than the threshold for inelastic scattering where the target nucleon is broken up.

- an antineutrino interacts with a neutron and the neutron undergoes FSI possibly knocking a proton out of the nucleus or another nucleus. Both cases result in multiple proton emission.
4.3 Analysis Cuts

NCE events constitute about 18% of the total events in MiniBooNE. In order to isolate a sample of NCE events we perform a series of analysis cuts. These are various conditions on the experimental variables, like PMT charge, time or reconstructed energy, which differentiates the NCE events from other events in the MiniBooNE sample. These analysis cuts are based on the physics processes and Monte Carlo studies. The development of the selection cuts was done as a part of this dissertation research. We describe below each cut in detail.

- Only 1 subevent.

A subevent is a cluster of at least 10 tank PMT hits with no more than 10 ns between any two consecutive hits. In order to be classified as subevents of the same event, the subevents must occur within the same DAQ window (19.2 \( \mu s \)). For example, a CCQE interaction has two subevents:

\[
\begin{align*}
1^{st} \text{subevent:} & \quad \nu_\mu + n \rightarrow \mu^- + p \\
2^{nd} \text{subevent:} & \quad \mu^- \rightarrow e^- + \bar{\nu}_e + \nu_\mu
\end{align*}
\]

The first subevent is associated with the primary neutrino interaction where a muon and proton is produced. The second subevent is associated with the decay of the muon. Fig. 4.2 shows the PMT hit time distribution for a typical CCQE event.
A typical NCE interaction has only one subevent associated with the primary neutrino interaction.

- **Veto hits < 6.**

  This cut excludes events which are entering or exiting the detector and register activity in the veto region. Cosmic rays and neutrino interactions in the material surrounding the detector account for entering events. The veto cuts removes 99.99% of the cosmic ray background A CCQE interaction in which the muon exits the detector before decaying can be a background for this analysis. These events also trigger veto activity and are excluded by this cut.

---

**Figure 4.2:** A part of beam spill having a CCQE candidate event. The first cluster of PMT hits is from the muon in the primary neutrino interaction, and the second is due the delayed decay of the muon. From Ref [93]
Figure 4.3: The above plot shows the distribution of subevent times after various cuts. The veto hits < 6 (red to green) cut removes much of the beam-off background. The event window has been shifted to start from zero while making this plot. From Ref [93]

- **Tank hits > 12.**

  This cut ensures a minimum number of tank PMT hits so that the event is reconstructable. The NCFitter reconstructs 7 parameters of each event: 3 defining the position, 2 direction parameters, and 1 parameter each for time and energy. At low energies, when protons are below the Cherenkov threshold, only the event position and time can be reconstructed, while the energy can be computed from the total charge and event location. Therefore, to reconstruct the 4 event parameters we require to have at least 3 times as many PMT hits.

- **Event in beam window.**

  A cut on the reconstructed event time in NCFitter ensures that the event happened within the beam time window, 4400 ns < $t_{\text{evt}}$ < 6500 ns, and thus the beam-unrelated events are excluded. Here $t_{\text{evt}} = 0$ corresponds to start of data taking by the detector which is ~ 5 $\mu$s before the arrival of the beam. As seen from Fig. 4.3 most of the
beam-unrelated events are due to Michel electrons from cosmic-ray muon decays.

![Energy Distribution Diagram](image)

**Figure 4.4:** The energy cut. Reconstructed nucleon energy distribution for $\bar{\nu}$ NCE signal and various backgrounds. The arrow indicates the part included in the analysis.

- **Reconstructed energy $< 650$ MeV.**

As seen in Fig. 4.4 NCE events lie in the low energy region as they produce less light as compared to other neutrino interactions. A cut on the energy while retaining NCE events, excludes many backgrounds which tend to rise at higher energies.
Figure 4.5: The particle identification cut. Time likelihood difference between the proton and electron hypotheses for MC $\bar{\nu}$ NCE sample. The arrow indicates the part included in the analysis.

- $\ln(L_e/L_p) < 0.42$.

This is a particle identification cut which selects proton-like events while rejecting electron-like events. Fig. 4.5 shows the time likelihood difference between events reconstructed under an electron and a proton hypothesis, for both Monte Carlo NCE scattering events and beam-unrelated backgrounds. The beam-unrelated backgrounds are dominated by electrons, and are significantly reduced as a result of this cut.

- **Fiducial volume cut, $R < 5$ m.**

The final cut selects a fiducial volume of $R < 5$ m where $R$ is the reconstructed radius in the NCFitter. This cut ensures that the events in the sample are well reconstructed, as the events close to the PMTs cannot be reconstructed reliably. Additionally, this cut also reduces the dirt background, which are neutrino interactions in the dirt surrounding the detector.
4.4 Sample composition

A total of 60,605 events pass the analysis cuts, representing the largest sample of antineutrino NCE scattering events ever collected. The data set corresponds to $10.1 \times 10^{20}$ POT. The cut efficiency is 33%. According to the MC prediction, 48% of the sample are $\bar{\nu}$ NCE events, and the rest 52% are backgrounds. The three major backgrounds are dirt events (17%), irreducible events (14%) and neutrino-induced events (19%). Figure 4.6 shows the reconstructed energy spectrum for the data along with the MC predictions for the signal and various backgrounds. There is some disagreement between data and the MC prediction in the low energy region, where the MC underpredicts the data, and in the intermediate energy region, where the MC overpredicts the data. We explore a possible reason for this discrepancy in §4.12.

The dirt events contribute to the background at low energy (below 300 MeV). These are mostly due to the neutrino interactions in the dirt surrounding the detector, and the
resulting nucleon passes into the detector without firing enough veto PMTs. The dirt events are difficult to simulate as the material surrounding the detector has not been studied well enough. Hence we use the MiniBooNE data to measure the dirt contributions to the sample.

The irreducible events are so called because they mimic the NCE signal and we have to solely rely on the MC to estimate them. These are NC pion events in which the pion is absorbed and only the nucleon is visible, just as in NCE scattering events.

The neutrino-induced events are another major background. These are due to the intrinsic neutrino background in the antineutrino beam. The corresponding antineutrino background in the neutrino mode beam was negligible, due to the lower cross section. MiniBooNE has measured the neutrino background in its antineutrino mode [107] which is used by this analysis to constrain the neutrino induced background.

In the next section we describe the procedure of estimating the various backgrounds in the sample.

4.5 Estimation of Backgrounds

In this section we estimate the various backgrounds, namely the dirt background, the NC$\pi$ irreducible background, and the neutrino induced wrong sign (WS) background.

4.5.1 Dirt Background

As mentioned earlier, dirt events in the detector result from neutrino interactions with the material surrounding the detector. The products of these interactions (neutrons in the neutrino mode and protons in the antineutrino mode) penetrate the detector without firing enough veto PMTs to be vetoed and hence contaminate our sample.

The measurement of the dirt background was a part of this dissertation research.

The dirt background is estimated using the MiniBooNE data. The dirt events have distinct kinematics as compared to in-tank interactions: they are preferentially reconstructed
upstream ($Z < 0 \text{ m}$) and in the outer regions of the detector with relatively lower energies. The dirt energy spectrum is measured by performing a template fit of the dirt-enriched samples of MC to the MiniBooNE data in three variables, namely the reconstructed event $Z$ coordinate, the radial position, $R$, and energy.

### 4.5.1.1 Generation of Dirt-Enriched Samples

To measure the dirt background, three additional samples of events with an increased dirt event fraction are generated. This is done for three variables: the $R$ distribution, the $Z$ distribution and $T$ (kinetic energy) distribution. They have the following precuts:

- Only 1 Subevent,
- Veto hits < 6,
- Tank hits > 12,
- Event in beam window, and
- $\ln(L_e/L_p) < 0.42$.

These are the same selection criteria as for the NCE scattering sample with the exception of the fiducial volume and event energy cuts. In addition, the following cuts are applied on individual samples:

<table>
<thead>
<tr>
<th>Sample</th>
<th>Purpose of sample</th>
<th>Cuts: Precuts+</th>
</tr>
</thead>
<tbody>
<tr>
<td>NCE</td>
<td>NCE sample (dirt-reduced)</td>
<td>$R &lt; 4.2 \text{ m for } E &lt; 200 \text{ MeV} &amp; R &lt; 5 \text{ m for } E &gt; 200 \text{ MeV}$</td>
</tr>
<tr>
<td>Dirt_Z</td>
<td>Fit dirt with $Z$ (dirt-enhanced)</td>
<td>$3.8 \text{ m} &lt; R &lt; 5.2 \text{ m}$</td>
</tr>
<tr>
<td>Dirt_R</td>
<td>Fit dirt with $R$ (dirt-enhanced)</td>
<td>$Z &lt; 0$</td>
</tr>
<tr>
<td>Dirt_E</td>
<td>Fit dirt with energy (dirt-enhanced)</td>
<td>$3.8 \text{ m} &lt; R &lt; 5.2 \text{ m} &amp; Z &lt; 0$</td>
</tr>
</tbody>
</table>

**Table 4.1:** Sample names, purpose and cuts to create a dirt-enriched sample.
4.5.1.2 Dirt Measurement from the Z Distribution

In the measurement of dirt using the Z distribution we make a total MC distribution histogram which is the sum of the in-tank MC and the dirt MC histograms. We also have the NCE data for this distribution. We vary the dirt MC and the in-tank MC to find the best fit to the data. We do this in different energy bins (10 bins of 61 MeV each) between 40 MeV and 650 MeV. The plots in Fig. 4.7 below show the Z distribution dirt estimation. Note that the “after fit” total MC better describes the data as compared to the “before fit” total MC. There is not many dirt events in energy bins greater than 350 MeV.
Figure 4.7: Dirt estimation using Z distribution. (a) and (b) show the first two energy bins (40–101 MeV and 101–162 MeV) of the 10 energy bins in Z where the dirt is estimated. Data (black) is shown with statistical errors. Dotted red shows the total (signal + dirt) before fit and solid red shows total MC after fit. Panels (c) and (d) show the last two energy bins, 528–589 MeV and 598–650 MeV bins of the 10 bins. The error bars are relatively large here due to the low statistics.

We obtain a correction function from the best fits in each energy bin. The dirt energy correction function we obtain is shown in Fig. 4.8. The error shown is the error returned by the MINUIT fitting package.
4.5.1.3 Dirt Measurement from the R Distribution

The dirt measurement using the R distribution is performed by using the corresponding Dirt_R samples and repeating the above procedure, as shown in [Fig. 4.9].
Figure 4.9: Dirt estimation using the R distribution. Here also panels (a) and (b) show the first two bins ranging from 40–162 MeV where Total MC (solid red) after fit matches better with data. Panels (c) and (d) show the last two energy bins, 528–589 MeV and 598–650 MeV bins, out of the 10 bins where the error bars are relatively large here due to low statistics.

The dirt energy correction function obtained from fitting the R distribution is shown in Fig. 4.10.
4.5.1.4 Dirt Measurement from Energy distribution

In this method dirt is measured using two samples: NCE signal and dirt-enriched sample with Dirt_E cuts. For both samples we have MiniBooNE data, MC prediction for NCE, dirt and in-tank background histograms, as illustrated in [Fig. 4.11].
Figure 4.11: Reconstructed energy distribution with NCE cuts (top) and "Dirt_E" cuts (bottom) for data (black) with statistical errors, NCE signal MC (blue), dirt (brown) and intank-backgrounds (green). The spike at 200 MeV for the spectrum on top is due to the energy dependent fiducial volume cut used to make a dirt reduced sample.

We define the following histograms:

$$\bar{\nu} = \text{reconstructed energy spectrum for data},$$

$$B = \text{reconstructed energy for MC in-tank backgrounds},$$
\( S = \) reconstructed energy spectrum for MC NCE signal, and
\( D = \) reconstructed energy spectrum for MC dirt

with upper indices defined as:
\( s = \) NCE event sample and
\( d = \) Dirt_E event sample

In terms of the definitions introduced we have the following relationships:

\[
B_{i}^{s} + S_{i}^{s} + D_{i}^{s} = \bar{\nu}_{i}^{s},
\]

\[
B_{i}^{d} + S_{i}^{d} + D_{i}^{d} = \bar{\nu}_{i}^{d}.
\]

Furthermore we define the following fractions in the two samples [Fig. 4.12]:

\[
f_{i} = \frac{D_{i}^{d}}{D_{i}^{s}} \quad \text{and} \quad g_{i} = \frac{S_{i}^{d}}{S_{i}^{s}}.
\]

Figure 4.12: fractions f and g as functions of reconstructed energy

Finally one can express \( D_{i}^{s} \) (the dirt energy spectrum in the NCE sample) in terms of the above definitions :

\[
D_{i}^{s} = \frac{g_{i}(\bar{\nu}_{i}^{s} - B_{i}^{s}) - (\bar{\nu}_{i}^{d} - B_{i}^{d})}{g_{i} - f_{i}}
\]

The result of this measurement in terms of dirt energy correction function is shown in

96
4.5.1.5 Combined Dirt Correction

We notice that the errors go up beyond 300 MeV in the dirt energy correction functions obtained by all three methods (Z_dist, R_dist, E_dist). This is because most dirt events have energies below 300 MeV and there are not many dirt events at higher energies to perform the fits.
Figure 4.14: Dirt energy correction combined fit using a 0-th order polynomial.

We perform a combined fit on the dirt correction functions obtained by the three methods for the energy range 40 MeV to 325 MeV, as shown in Fig. 4.14. The fitted correction function is to a 0-th order polynomial and yields $0.625 \pm 0.032$, where the error is that returned by the MINUIT fitting package.

4.5.2 Estimation of Neutrino Induced Background

Neutrino-induced events in the detector are a major background for the antineutrino NCE scattering cross section measurement. The neutrino contamination in the antineutrino mode is more significant than the antineutrino contamination in the neutrino mode (see Fig. 3.7) due to the leading particle effect: the protons hitting the Be target produce 2 times as many $\pi^+$'s as compared to $\pi^-$'s, and cross section: at MiniBooNE energies ($\sim 1$ GeV) the neutrino cross section is 3 times higher than the antineutrino cross section.

In order to estimate the wrong sign (WS) background we refer to MiniBooNE’s published measurement of the neutrino component in the antineutrino beam [107] to correct the WS flux and the measured NCE neutrino cross section [60] to correct the WS cross section.
As discussed in §2.4.5, the MiniBooNe flux estimation has inputs from the HARP experiment which studied the proton-Be interactions on a replica MiniBooNE target. However, as seen from Fig. 4.15, there are regions in phase space not covered by the HARP measurements, particularly at small angles where forward peaked pions which are not deflected by the MiniBooNE horn, which are a major source of neutrino contamination at the detector.

Figure 4.15: Momentum vs pion angle for the MiniBooNE pion production based on MC. The black box encloses the measurements covered by HARP.

MiniBooNE has measured the neutrino component of the antineutrino beam using two independent methods:

1. Using the single $\pi^+$ (CC1$\pi^+$) sample: In the antineutrino mode, the CC1$\pi^+$ events are exclusively due to $\nu_\mu$ interactions which can be clearly identified by MiniBooNE. Comparing the data with model prediction for this sample allows to measure the neutrino background.

2. Using the neutrino and antineutrino charged-current quasi elastic (CCQE) sample: The primary muon resulting from a CCQE interaction is more forward peaked in the
antineutrino induced CCQE interaction as compared to a neutrino induced CCQE interaction. This difference is exploited by performing a simultaneous angular fit to data.

The results of the measurement are summarized in Fig. 4.16: The CC1π⁺ analysis indicates that the $\nu_\mu$ flux should be scaled by $0.76 \pm 0.11$, while the CCQE angular fits indicate a correction factor of $0.65 \pm 0.23$.

Of the two methods outlined above, method 2 utilizes the antineutrino CCQE scattering interaction. Since the antineutrino NCE scattering interaction shares many of the cross section parameters with the antineutrino CCQE interaction – $M_A$ and $\kappa$, for instance – using the WS correction factor from method 2 would instill a model dependence on the present cross section measurement. In a separate study, a third method was used to estimate the neutrino component of the antineutrino beam [108]. This method exploits the fact that stopped negative muons undergo nuclear capture on carbon atom at a rate of 8% [109], so neutrino induced CCQE events have a significantly lower probability for producing Michel electrons compared to antineutrino CCQE events. The third method suggested that the $\nu_\mu$ flux be scaled by $0.81 \pm 0.15$.

For the present analysis, we take the average between the first and the third method and arrive at a correction factor of $0.78 \pm 0.12$ to correct the wrong sign background in the NCE sample.
In order to correct the WS cross section we use the neutrino NCE measurement. To summarize the WS component in the antineutrino NCE sample was corrected as:

\[ B_{WS}^{corr} = 0.78 \times B_{WS} \times \frac{\nu NCE_{data}^{i}}{\nu NCE_{MC}^{i}} \]  

(4.5)

where \( B_{WS}^{corr} \) is the neutrino induced background after WS correction, \( B_{WS} \) is the WS background before correction, and the last term is the correction factor from the neutrino mode cross section measurement. The error associated with the WS estimation is accounted for in the error analysis discussed in §4.7.
4.5.3 The Irreducible Background

The irreducible background is due to nucleon excitation into a resonant state and subsequent decay of the resonant state to a pion and a nucleon:

\[ \bar{\nu} + p \rightarrow \bar{\nu} + p + \pi^0, \]
\[ \bar{\nu} + p \rightarrow \bar{\nu} + n + \pi^+, \]
\[ \bar{\nu} + n \rightarrow \bar{\nu} + n + \pi^0, \]
\[ \bar{\nu} + n \rightarrow \bar{\nu} + p + \pi^- . \]

In addition to the above antineutrino interactions, the irreducible background also includes the corresponding neutrino interactions. The pions may experience an absorption nucleus and as a result the final state of such a neutrino interaction is only nucleons, which is equivalent to the products of the NCE interaction. The MC model is used to estimate the irreducible background.

4.6 Unfolding

After the backgrounds have been subtracted the signal needs to be corrected for limited detector resolution, mis-reconstructions, and detector efficiency. This procedure is referred to as unfolding or unsmearing.

The first step in unfolding is using the MC information to migrate the reconstructed energy spectrum to the true energy spectrum, where the true nucleon kinetic energy is the sum of the kinetic energies of all nucleons in final state. In order to do this we employ a \((m \times n)\) migration matrix which correlates the reconstructed and true energy of events that pass the selection cuts:

\[ M_{ij} \quad \text{where} \quad i = 1, \ldots, n \quad \text{and} \quad j = 1, \ldots, m \] (4.6)
where $M_{ij}$ is the number of events with true energy in bin $i$ and reconstructed energy in bin $j$.

![Efficiency plot](image)

**Figure 4.17**: Efficiency for $\bar{\nu}$ NCE events with the selection cuts.

The second step is correcting for the limited detector efficiency that distort the original spectrum. This is achieved by defining the efficiency as the ratio of the true energy spectrum before the selection cuts to the same spectrum after cuts:

$$
\epsilon_i = \frac{\mu_{i}^{MC, after \, cuts}}{\mu_{i}^{MC, before \, cuts}}.
$$

(4.7)

Putting the above two steps together we construct the unfolding matrix $U_{ij}$:

$$
U_{ij} = \frac{M_{ij}}{\epsilon_i \sum_{k=1}^{m} M_{kj}}.
$$

(4.8)

where the migration matrix is normalized by dividing each element by the sum of the rows. This method is called the direct matrix method and is based on Bayes’ theorem [110]. The
reconstructed energy spectrum is thus *unfolded* to the true energy spectrum as follows:

\[
\sigma_i^{CV} = \sum_j U_{ij}^{CV} D_j \frac{S_j^{CV}}{S_j^{CV} + B_j^{CV}}
\]  

(4.9)

In the above formula, \(\sigma_i^{CV}\) is the unfolded energy spectrum. The superscript CV denotes that the unfolding matrix was constructed using the MC central value (CV) prediction for the migration matrix and efficiency. Here central value refers to the fact that all parameters in the Monte Carlo simulation are set to their nominal values. Similarly we use the CV prediction of signal and backgrounds to subtract the backgrounds from data using the method of *signal fraction*.

The direct matrix method gives a well-behaved solution but is inherently biased as it depends on the MC prediction of the true and reconstructed spectra. We account for the error introduced due to this bias as a systematic error, which is estimated in §4.8.

### 4.7 Measurement Uncertainties

Before we measure the final cross section we need to assess the systematic and statistical error associated with the measurement. The systematic errors can be broadly classified into one of the following three types:

**A. Flux errors:** the uncertainty in the flux is due the combination of the following uncertainties:

- POT error: this error is due to the uncertainty in number of POT delivered to the MiniBooNE target by the Fermilab Booster.

- Beam error: this is the error associated with horn uncertainties and uncertainties in the target that affect the neutrino flux. The uncertainty involves parameters like: skin depth, horn current, nuclear inelastic cross section, nuclear quasi-elastic cross section, pion inelastic cross section, pion quasi-elastic cross section, and pion total cross section.
• WS error: this error is due to the uncertainty in estimation of neutrino fraction in the antineutrino mode as described in §4.5.2. An uncertainty of 12% is assigned to this measurement as per Ref. [107].

The next four errors are due to the uncertainties in the meson production in the target namely

• $K^0$ production in the target
• $K^+$ production in the target
• $\pi^+$ production in the target
• $\pi^-$ production in the target

B. Cross section errors: this class of errors include the uncertainties in the cross section modelling.

• Hadronic model error: the uncertainties in the hadron production model in the Mini-BooNE target gives rise to this error.
• $\pi^0$ yield error: the uncertainty in the $\pi^0$ production in the detector.
• Cross section error: this error accounts for the uncertainties in the cross section parameters shown on table. For the $\bar{\nu}$ NCE cross section measurement, these parameters are allowed to vary only for the background events.
• Dirt error: the uncertainty in the dirt background measurement of §4.5.1.

C. Detector errors: this class of errors are due to the limitations of the detector hardware.

• Discriminator threshold error: the error due to the fluctuation of the discriminator threshold value for each PMT.
• Q–T correlation: the error due to the uncertainty in the model of charge-time simulation of the PMTs.
• Optical model error: this error is due to the uncertainty in the modelling of the optical properties of the detector target medium. The MiniBooNE optical model has 35 parameters which describe among other things, the Cherenkov and scintillation light production, reflections, etc.

The uncertainties associated with the volume, density, and chemical composition of the target and detector materials factor into the uncertainty in the total number of targets ($N_{tar}$). The density of oil is known to within 0.1% ($\pm 0.001 \text{g/cm}^3$), the thermal expansion ($\sim 10^{-5}/\text{K}$) is negligible [87], and so is the error on Avogadro’s number [1] – which is used to calculate the number of target nucleons. For the chemical composition we use $(\text{CH}_2.06)_n$ as a model of the oil which differs from the simple model $(\text{CH}_2)_n$ by 0.3%. Since the total error associated with the number of target nucleons (0.3%) is negligible as compared to the other errors, we do not assign a separate error for it.

Finally, the list of uncertainties also includes

• Statistical error: the statistical fluctuation in the reconstructed energy distribution accounts for the statistical error.

• Unfolding error: the last error is to account for the bias introduced due to the unfolding procedure explained in §4.9.

Thus we have a total of 16 errors.

### 4.8 Multisims and Unisims

The MC sample used in MiniBooNE depends on various model predictions of flux, cross section, detector effects, etc. As discussed in Chapter 3, the various uncertainties in the model predictions manifest as systematic errors in our measurement. In order to account for these uncertainties, we vary the MC sample with some parameters floated around their best estimates within an allowed region.
The MC with the best estimation of all its parameters is called the CV. A \textit{unisim} is a set of MC variation, when only one parameter in a model is varied, and a set of MC is created with the parameter value chosen randomly around its mean with a variance of \(1-\sigma\). When several parameters are varied at once, with some parameters correlated, then the resulting set of MC variation is called a \textit{multisim}.

For each of the errors mentioned in §4.7 a set of multisim/unisim is created and the uncertainty due to that error is estimated as described below in §4.8.

4.9 Error Calculation

In this section we describe the method used to estimate the various errors, namely the systematic errors, the statistical error, the unfolding error, and finally the total error.

4.9.1 Systematic Errors

In the present analysis we treat each MC variation or \textit{multisim} as a possible MC CV (best estimate of the prediction). We then calculate the migration matrix and efficiency associated with each MC variation and unfold data.

For each \(k\)-th multisim the unfolded true spectrum is:

\[
\sigma_i^k = \sum_j U_{ij}^k D_j \frac{S_j^k}{S_j^k + B_j^k},
\]

(4.10)

where \(i\) is the bin of true energy, \(j\) is the bin of reconstructed energy, \(U_{ij}^k\) is the unfolding matrix for the \(k\)-th multisim, \(D\) is the data, \(S\) the signal, and \(B\) backgrounds. Again the error associated with the unfolding procedure is calculated as a separate systematic error §4.9.3. The error associated with each systematic error is calculated as:

\[
E_i^\sigma = \sqrt{\frac{1}{N} \sum_{k=1}^{N} (\sigma_i^k - \sigma_i^{CV})^2},
\]

(4.11)
where $N$ is the number of MC variations for each multisim.

### 4.9.2 Statistical Error

The statistical error for this measurement is due to the statistical fluctuations in the observable variable— the reconstructed proton energy. The error on each reconstructed energy spectrum for data is $\sqrt{D_j}$.

We construct a unisim where each bin of the spectrum has a value randomly chosen from a Gaussian with a mean value of $D_j$ and variance $\sqrt{D_j}$. We then propagate this unisim through the unfolding procedure to estimate the final statistical uncertainty in the cross section.

### 4.9.3 Unfolding Errors

The final error we consider is the error due to the bias in the unfolding procedure. As mentioned earlier, the unfolding matrix depends on the MC prediction that was used to produce it, and is biased. To eliminate the bias we need to unfold it over several iterations, and for each iteration, using the unfolded distribution as the new true energy spectrum for the next iteration. Theoretically, the unfolded distribution should converge after several iterations. However, when unfolding data, certain bins with low statistics do not converge as compared to MC.

Based on MC studies (which were based on 8 times the statistics as compared to the data) we observed that the difference between the unfolded spectrum and the “true” spectrum is less than 1% after 7 iterations. Hence, we assume that the bias goes away after approximately 7 iterations, and we calculate the bias in unfolding for each $k$-th multisim:

$$
Bias_i^k = \sigma_i^{k,7^{\text{th}}\text{iter}} - \sigma_i^{k,1^{\text{st}}\text{iter}},
$$

where $i$ is the bin of true energy for the $k$-th MC variation. The bias for the particular
systematic error (particular multisim/unisim) is calculated as:

\[ \text{Multisim\_Bias}_i^a = \sqrt{\frac{1}{N_a} \sum_{k=1}^{N_a} (\text{Bias}_k^i)^2}, \]  

(4.13)

where \( N_a \) is the number of MC variations for the \( a^{th} \) error.

The total unfolding bias for the 15 systematic and statistical multisims (unisims) is

\[ \text{Unfolding\_error}_i = \sqrt{\frac{1}{15} \sum_{k=1}^{15} (\text{Multisim\_Bias}_k^i)^2}. \]  

(4.14)

### 4.9.4 Total Error

Adding up all the 16 errors (14 systematic errors, 1 statistical error, and the unfolding error) in quadrature gives the total uncertainty in the cross section measurement.

The individual contribution of each error towards the total uncertainty was also estimated. We do this by taking the ratio of the integral of an individual error over the range of true energy spectrum to the total integral of the unfolded true energy spectrum. Table 4.2 lists the individual error contribution thus calculated and also the total error.

### 4.10 The \( \bar{\nu} \) Neutral Current Elastic Differential Cross-section

As explained in §4.1, the differential cross section is measured in terms of the momentum transfer squared to the nucleon, \( Q^2 \). In MiniBooNE \( Q^2 \) is is the total kinetic energy of the outgoing nucleons in the interaction, assuming the target nucleon is at rest viz.

\[ Q^2 = 2M_N \sum_i T_i = 2M_N T, \]  

(4.15)
<table>
<thead>
<tr>
<th>Type of Error</th>
<th>Source of error</th>
<th>value %</th>
</tr>
</thead>
<tbody>
<tr>
<td>Statistical</td>
<td></td>
<td>6.3</td>
</tr>
<tr>
<td>Flux</td>
<td>POT</td>
<td>1.7</td>
</tr>
<tr>
<td></td>
<td>Beam</td>
<td>2.9</td>
</tr>
<tr>
<td></td>
<td>$K^0$ production in the target</td>
<td>0.1</td>
</tr>
<tr>
<td></td>
<td>$K^+$ production in the target</td>
<td>0.3</td>
</tr>
<tr>
<td></td>
<td>$\pi^-$ production in the target</td>
<td>4.7</td>
</tr>
<tr>
<td></td>
<td>$\pi^+$ production in the target</td>
<td>0.1</td>
</tr>
<tr>
<td></td>
<td>WS estimation</td>
<td>3.5</td>
</tr>
<tr>
<td>Cross section</td>
<td>Hadronic interactions</td>
<td>2.9</td>
</tr>
<tr>
<td></td>
<td>Cross-section (backgrounds)</td>
<td>3.1</td>
</tr>
<tr>
<td></td>
<td>Dirt estimation</td>
<td>1.7</td>
</tr>
<tr>
<td>Detector</td>
<td>Discriminator threshold</td>
<td>1.1</td>
</tr>
<tr>
<td></td>
<td>Charge-time PMT response</td>
<td>1.8</td>
</tr>
<tr>
<td></td>
<td>Optical Model</td>
<td>15.0</td>
</tr>
<tr>
<td>Unfolding</td>
<td></td>
<td>7.3</td>
</tr>
<tr>
<td>Total</td>
<td></td>
<td>21.0</td>
</tr>
</tbody>
</table>

Table 4.2: Individual error contributions to the total antineutrino NCE scattering cross section error.

where $M_N$ is the nucleon mass and $T$ is the sum of the kinetic energies of the final state nucleons (the summation index $i$ goes over the final state particles). Experimentally, $\sum T_i$ is proportional to the total visible energy deposited in the PMTs in the detector.

All that is left to do is to calculate the last few ingredients that go into the differential cross section formula, namely:

- Number of target nucleons, $N^{\text{tar}}$

  This is calculated as $N^{\text{tar}} = N_A \rho_{\text{oil}} (4\pi R^3 / 3)$ where $N_A$ is Avogadro’s number, $\rho_{\text{oil}} = 0.845 \pm 0.001$ g/cm$^3$, and $R = 610.6$ cm (MiniBooNE detector radius). Since the error on $N^{\text{tar}}$ is negligible (0.3%) as compared to the other errors we do not assign an error on it. See §4.7.

- Number of protons on target ($N_{\text{POT}}$)

  This corresponds to $10.1 \times 10^{20}$ for the data set.
• Integrated neutrino flux ($\int \Phi dE_\nu$)

This is the total integrated neutrino flux for $\bar{\nu}_\mu$ and $\bar{\nu}_e$

Putting it all together, the flux-integrated differential cross section is given by:

$$\frac{d\sigma^{\bar{\nu}\text{NCE}}_i}{dQ^2} = \frac{\sigma_i / (dQ^2/dT_N \Delta T_N)}{N^{\text{tar}} N^{\text{POT}} \int \Phi dE_\nu}$$

(4.16)

where $\sigma_i$ is the number of entries in the $i^{th}$ bin of the unfolded kinetic energy distribution; $dQ^2/dT_N = 2M_N = 1.877$ GeV, and $\Delta T_N = 0.018$ GeV is the bin width of the unfolded kinetic energy distribution.

Figure 4.18 shows the MiniBooNE antineutrino nucleon NCE scattering cross section. The uncertainties include both systematic and statistical errors. Even though the systematic errors are mostly scaling errors, they do show bin by bin variation in case of certain errors. For instance, the optical model has large uncertainties in the low $Q^2$ region, while the flux error has large uncertainties in the high $Q^2$ region.
Also shown in Fig. 4.18, is the previous measurement of this cross section done by the BNL E734 experiment [62]. The two measurements are not directly comparable, since they represent flux-averaged cross sections with different average neutrino energies. The BNL E734 antineutrino beam had an average energy of about 1.2 GeV, as compared to the MiniBooNE antineutrino beam of approximately 0.6 GeV. The higher BNL E734 beam energy is the reason for the higher cross section. (Note that the errors in the BNL E734 measurement shown in Fig. 4.18 have been calculated from Tables VIII, IX, and X in Ref. [62].)

The MiniBooNE target is essentially CH$_2$, which implies that the antineutrino NCE scattering cross section includes three different processes:

1. the antineutrino scattering off free protons in the hydrogen atom,
2. the antineutrino scattering off bound protons in the carbon atom and

3. the antineutrino scattering off bound neutrons in the carbon atom,

Therefore, the MiniBooNE $\bar{\nu}N \rightarrow \bar{\nu}N$ cross section is expressed as:

$$
\frac{d\sigma_{\bar{\nu}N \rightarrow \bar{\nu}N}}{dQ^2} = \frac{1}{7} \frac{d\sigma_{\bar{\nu}p \rightarrow \bar{\nu}p,H}}{dQ^2} + \frac{3}{7} \frac{d\sigma_{\bar{\nu}p \rightarrow \bar{\nu}p,C}}{dQ^2} + \frac{3}{7} \frac{d\sigma_{\bar{\nu}n \rightarrow \bar{\nu}n,C}}{dQ^2}
$$

where each individual term is the cross section per nucleon.
4.11 Antineutrino to Neutrino Neutral Current Cross-Section Ratio

MiniBooNE has already reported the neutrino nucleus neutral current scattering cross section using the world’s largest data sample of such events [60]. This unprecedented statistics allowed the measurement of a differential cross section. The antineutrino cross section reported here also represents the largest sample of such events collected to date. Since both measurements were made in the same beamline, with the same detector and using the same analysis software, we expect that many of the systematic errors are common to both. A bin-by-bin ratio of the two cross section measurements would result in cancellation of the common systematic errors. The resulting cross section ratio plot would encompass information from both the neutrino and antineutrino NCE scattering cross section while minimizing the errors. One of the main motivations for measurement of this cross section is to better understand and model the neutrino nucleon interactions. We believe that such a ratio measurement where the errors are carefully accounted for would aid the theoretical physics community to test the various models.

4.11.1 The Data Set

The data set for the ratio measurement consists of the entire neutrino mode and antineutrino mode neutral current cross section data. This consists of 94,531 neutrino-nucleon neutral current elastic candidate events which passed the selection cuts corresponding to $6.46 \times 10^{20}$ POT. In the antineutrino mode, a total $10.1 \times 10^{20}$ POT was collected resulting in some 60,605 events that pass the selection cuts. Figure 4.19 shows both the neutrino and the antineutrino cross sections as a function of same $Q^2$ bins.
4.11.2 Error Estimation

In order to account for the errors in the ratio of antineutrino to neutrino cross section, we divide the errors into two classes, namely correlated errors and uncorrelated errors.

4.11.2.1 Correlated errors

Correlated errors are those errors which are common to both the neutrino and antineutrino modes. These include: the POT error, beam error, \( K^0 \) production error, \( K^\pm \) production error, \( \pi^\pm \) production error, hadronic interactions, cross-section, \( \pi^0 \) yield error, discriminator threshold error, charge-time PMT response error, and the optical model error. For a detailed description of the stated errors see §4.7.

To estimate the error, we employ the same *multisim* method described in §4.8. First we obtain the unfolded true energy spectrum for each \( k \)–th multisim for both the antineutrino

![Figure 4.19: A bin-by-bin comparison of the neutrino and antineutrino NCE scattering differential cross sections.](image)
and neutrino modes:

\[
\sigma_{i}^{k,\bar{\nu}} = \sum_{j} U^{k,\bar{\nu}}_{i,j} D_{j}^{\bar{\nu}} \frac{S_{j}^{k,\bar{\nu}}}{S_{j}^{k,\bar{\nu}} + B_{j}^{k,\bar{\nu}}} \quad \text{and} \quad \sigma_{i}^{k,\nu} = \sum_{j} U^{k,\nu}_{i,j} D_{j}^{\nu} \frac{S_{j}^{k,\nu}}{S_{j}^{k,\nu} + B_{j}^{k,\nu}},
\]

(4.17)

where the superscripts \( \bar{\nu} \) and \( \nu \) denote antineutrino and neutrino, \( i \) is the bin of true energy, \( j \) is the bin of reconstructed energy, \( U^{k}_{i,j} \) is the unfolding matrix for the \( k \)-th multisim, \( D \) is the data, \( S \) the signal, and \( B \) backgrounds.

In the above unfolding procedure, the \( k \)-th multisim denotes the same variation of MC parameters in both modes – antineutrino and neutrino. Thus, the unfolded spectrum for the ratio is:

\[
\sigma_{i}^{k,\bar{\nu}/\nu} = \frac{\sigma_{i}^{k,\bar{\nu}}}{\sigma_{i}^{k,\nu}}.
\]

(4.18)

The CV unfolded spectrum for the ratio is

\[
\sigma_{i}^{CV,\bar{\nu}/\nu} = \frac{\sigma_{i}^{CV,\bar{\nu}}}{\sigma_{i}^{CV,\nu}},
\]

(4.19)

where we use the same unfolding procedure as for the multisims, except now it is just for the one “best-estimate” or central value.

For each of the correlated errors, the error matrix is evaluated as:

\[
E_{i,j}^{\bar{\nu}/\nu} = \sqrt{\frac{1}{N} \sum_{k=1}^{N} \left( \sigma_{i}^{k,\bar{\nu}/\nu} - \sigma_{i}^{CV,\bar{\nu}/\nu} \right)^{2}},
\]

(4.20)

where \( N \) is the number of MC variations for each multisim.

### 4.11.2.2 Uncorrelated errors

The uncorrelated errors, which include the dirt estimation error, the unfolding error, and the WS estimation error, do not cancel out in the ratio. In order to estimate the uncorrelated error contribution to the total error in the ratio measurement, first the individual
uncorrelated error in each mode is estimated:

\[
E_{\bar{\nu}} = \sqrt{\frac{1}{N} \sum_{k=1}^{N} (\sigma_{k,\bar{\nu}} - \sigma_{CV,\bar{\nu}})^2} \quad \text{and} \quad E_{\nu} = \sqrt{\frac{1}{N} \sum_{k=1}^{N} (\sigma_{k,\nu} - \sigma_{CV,\nu})^2}.
\] (4.21)

Then, we use the formula for error propagation in a ratio where there is no correlation between the individual errors:

\[
E_{\bar{\nu}/\nu} = \sqrt{\left(\frac{\sigma_{CV,\bar{\nu}}}{\sigma_{CV,\nu}}\right)^2 \left[\left(\frac{E_{\bar{\nu}}}{\sigma_{CV,\bar{\nu}}}ight)^2 + \left(\frac{E_{\nu}}{\sigma_{CV,\nu}}\right)^2\right]}.
\] (4.22)

The total error on the ratio is evaluated by adding each of the \(E_{\bar{\nu}/\nu}\)’s in quadrature. Table 4.3 shows the individual and total error, in the antineutrino mode, the neutrino mode, and the ratio of the two modes.

<table>
<thead>
<tr>
<th>Type of Error</th>
<th>Source of error</th>
<th>(\bar{\nu}) mode</th>
<th>(\nu) mode</th>
<th>ratio</th>
</tr>
</thead>
<tbody>
<tr>
<td>Statistical</td>
<td></td>
<td>6.3</td>
<td>3.1</td>
<td>6.9</td>
</tr>
<tr>
<td>Flux</td>
<td>POT</td>
<td>1.7</td>
<td>1.8</td>
<td>0.0</td>
</tr>
<tr>
<td></td>
<td>Beam</td>
<td>2.9</td>
<td>4.7</td>
<td>7.3</td>
</tr>
<tr>
<td></td>
<td>(K^0) production in the target</td>
<td>0.1</td>
<td>0.1</td>
<td>0.1</td>
</tr>
<tr>
<td></td>
<td>(K^+) production in the target</td>
<td>0.3</td>
<td>0.1</td>
<td>0.4</td>
</tr>
<tr>
<td></td>
<td>(\pi^-) production in the target</td>
<td>4.7</td>
<td>0.1</td>
<td>4.7</td>
</tr>
<tr>
<td></td>
<td>(\pi^+) production in the target</td>
<td>0.1</td>
<td>4.1</td>
<td>4.6</td>
</tr>
<tr>
<td></td>
<td>WS estimation</td>
<td>3.5</td>
<td>0.0</td>
<td>4.0</td>
</tr>
<tr>
<td>Cross section</td>
<td>Hadronic interactions</td>
<td>2.9</td>
<td>4.2</td>
<td>5.9</td>
</tr>
<tr>
<td></td>
<td>Cross-section (backgrounds)</td>
<td>3.1</td>
<td>3.4</td>
<td>5.9</td>
</tr>
<tr>
<td></td>
<td>Dirt estimation</td>
<td>1.7</td>
<td>1.7</td>
<td>2.3</td>
</tr>
<tr>
<td>Detector</td>
<td>Discriminator threshold</td>
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<td>1.6</td>
<td>1.4</td>
</tr>
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<td></td>
<td>Charge-time PMT response</td>
<td>1.8</td>
<td>2.3</td>
<td>2.1</td>
</tr>
<tr>
<td></td>
<td>Optical Model</td>
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<td>15.0</td>
<td>6.6</td>
</tr>
<tr>
<td>Unfolding</td>
<td></td>
<td>7.3</td>
<td>8.3</td>
<td>15.0</td>
</tr>
<tr>
<td>Total</td>
<td></td>
<td>21.0</td>
<td>25.0</td>
<td>25.0</td>
</tr>
</tbody>
</table>

Table 4.3: NCE scattering cross section errors for the neutrino mode, the antineutrino mode, and the ratio.
4.11.3 Result

The bin-by-bin ratio of the antineutrino NCE cross section to the neutrino NCE cross section was made and is shown in Fig 4.20. The correlated and uncorrelated errors were estimated and are also shown in the same plot. The ratio measurement cancels out many of the systematic errors. Statistical fluctuations account for the residual error in those systematics which are fully correlated. Also shown in Fig. 4.20 are MC predictions for different values of $M_A$ and $\kappa$. We note that the ratio is relatively independent of variations in $M_A$ and $\kappa$.

![Figure 4.20: Ratio of antineutrino to neutrino NCE scattering cross section in MiniBooNE with total error (grey band). The predicted ratio from MC simulations with different $M_A$ and $\kappa$ values is shown superimposed. Also shown is the calculated ratio of antineutrino to neutrino NCE scattering cross section from the BNL E734 experiment (brown) [62] with the errors in the two modes added in quadrature. This overestimates the error in the ratio for the BL E734 measurement as many systematic errors are expected to be correlated and hence cancel.](image)

An antineutrino to neutrino differential cross section ratio plot for the BNL E734 experiment was generated from Fig. 35 from Ref. [62] and overlaid on the MiniBooNE ratio
measurement in Fig. 4.20. The errors on the BNL E734 experiment are overestimated as the errors in the individual neutrino and antineutrino measurement have been added in quadrature. Many systematic errors would cancel in the case of BNL E734 experiment just as in the MiniBooNE measurement.

We note that the BNL E734 ratio measurement is higher than the MiniBooNE measurement. However, as previously stated, the two experiments are not strictly comparable; the different ratio of the antineutrino to neutrino average beam energies in the BNL E734 and MiniBooNE results in different cross section ratios. For the BNL E734 experiment the average neutrino and antineutrino beam energies were about 1.3 GeV and 1.2 GeV, respectively, whereas in MiniBooNE the average neutrino and antineutrino beam energies were approximately 0.8 GeV and 0.6 GeV, respectively.

The MiniBooNE antineutrino NCE cross section measurement allows us to make a direct comparison to the neutrino mode NCE cross section measurement made by MiniBooNE, which was done using the same target and beamline, but with the opposite polarity of the magnetic focusing horn.
4.12 Axial Vector Mass Measurement

One of the parameters in the antineutrino-nucleus neutral current cross section is the axial vector mass, $M_A$. As discussed in §2.4, measurements made by deuterium-based bubble chamber experiments have reported a value of $M_A = 1.026 \pm 0.021$ GeV. However recent experiments on nuclear targets (such as MiniBooNE with a CH$_2$ target) have reported $M_A$ values which are about 20–30% higher. In the the CCQE channel MiniBooNE reported a value of $M_A = 1.35 \pm 0.17$ GeV [59] and the neutrino mode NCE analysis reported a value of $M_A = 1.39 \pm 0.11$ GeV [60], consistent with that from the CCQE channel.

In this section we attempt a $\chi^2$-fit to the antineutrino neutral-current data, to extract the value of $M_A$ which best describes it. In principle, one needs to fit the observed cross section data to the cross section MC prediction for different values of $M_A$ in $Q^2$ bins. However, we can exploit the relation between the momentum transfer and the nucleon kinetic energy in MiniBooNE NCE interactions, $Q^2 = 2M_N T_N$ to do the fitting in bins of reconstructed energy instead of $Q^2$. This avoids the unfolding procedure and the associated unfolding error. In order to account for the uncertainties, both systematic and statistical, we also construct an error matrix which is used in the fitting procedure.

For this study, the data sample has the standard NCE cuts and background subtraction procedure as described in §4.3 and §4.5, respectively. A reweighting procedure was used to generate antineutrino NCE signal MC with different values of $M_A$ and $\kappa$.

Figure 4.21 shows the MC with different values of $M_A$ compared to data in the reconstructed energy variable. We see that $M_A$ changes the overall normalization of the spectrum with minimal shape variation. In Fig. 4.22 we see data compared to MC with different $\kappa$ values. $\kappa$ denotes a Pauli blocking scaling parameter which modifies the shape of the spectrum at low $Q^2$ while the normalization is unchanged.
Figure 4.21: Absolutely normalized reconstructed energy spectra for antineutrino NCE data and MC with different $M_A$ values and $\kappa = 1.022$.

Figure 4.22: Absolutely normalized reconstructed energy spectra for antineutrino NCE data and MC with different $\kappa$ values and $M_A = 1.23\text{ GeV}$.

4.12.1 Error Matrix

To generate the error matrix which has the information of the systematic and statistical uncertainties we use the method of *multisims* as described before §4.8. For each each $k$-th
multisim we generate a value of the reconstructed energy $T$:

$$T_i^k = D_i \frac{S_i^k}{S_i^k + B_i^k}, \quad (4.23)$$

where $i$ is the bin of reconstructed energy, $D$ is the data, $S$ the signal, and $B$ backgrounds.

For each of the error we calculate the error matrix as:

$$M_{i,j} = \frac{1}{N} \sum_{k=1}^{N} (T_i^k - T_{CV}^k) (T_j^k - T_{CV}^k), \quad (4.24)$$

where $i, j = 1, \ldots, n$ number of reconstructed energy bins, $N$ is the number of MC variations in the multisim, and $T^k$ is the $k$-th multisim and $T_{CV}$ is the CV.

The total error matrix ($M_{i,j}^{tot}$) is the sum of the 15 systematic and one statistical error matrices. Table 4.4 shows the list of the errors along with the normalization error for each error, which was evaluated as:

$$Error^N = \sqrt{\sum_{i,j} M_{i,j}}. \quad (4.25)$$

<table>
<thead>
<tr>
<th>Source of error</th>
<th>value %</th>
</tr>
</thead>
<tbody>
<tr>
<td>Beam</td>
<td>3.4</td>
</tr>
<tr>
<td>K$^+$ production in the target</td>
<td>0.3</td>
</tr>
<tr>
<td>π$^-$ production in the target</td>
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<tr>
<td>POT</td>
<td>1.8</td>
</tr>
<tr>
<td>Cross-section (backgrounds)</td>
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</tr>
<tr>
<td>Optical Model</td>
<td>18.0</td>
</tr>
<tr>
<td>Dirt estimation</td>
<td>1.7</td>
</tr>
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<td>WS estimation</td>
<td>4.9</td>
</tr>
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<td>Statistical</td>
<td>7.6</td>
</tr>
<tr>
<td>Discriminator threshold</td>
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</tr>
<tr>
<td>Charge-time PMT response</td>
<td>2.9</td>
</tr>
<tr>
<td><strong>Total</strong></td>
<td><strong>24.5</strong></td>
</tr>
</tbody>
</table>

**Table 4.4:** Individual normalization errors and the total normalization error.
4.12.2 Simultaneous $M_A$ and $\kappa$ Fit

In order to perform a simultaneous $M_A$ and $\kappa$ fit to MiniBooNE data, we first generate the reconstructed MC spectrum corresponding to different combinations of $M_A$ and $\kappa$. For this fit we choose 54 values of $M_A$ from 1.00 GeV to 1.54 GeV, and 54 values of $\kappa$ from 1.00 to 1.054. The $\chi^2$ is calculated as:

$$
\chi^2(M_A, \kappa) = \sum_{i=1}^{n} \sum_{j=1}^{n} \left[ T_{i}^{MC}(M_A, \kappa) - T_{i}^{Data} \right] (M_{ij}^{tot})^{-1} \left[ T_{j}^{MC}(M_A, \kappa) - T_{j}^{Data} \right], \tag{4.26}
$$

where $(M_{ij}^{tot})^{-1}$ is the inverse of the total error matrix evaluated in §4.11.1. The result of the $\chi^2$-fit for 25 degrees of freedom is shown in Fig. 4.23 below. The best fit value of the $\chi^2$ corresponds to an $M_A = 1.29 \pm 0.02$ GeV and $\kappa = 1.026 \pm 0.02$.

We also looked at the following values of $M_A$ and $\kappa$ which are of special interest:

- $M_A = 1.02$ and $\kappa = 1.000$, the world average value of these parameters from deuterium-based bubble chamber experiments,
\( M_A = 1.39 \) and \( \kappa = 1.000 \), which was the result from the neutrino mode NCE scattering measurement [60], and

\( M_A = 1.35 \) and \( \kappa = 1.007 \), which was the result from the neutrino mode CCQE scattering measurement [59].

Figure 4.24 shows the reconstructed energy spectrum with errors, along with the three different values of \( M_A \) and \( \kappa \), mentioned above. We see that at low energies, a higher \( M_A \) agrees with the antineutrino NCE scattering data, however at higher energies there is disagreement between data and previous \( M_A \) measurements in the neutrino mode. When the antineutrino NCE scattering data is compared to the world-average values of \( M_A \) and \( \kappa \), there is significant difference in normalization at low energies.

Overall we see the antineutrino NCE scattering data agrees with a high value of \( M_A \) as compared to the world-average, which is consistent with previous measurements in the neutrino mode NCE scattering and CCQE scattering. However, the shape of the antineutrino NCE scattering spectrum is not reproduced by either the world-average value or the neutrino mode MiniBooNE measurements, which is reflected in the poor values of \( \chi^2 \) for those values of \( M_A \) and \( \kappa \).
Figure 4.24: $\bar{\nu}$ NCE reconstructed energy spectrum with the total normalization error. Also shown are three different values of $M_A$: 1.35, 1.39, and 1.02. The $\chi^2$ values are 78.9, 107.6, and 177.0 for 25 DOF, respectively. The distributions are absolutely normalized.
Chapter 5

Conclusions

One of the main goals of the next-generation neutrino experiments is to test the three neutrino flavor paradigm by obtaining high-precision values of the neutrino oscillation parameters. Accelerator-based neutrino experiments play an important role in testing the oscillation model, as both the neutrino energy and oscillation length can be relatively well controlled. However, there is a dearth of neutrino (and antineutrino) cross section information in the energy region important for accelerator-based neutrino experiments [111]. The CCQE channel is an important signal interaction for the oscillation physics and there is a discrepancy between the low (1 GeV) energy regime, reported by MiniBooNE [59] and the high (3 GeV) region, as reported by NOMAD [112]. Recent results from the MiniBooNE neutrino CCQE scattering measurement and the neutrino NCE measurements point to an enhancement, with many possible theoretical explanations [40, 41, 42, 43, 44, 45].

As most of the new generation of accelerator-based neutrino detectors are made of nuclear targets such as carbon, there is an urgent need to understand the neutrino nuclear interactions. The NCE channel provides an important cross check to the CCQE channel measurement as both have similar nuclear effects and cross section formula, furthermore NCE interactions provide information on nucleon kinematics in the experiment.

This thesis reports the antineutrino-nucleus neutral current scattering cross section ( Chap-
The data set consists of 60,605 events passing the selection cuts corresponding to $10.1 \times 10^{20}$ POT, which represents the world’s largest sample of such events. The final sample is more than one order of magnitude larger than the previous antineutrino NCE scattering cross section measurement reported by the BNL E734 experiment. Furthermore, the measurement presented in this dissertation spans a wider range in $Q^2$, including the low-$Q^2$ regime where the cross section rollover is clearly visible.

A $\chi^2$-based minimization was performed to determine the best value of $M_A$ and $\kappa$ that matches the antineutrino NCE scattering data. However, the best fit values of $M_A=1.29$ GeV and $\kappa=1.026$ still give a relatively poor $\chi^2$, which suggests that the underlying nuclear model (based largely on the relativistic Fermi gas model) may not be an accurate representation for this particular interaction.

Additionally, we present a measurement of the antineutrino/neutrino-nucleus NCE scattering cross section ratio. The neutrino mode NCE sample used in this study, corresponding to $6.4 \times 10^{20}$ POT, is also the world’s largest sample (also by an order of magnitude). We have demonstrated that the ratio measurement is robust, as most of the correlated errors cancel, as expected. Furthermore, this ratio also proves to be rather insensitive to variations in the axial mass and the Pauli blocking parameter. This is the first time that this ratio has been experimentally reported. We believe this measurement will aid the theoretical physics community to test various model predictions of neutrino-nucleon/nucleus interactions.

In Appendix A, we discuss a possibility of searching for a light (MeV-scale) dark matter candidate events which can appear in the neutral-current nucleon scattering sample. Currently, most searches for dark matter are looking for a weakly interacting massive particle (WIMP) of GeV-scale mass. However, a MeV-scale dark matter particle is theoretically equally probable.
Appendix A

Search for a *light* dark matter particle at MiniBooNE

A.1 Introduction

Recently there have been a number of publications exploring the sensitivity of fixed-target neutrino experiments to MeV-scale dark matter candidates [113, 114]. Many of these models look for non-gravitational interaction signatures which are of particular interest to particle physics. Light dark matter candidates or mediator particles, that annihilate, scatter or decay, have been explored to explain anomalous experimental observations. [115, 116].

An interesting consequence of models with light (sub-GeV) dark matter is the production of high intensity “dark matter beam”, generated as dark matter particles are pair-produced as a result proton-target interactions and boosted along the beam direction. The ensuing scattering of these light dark matter would manifest as an excess over the known neutral-current type scattering events.
Figure A.1: Tree-level annihilation (left) and scattering (right) of scalar dark matter in the U(1)′ hidden sector.

A.2 MiniBooNE Neutral Current Interactions

A recent paper [117] is of particular interest. In this analysis the authors explore a class of MeV-scale dark matter models, originally used to explain the strength of 511 keV emission from the galactic center [118].

The authors employ a modified Lagrangian:

\[
\mathcal{L}_{V,\chi} = -\frac{1}{4} V_{\mu\nu}^2 + \frac{1}{2} m_v^2 V_{\mu}^2 + \kappa V_{\mu} \partial_\mu F^{\nu\mu} + |D_\mu \chi|^2 - m_\chi^2 |\chi|^2 + \mathcal{L}_{h'}
\]  

(A.1)

which assumes a hidden sector charged under a U(1)′ gauge group, with a vector portal coupling to the SM via kinetic mixing [119], which is spontaneously broken at a low scale by a Higgs’ sector leading to a mass for the vector mediator \( V_\mu \). The model has four parameters: \( m_\chi, m_V \)-the masses of the dark matter candidate and its vector mediator, the U(1)′ gauge coupling \( e' \), and the kinetic mixing coefficient \( \kappa \).

The annihilation of the dark matter candidate \( \chi \) is given by the diagram in Fig.A.1 (left). Rotating the diagram gives and corresponding scattering rate off electrons and nucleons in Fig.A.1 (right) which can, in principle, be used to detect the dark matter candidate. A dark matter beam can be produced via the following processes (as taken from Ref. [117], where some of the emerging particles have been suppressed), for a small \( m_V \):

1. \( p + p \rightarrow X + \pi^0, \eta \)
2. \( \pi^0, \eta \rightarrow \gamma + V \)
3. $V \rightarrow 2\chi$

and may be detected through neutral current-like processes with electrons or nucleons:

1. $e + \chi \rightarrow e + \chi$

2. $N + \chi \rightarrow N + \chi$

By calculating the number of dark matter neutral current-like scattering events that would be expected at MiniBooNE and comparing it to the actual number, from the neutrino-nucleon data [60], and estimating the number of neutrino-electron scattering events, the authors were able to probe the parameter space of this model. The sensitivity is limited due to the fact that the authors had to estimate the rate of electron scattering in MiniBooNE which has not been published. The results are shown in Fig. 4.

![Figure A.2: Expected number of neutral current-like dark matter nucleon scattering events at MiniBooNE. The regions represent greater than 10 (light), 1000 (medium) and $10^6$ (dark) expected events for $m_\chi = 1$ MeV. The black line corresponds to a particular value of $\kappa$ and the dotted line indicates the total number of neutrino events observed. Figure from Ref. [117]](image)
A.3 Plan of the Project

We propose to do a search for light (∼ 1 MeV scale) dark matter at the MiniBooNE experiment. The analysis will be along similar lines as discussed in §A.2.

First we will calculate the number dark matter of neutral current-like scattering events expected at MiniBooNE detector, following [117] and compare it to the total number of such events actually observed. The sample would include:

1. all neutrino-nucleus and antineutrino-nucleus scattering data collected by MiniBooNE up to May 2011.

2. hitherto unpublished electron scattering data, again both neutrino-electron and antineutrino-electron scattering data accumulated in the same run period as above. (MiniBooNE has the ability to identify electron scattering events, see [120] for details)

We believe that by looking at a larger sample of neutral current-like events and having access to accurate detector efficiency information, we will be able to probe a larger region of the parameter space described in this model.

Possibility of using time of flight

Assuming that some neutral current scattering events are due to massive dark matter particles as opposed to (almost) massless neutrinos, there will be a time difference between such scattering events and those caused by neutrinos. The (more) massive dark matter candidates would likely cause scattering events after the neutrino beam has arrived at the detector.

MiniBooNE employs a resistive wall monitoring (RWM) system which gives us accurate information of beam arrival time to the detector. We propose to exploit the excellent timing resolution of the MiniBooNE detector (∼ 2 ns) to look for any potential accompanying dark matter beam by looking for late events within the beam window. See [70] for a description of the timing resolution of MiniBooNE detector.
A.4 Conclusion

The proposed dark matter search in MiniBooNE opens an exciting experimental avenue to search for the hidden sector. It would also help in excluding exotic models as we look for beyond standard model physics.
References


[64] E. Church et al., “A letter of intent for an experiment to measure \nu_\mu \rightarrow \nu_e oscillations and nu/mu disappearance at the Fermilab booster: BooNE,” 1997.


